

VALIDATION OF HIGH STRAIN RATE, MULTIAXIAL LOADS  
USING AN IN-PLANE LOADER, DIGITAL IMAGE CORRELATION, AND FEA

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## ABSTRACT

Montana State University's In-Plane Loader (IPL) is a machine designed to test for mechanical properties at multi-axial states of stress and strain by in-plane translation and rotation. Historically the machine has been used to characterize composite lay-ups, where applying multi-axial loads can better describe anisotropic materials. The IPL testing machine uses Digital Image Correlation (DIC) software and a stereoscopic camera system to measure strains on the surface of the test coupon by tracking a stochastic pattern applied to the gage section.

The focus of this work was to test the capabilities beyond quasi-static composites testing, specifically looking to explore the feasibility of testing plastics and metals at strain rates from  $10^0$  to  $10^3 \text{ s}^{-1}$ . This work explored the speed and loading capabilities of the IPL and determined a suitable coupon geometry which balances gage section area with material strength. 304 Stainless Steel was tested both on the IPL and in uniaxial tension. Experimental tensile test data was fit to a Johnson Cook strain rate sensitive constitutive model. This constitutive equation was then used with an implicit dynamic finite element analysis (FEA) model. To study the validity of high rate testing of steel in the IPL, strain from the DIC experimental data was compared with the FEA results. While the strains predicted by the FEA model varied from experimental results, a better understanding of the IPL capabilities has been achieved. Moving forward, a series of recommendations have been made so that high strain rate multi-axial testing of metals can be implemented with more robust constitutive models.

## INTRODUCTION

### Motivation

In order to classify a materials behavior their material properties must be determined. Tests for intrinsic material properties such as elastic modulus ( $E$ ), shear modulus ( $G$ ), and Poisson's ratio ( $\nu$ ) are carried out in pure tension or shear as to eliminate off axis loading. However, when parts are designed for use, rarely do loads act in pure tension or shear on the component. Multiaxial systems are utilized to experientially study non-ideal load cases. The In-Plane Loader (IPL), combined with Aramis Digital Image Correlation software (DIC) allows for a user to study the effects of a complex loading path, while outputting force, displacement, and strain data, with minimal post processing.

In the interest of developing a better understanding of materials experiencing multi-axial loads under elevated strain rates. The objectives of this research project are:

1. Validate the in-plane loaders ability to characterize behavior of strain rate sensitive materials under multiaxial loading.
2. Develop a method to compare data collected by the In-Plane Loader and digital image correlation with results obtained using finite element analysis software.
3. Provide input for the next iteration of the In-Plane Loader.

### Elastic and Plastic Deformations

When designing parts and assemblies, it is desirable to stay within materials elastic limits. Within a material's elastic regime, its stress and strain curve behaves in a predictable, linear manner as seen in Figure 1.

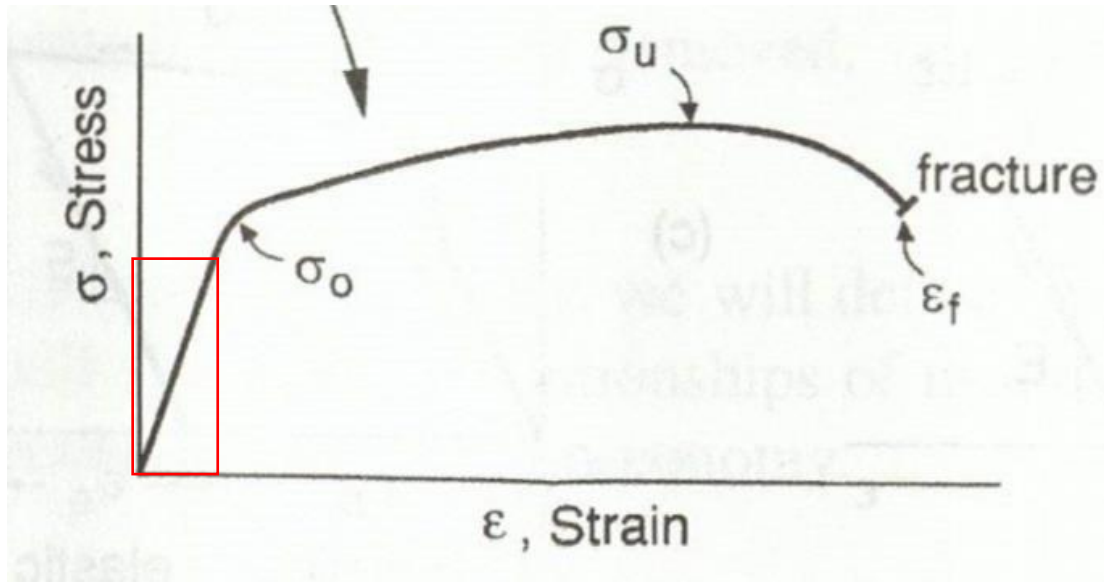


Figure 1. Stress/Strain curve with linear elastic region highlighted in red box.<sup>1</sup>

For an isotropic material, under a uniaxial load the behavior is like a linear spring. This relationship is shown below (eqn. 1) in the tensor notation form.

$$\sigma_{ij} = C_{ijkl}\epsilon_{kl} \quad (1)$$

Elastic deformation does not involve the breaking of atomic or chemical bonds, but rather the stretching of the bonds [2]. Strain in the elastic regime is recovered when the

<sup>1</sup> 1. Dowling, N.E., *Mechanical Behavior of Materials*. Fourth ed. 2013, Upper Saddle River, NJ: Pearson. 936.

applied load is removed. Unlike plasticity or creep, this deformation is independent of loading rates or time [1].

When a material is placed under a load which exceeds its elastic limit, or yield stress, an inelastic deformation occurs, causing a permanent change in atomic configuration [2]. At this point a portion of the strain will remain in the material once the load is removed, typically this plastic strain is time independent, however certain materials will exhibit a time dependence [3]. In Mechanical Behavior of Materials, Dowling states that; “inelastic deformation that occurs nearly instantaneously as the stress is applied is known as plastic deformation”. This permanent deformation is caused by shear stress induced by the motion of dislocations in the material. This is described as an incremental process as atomic bonds are not broken simultaneously, but rather progress through the material [1].

### Strain Rate Sensitive Constitutive Models

#### Materials Tested

The material chosen for this study was 304 Stainless Steel. This was chosen as 304 SS can represent a wider variety of materials with interesting strain rate sensitive properties. The focus on stainless steel in this thesis was initially due to its strain rate sensitivity, to explore the IPL’s ability to characterize strain rate sensitive multi-axial loading. Adjustments to the materials geometries were made as testing progressed due to discovering limitations in the IPL’s gripping ability. Historically at Montana State University composite coupons were given a single notch to generate asymmetric strain fields. The high elastic modulus of stainless steel used in this study led to a double notch being used.

### Strain Rate Sensitive Plasticity (Viscoplastics)

Many plastics and metals exhibit work hardening or a change in the stress/strain slope,  $\frac{d\sigma}{d\epsilon}$ , when experiencing plastic deformation [3]. Historically understanding of high strain rate plastic deformation behavior was driven by ballistic research. An early study of the effectiveness of tank armor is show in Figure 2.

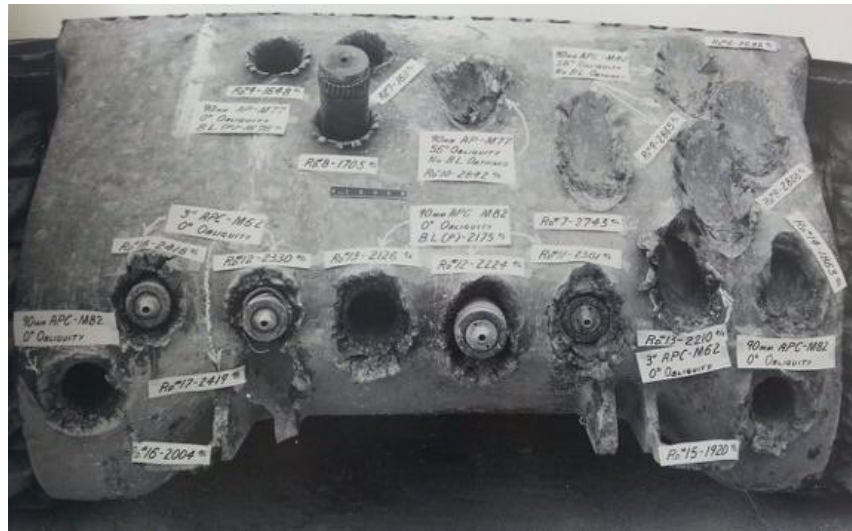


Figure 2. Studying the effects of ballistic impacts on tank armor during World War II.<sup>2</sup>

Furthermore, other relationships exist for work hardening. As temperature increases material softening will occur, as strain rate increases stiffening occurs [4]. These high temperature and strain rate conditions are both present in high speed impacts. This phenomenon is also highly dependent on the materials crystal structure. In 1929 F.H. Norton studied material flow rates at elevated temperatures, writing “It is only within a relatively few years that the importance of the time element in determining the useful

<sup>2</sup> <https://www.snafu-solomon.com/2017/12/m4a3e2-jumbo-out-armored-tiger-1s.html>

strength of steel at high temperatures” [5]. An example of this thermal softening can be seen in Figure 3.

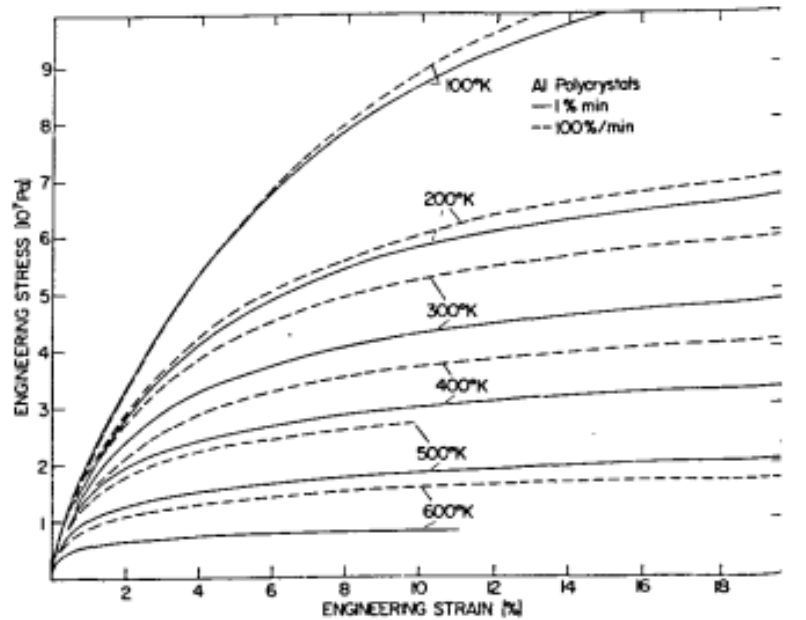


Figure 3. Plot created by U.F. Kocks illustrating temperature and strain rate dependence in aluminum.<sup>3</sup>

To analytically describe the behavior of solids often rheological models are used. These models consist of various combinations of springs, dashpots, and sliders [6]. With these analogues, equations can be derived that will incorporate plastic deformation, rate sensitivity, and temperature sensitivity to the materials behavior. Shames and Cozzarelli illustrate the rheological model for a rate-sensitive viscoplastic material by placing a Saint-Venant element (dry friction element) in parallel with a nonlinear Kelvin element (spring and dashpot in parallel)[6]. This is placed in series with a spring element, to account for

<sup>3</sup> 4. Kocks, U.F., *Laws for Work-Hardening and Low-Temperature Creep*. Journal of Engineering Materials and Technology, 1976. **98**(1): p. 76-85.

the elastic deformation in the material. The authors show that the Saint-Venant element forces these constraints. While useful, experimental testing and validation can provide a more accurate material model.

The IPL is unique in that it is capable of testing materials at speeds between quasi-static and ballistic impacts. An area which has not been covered in depth historically. Table 1 contains a range of strain rates, and where the IPL capabilities lie.

Table 1. Comparison of various material testing rates.

| Test Type                     | Test Rate                             |
|-------------------------------|---------------------------------------|
| Quasi-Static                  | $10^{-4}$ to $10^{-3} \text{ s}^{-1}$ |
| In-Plane Loader               | $10^{-2}$ to $10^0 \text{ s}^{-1}$    |
| Car Accident/Ballistic Impact | $10^2$ to $10^3 \text{ s}^{-1}$       |
| Explosives                    | $10^3$ to $10^5 \text{ s}^{-1}$       |

#### Work of Johnson-Cook

Published in 1985, Gordon R. Johnson of Honeywell Inc. Defense Systems Division, and William H. Cook of the Air Force Armament Laboratory, modeled the high strain rate and high temperature behavior of a variety of metals. Johnson and Cook highlight that under dynamic loading (impacts, explosions, and metal forming operations) high strain rates events additionally exhibit high temperatures and large strains [7]. The researchers tested from quasi static speeds up to high strain rates up to  $650 \text{ s}^{-1}$  in dynamic impacts. Johnson and Cook studied the effects of strain rate and temperature on oxygen-

free high thermal conductivity (OHFC) Copper, Armco Iron, 4340 steel, and nine other metals. For von Mises tensile flow stress, Johnson and Cook arrived at the analytic expression in Equation 3.

$$\sigma = [A + B\epsilon^n][1 + C\ln\dot{\epsilon}^*][1 - T^{*m}] \quad (2)$$

Here A is the materials yield stress; B is the strain-hardening constant (in units of stress). Strain is  $\epsilon$ , the strain hardening exponent is n, and the strain rate constant is C. Additionally,  $\dot{\epsilon}^* = \frac{\dot{\epsilon}}{\dot{\epsilon}_0}$  is a dimensionless plastic strain rate, a ratio where  $\dot{\epsilon}_0$  is an experimentally determined reference strain rate (typically  $1.0 \text{ s}^{-1}$ ), and  $\dot{\epsilon}$  is the plastic strain rate.  $T^*$  is the homologous temperature defined as  $\frac{T-T_0}{T_m-T_0}$ , where T is testing temperature,  $T_0$  is the reference temperature, and  $T_m$  is the materials melting temperature.

In Equation 2, the terms in the second and third terms are used to introduce strain rate and temperature dependence, respectively, to the materials stress vs. strain relationship. Johnson and Cook performed quasi-static tensile tests, biaxial torsion/tension tests, and Hopkinson bar tests to determine A, B, n, C, and m.

The Johnson-Cook model was then tested against a computational model, and cylinder impact tests, at strain rates exceeding  $10^5 \text{ s}^{-1}$ , the authors point out that the results show agreement among the tests performed. Results from the paper are shown below in Figure 4.

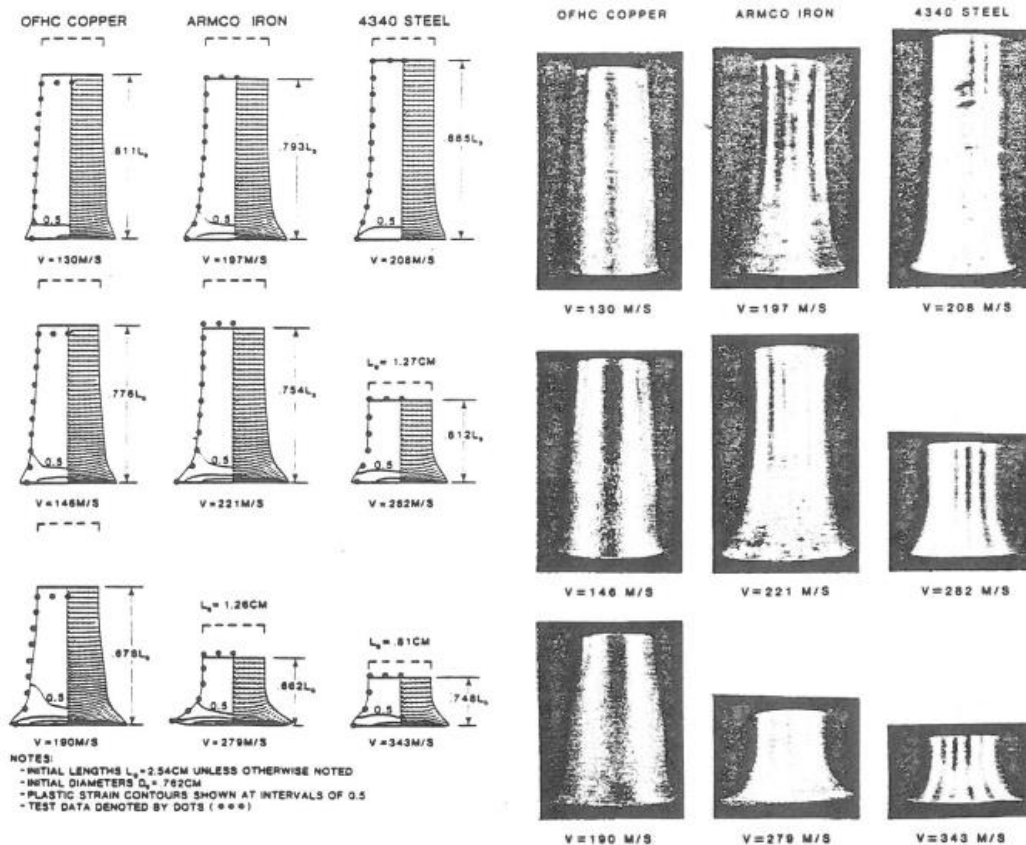


Figure 4. Johnson and Cook's comparison of their computational model to cylinder impact tests.<sup>4</sup>

The Johnson-Cook parameters for all materials tested by the researchers are shown below in Table 2.

<sup>4</sup> 7. Johnson, G.R., Cook, William H., *A Constitutive Model and Data for Metals Subjected to Large Strains, High Strain Rates and High Temperatures*. Proceedings: Seventh International Symposium on Ballistics, 1983. 7: p. 541-547.

Table 2. Johnson-Cook constants for a variety of metals, as determined by the researchers in 1983.<sup>5</sup>

| MATERIAL                    | DESCRIPTION            |                                 |                             |                               | CONSTITUTIVE CONSTANTS FOR<br>$\sigma = [A + B\epsilon^n][1 + C\ln\epsilon^*][1 + T^m]$ |            |     |      |      |
|-----------------------------|------------------------|---------------------------------|-----------------------------|-------------------------------|-----------------------------------------------------------------------------------------|------------|-----|------|------|
|                             | HARDNESS<br>(ROCKWELL) | DENSITY<br>(kg/m <sup>3</sup> ) | SPECIFIC<br>HEAT<br>(J/kgK) | MELTING<br>TEMPERATURE<br>(K) | A<br>(MPa)                                                                              | B<br>(MPa) | n   | C    | m    |
| OFHC COPPER                 | F-30                   | 8960                            | 383                         | 1356                          | 90                                                                                      | 292        | .31 | .025 | 1.09 |
| CARTRIDGE BRASS             | F-67                   | 8520                            | 385                         | 1189                          | 112                                                                                     | 505        | .42 | .009 | 1.68 |
| NICKEL 200                  | F-79                   | 8900                            | 446                         | 1726                          | 163                                                                                     | 648        | .33 | .006 | 1.44 |
| ARMCO IRON                  | F-72                   | 7890                            | 452                         | 1811                          | 175                                                                                     | 380        | .32 | .060 | 0.55 |
| CARPENTER ELECTRICAL IRON   | F-83                   | 7890                            | 452                         | 1811                          | 290                                                                                     | 339        | .40 | .055 | 0.55 |
| 1006 STEEL                  | F-94                   | 7890                            | 452                         | 1811                          | 350                                                                                     | 275        | .36 | .022 | 1.00 |
| 2024-T351 ALUMINUM          | B-75                   | 2770                            | 875                         | 775                           | 265                                                                                     | 426        | .34 | .015 | 1.00 |
| 7039 ALUMINUM               | B-76                   | 2770                            | 875                         | 877                           | 337                                                                                     | 343        | .41 | .010 | 1.00 |
| 4340 STEEL                  | C-30                   | 7830                            | 477                         | 1793                          | 792                                                                                     | 510        | .26 | .014 | 1.03 |
| S-7 TOOL STEEL              | C-50                   | 7750                            | 477                         | 1763                          | 1539                                                                                    | 477        | .18 | .012 | 1.00 |
| TUNGSTEN ALLOY(.07Ni,.03Fe) | C-47                   | 17000                           | 134                         | 1723                          | 1506                                                                                    | 177        | .12 | .016 | 1.00 |
| DU-.75Ti                    | C-45                   | 18600                           | 117                         | 1473                          | 1079                                                                                    | 1120       | .25 | .007 | 1.00 |

Using their equation for flow stress, Johnson and Cook conducted further research to determine the strain to fracture of the same materials. This research will not study the fracture behavior in depth, but it is worth noting that even in 1985 the authors mention their interest in studying complicated loading paths, such as the multi-axial loads produced by the IPL. Equation 3 is defined by the paper as strain to fracture

$$\epsilon^f = [D_1 + D_2 \exp(D_3 \sigma^*)][1 + D_4 \ln \epsilon^*][1 + D_5 T^*] \quad (3)$$

While this research paper will not cover fracture mechanics at high strain rates, it should be noted that this should be considered when further exploring future work using the IPL.

<sup>5</sup> 7. Ibid.

Work of Zerilli and Armstrong

Frank J. Zerilli and Ronald W. Armstrong's 1987 paper makes an attempt to offer an improved version of a strain rate and temperature sensitive constitutive relation [8]. The authors note that the flow stress of two of the materials Johnson and Cook tested: OFHC copper, and Armco iron, show different dependencies on strain rate and temperature. Noting that the OFHC copper shows a much higher strain dependence than the Armco iron. Zerilli and Armstrong explore the idea of dislocation mechanics to better describe constitutive relationships. Their first issue with existing theories is that cylinder impacts, which are commonly used in high strain rate testing, do not provide a detailed description of a materials strength. Dating back to 1947, a Taylor test shown in Figure 5, is sufficient in predicting the ratio of final length to initial length based on a projectiles kinetic energy [9].

This test, however it does not accurately work to model the shape of the deformed projectile. At the time, the authors saw a weakness in computer codes as they relied heavily on numerical fits, and they could not rely on these codes for predictions outside of existing data.

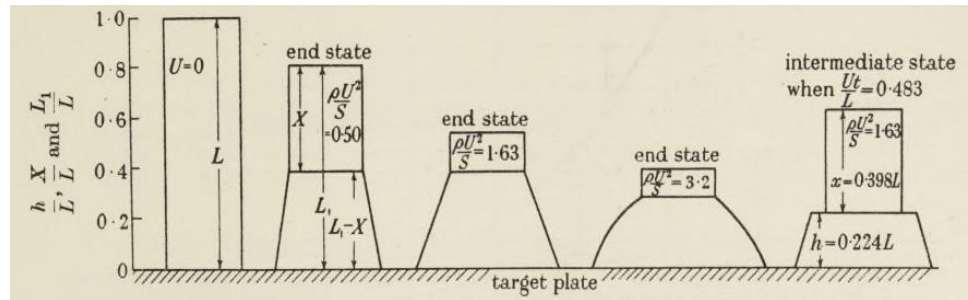


Figure 5. G.I. Taylor developed the Taylor test to explore strain hardening in his 1947 paper.<sup>6</sup>

The focus of the 1987 paper was improving strain-rate and temperature sensitive plasticity models exploring the notion that grain size of a material hugely influences strength and ductility. The researchers point to drastically different results between Johnson-Cook and Wilkins-Guinan constitutive models when studying copper impact tests with computer simulations. They introduce the idea of using a model based on grain size, accumulation of dislocations, and generation of dislocations by thermal activation energy. Furthermore, the authors discuss the differences in strain rate and temperature dependence for face centered cubic metals (FCC), and body centered cubic metals (BCC). For BCC metals, the thermal activation is independent of plastic strain in the material, whereas for an FCC, the thermal activation is observed to be highly dependent on plastic strain. Zerilli

<sup>6</sup> 9. Taylor, G., *The Use of Flat-Ended Projectiles for Determining Dynamic Yield Stress. I. Theoretical Considerations*. Proceedings of the Royal Society of London. Series A, Mathematical and Physical Sciences (1934-1990), 1948. **194**(1038): p. 289-299.

and Armstrong arrived at two constitutive equations. Equation 4 gives stress for an FCC metal, and Equation 5 gives stress for a BCC metal.

$$\sigma = \Delta\sigma'_G + c_2\epsilon^{1/2} \exp[-c_3T + c_4T\ln(\dot{\epsilon})] + kl^{-1/2} \quad (4)$$

$$\sigma = \Delta\sigma'_G + c_1 \exp[-c_3T + c_4T\ln(\dot{\epsilon})] + c_5\epsilon^n + kl^{-1/2} \quad (5)$$

Where  $c_1$ ,  $c_2$ , and  $c_5$  are units of stress (MPa),  $c_3$  and  $c_4$  are units of  $T^{-1}$  ( $K^{-1}$ ),  $n$  is unitless, and  $k$  is in units of stress x length<sup>1/2</sup> (MPa mm<sup>1/2</sup>).  $\Delta\sigma'_G$  in both equations is added to account for dislocation density. When comparing experimental cylinder impact results of the Zerilli Armstrong model with the Johnson and Cook's model OFHC copper, it was seen that the Johnson Cook model in Equation 2 did not predict large or small strains well [8]. The Zerilli Armstrong model, however appeared to better agree with experimental results. The results for the Zerilli Armstrong model applied to Armco iron did show a noticeable difference when comparing impact test simulations. Their model predicted too soft a material at large strains (as Johnson Cook does), but predicts a harder material at small strains, where Johnson Cook has been observed to predict a soft material.

Table 3. Comparison of Zerilli Armstrong model (Eq. (22)), Johnson Cook Model (Eq(1), and Johnson Cook experimental.<sup>7</sup>

| OFHC copper |                                        |            |                                 |                                 |                                |
|-------------|----------------------------------------|------------|---------------------------------|---------------------------------|--------------------------------|
| $T$<br>(K)  | $\dot{\epsilon}$<br>(s <sup>-1</sup> ) | $\epsilon$ | $\sigma$<br>experiment<br>(MPa) | $\sigma$ ,<br>Eq. (21)<br>(MPa) | $\sigma$ ,<br>Eq. (1)<br>(MPa) |
| 294         | 451                                    | 0.01       | 110                             | 113                             | 184                            |
| 294         | 451                                    | 0.10       | 200                             | 217                             | 268                            |
| 294         | 451                                    | 0.30       | 340                             | 328                             | 335                            |
| 493         | 449                                    | 0.01       | 110                             | 97                              | 154                            |
| 493         | 449                                    | 0.10       | 190                             | 165                             | 225                            |
| 493         | 449                                    | 0.30       | 280                             | 238                             | 281                            |
| 730         | 464                                    | 0.01       | 90                              | 84                              | 114                            |
| 730         | 464                                    | 0.10       | 140                             | 126                             | 167                            |
| 730         | 464                                    | 0.30       | 200                             | 171                             | 208                            |

| Armco iron |                                        |            |                                 |                               |                              |
|------------|----------------------------------------|------------|---------------------------------|-------------------------------|------------------------------|
| $T$<br>(K) | $\dot{\epsilon}$<br>(s <sup>-1</sup> ) | $\epsilon$ | $\sigma$<br>experiment<br>(MPa) | $\sigma$<br>Eq. (22)<br>(MPa) | $\sigma$<br>Eq. (1)<br>(MPa) |
| 294        | 407                                    | 0.01       | 397                             | 411                           | 357                          |
| 294        | 407                                    | 0.10       | 469                             | 478                           | 486                          |
| 294        | 407                                    | 0.30       | 535                             | 529                           | 590                          |
| 496        | 435                                    | 0.01       | 192                             | 248                           | 240                          |
| 496        | 435                                    | 0.10       | 298                             | 315                           | 326                          |
| 496        | 435                                    | 0.30       | 371                             | 366                           | 397                          |
| 733        | 460                                    | 0.01       | 143                             | 175                           | 177                          |
| 733        | 460                                    | 0.10       | 212                             | 242                           | 241                          |
| 733        | 460                                    | 0.30       | 275                             | 293                           | 293                          |

#### Abaqus Implementation of Zerilli Armstrong model

A Zerilli-Armstrong plasticity model was developed for Abaqus CAE by Dean Bonorchis at the University of Cape Town in his 2003 dissertation [10]. Bonorchis programmed a VUMAT custom plasticity model to implement Zerilli Armstrong for BCC and FCC materials. A VUMAT is a custom, user created material using an Abaqus explicit dynamic simulation, as opposed to an implicit dynamic UMAT material. The Abaqus explicit dynamic analysis module is computationally efficient for analyzing large models

<sup>7</sup> 8. Zerilli, F.J. and R.W. Armstrong, *Dislocation-mechanics-based constitutive relations for material dynamics calculations*. Journal of Applied Physics, 1987. **61**(5): p. 1816-1825.

[11]. The develop of Abaqus Dassault lists the advantages of this method in their documentation, including its usefulness in simulation high-speed dynamic events such as sheet metal forming[11]. Attempts were made to reproduce IPL tests with a Johnson-Cook based simulation of 304 stainless steel, however difficulties with wave speed in the material produced errors. A sample of the authors VUMAT process flowchart is shown below in Figure 6.

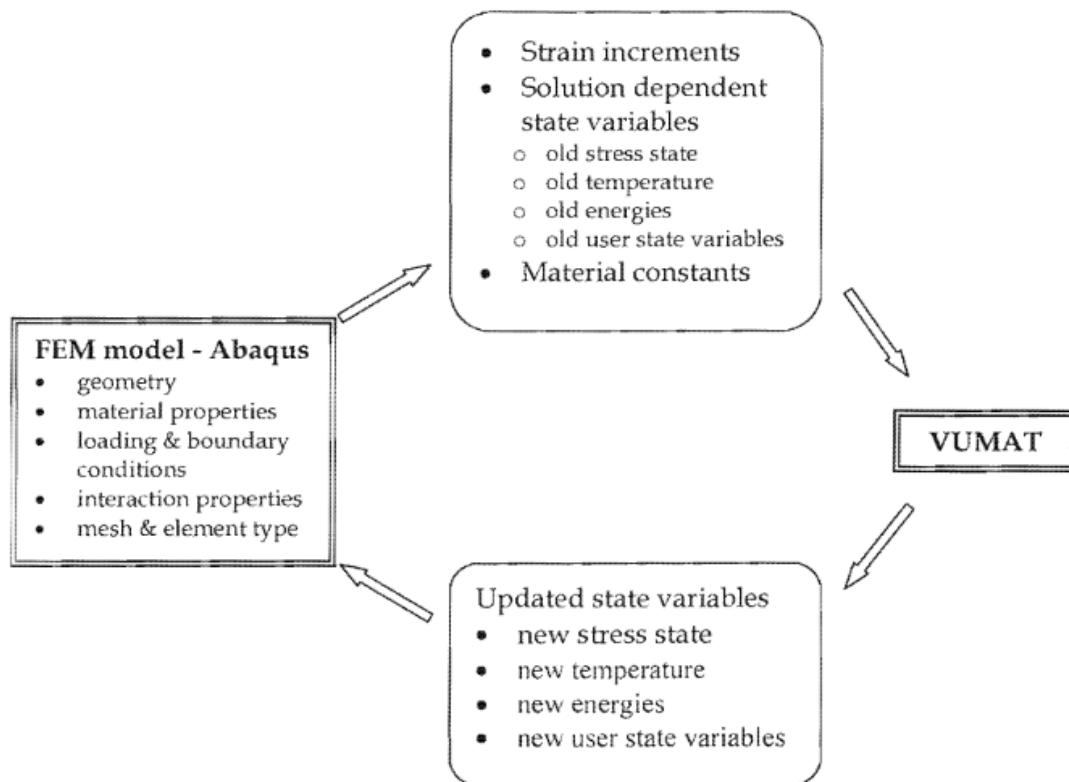


Figure 6. Abaqus flow chart used by Bonorchis to illustrate VUMAT solver.<sup>8</sup>

<sup>8</sup> 10. Bonorchis, D., *Implementation of Material models for High Strain Rate Applications as User-subroutines in Abaqus/Explicit*, in *Mechanical Engineering*. 2003, University of Cape Town. p. 229.

Bonorchis ran simple single element tests in various loading conditions using Abaqus to verify the accuracy of his custom materials. To solve the constitutive equations at each step, Bonorchis used a bisection and Newton methods in his solvers, however there is only a brief description of these, and the work does not go into detail as to how the equations were discretized. Once verification was complete, the author reproduced Taylor impact tests to verify his VUMATs with experimental results of OFHC copper and Armco iron, using the same methodology as Johnson and Cook, and Zerilli and Armstrong: by comparing shape of slugs after the impact. A sample of his results are shown below in Figure 7.

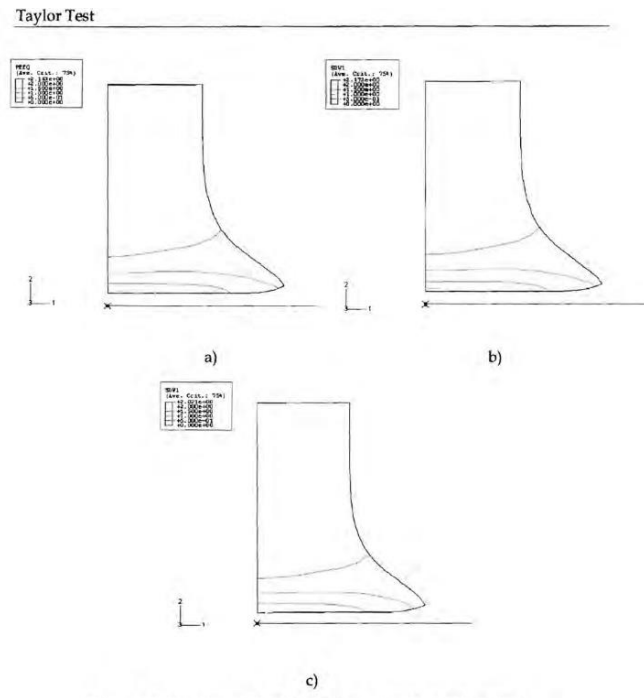


Figure 7. An example of results comparing the Abaqus prepackaged Johnson Cook Model (a), a custom Johnson-Cook VUMAT (b), and a custom Zerilli-Armstrong VUMAT (c).<sup>9</sup>

<sup>9</sup> 10. Ibid.

### Mechanical Threshold Stress- Follansbee and Kocks

P. S. Follansbee and U.F. Kocks developed the Mechanical Threshold Stress (MTS) model at Los Alamos National Laboratory in 1986, building on their previous work into strain rate sensitive of FCC metals [12]. The main property, the mechanical threshold stress, is a materials flow stress at 0 K. Flow stress is the stress required to maintain plastic deformation of a material, found between the materials yield stress and ultimate strength MTS itself is a theoretical value. Figure 8 shows a plot of the stress and strain of OFHC copper using mechanical threshold stress equation at varying rates.

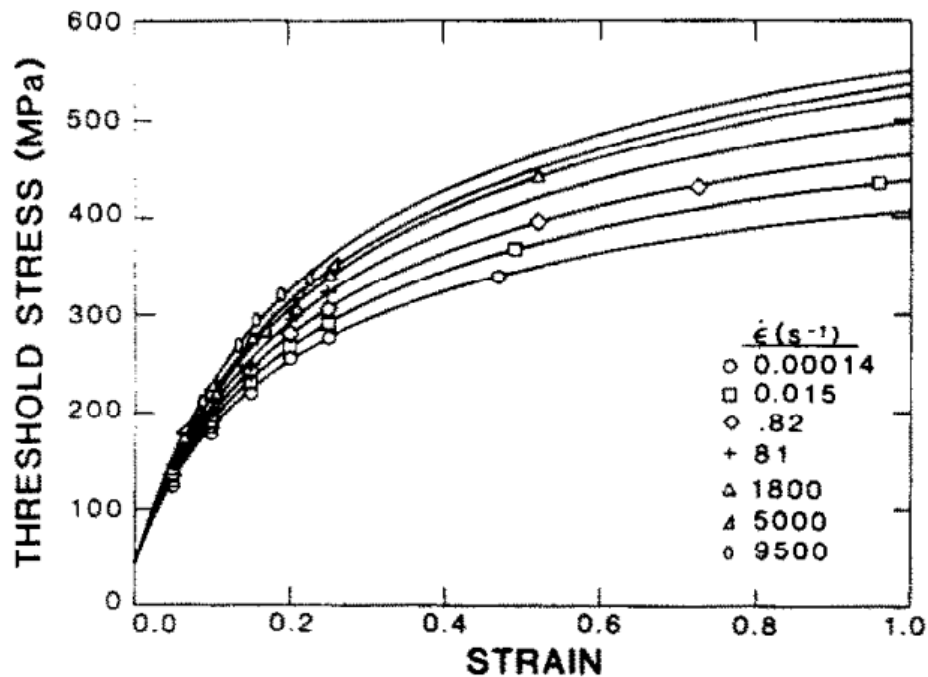


Figure 8. Strain hardening curves for OFHC copper using MTS equation.<sup>10</sup>

<sup>10</sup> 12. Follansbee, P.S. and U.F. Kocks, *A constitutive description of the deformation of copper based on the use of the mechanical threshold stress as an internal state variable*. Acta Metallurgica, 1988. **36**(1): p. 81-93.

Like Zerilli and Armstrong's work, the MTS model is based off of a materials thermal activation energy and density of dislocations in the metal. The authors pointed to a need for a single strain rate and temperature sensitive constitutive model that would also behave predictably at low strain rates. Previous work at the time had not been utilized for strain rates above  $\dot{\epsilon} = 10^3 \text{ s}^{-1}$ . This is important as the researchers note that strain rate sensitivity can increase drastically above this value. Copper was chosen as the material of interest as mechanical threshold stress data up to rates of  $\dot{\epsilon} = 10^4 \text{ s}^{-1}$  allows for the study into strain rates at level where the material becomes increasing strain rate sensitive. Mechanical threshold stress is defined by Equation 6 as;

$$\hat{\sigma} = \hat{\sigma}_a + s(\dot{\epsilon}, T)\hat{\sigma}_l \quad (6)$$

Where  $\hat{\sigma}_a$  accounts for rate independent effects, associated with grain boundaries or long-range barriers. The second term is a scaling function contains rate dependency associated with short-range obstacles. These are known respectively as the thermal and athermal components of the equation[13]. An Arrhenius equation, Equation 7, is used to account for a rate dependence on temperature [9].

$$\dot{\epsilon} = \dot{\epsilon}_0 \exp \left[ \frac{\Delta G(\sigma_t / \hat{\sigma}_t)}{kT} \right] \quad (7)$$

Here  $\dot{\epsilon}_0$  is a constant value, and  $k$  is the Boltzman constant ( $1.38 \times 10^{-23} \text{ J-K}^{-1}$ ), and  $\Delta G$  is the Gibb's free energy in Equation 8 which is equal to

$$\Delta G = g_0 \mu b^3 \left[ 1 - \left( \frac{\sigma_t}{\hat{\sigma}_t} \right)^p \right]^q \quad (8)$$

With  $g_0$  being a normalized activation energy,  $\mu$  is the materials shear modulus  $b$  is the magnitude of the Burger's vector,  $p$  and  $q$  are constants, which are used to characterize the shape of the obstacle profile, where  $0 \leq p \leq 1$ , and  $1 \leq q \leq 2$  [12].

The authors combine these equations to arrive at the general expression for MTS in Equation 9.

$$\sigma = \hat{\sigma}_a + (\hat{\sigma} - \hat{\sigma}_a) \left\{ 1 - \left[ \frac{kT \ln(\dot{\epsilon}_0 / \dot{\epsilon})}{g_0 \mu b^3} \right]^{\frac{1}{q}} \right\}^{\frac{1}{p}} \quad (9)$$

Follansbee and Kocks also discuss the strain hardening rate of an FCC metal,  $\theta = d\sigma/d\epsilon$ , using the relation in Equation 10.

$$\theta = \theta_0 - \theta_t(T, \dot{\epsilon}, \hat{\sigma}) \quad (10)$$

Where  $\theta_0$  is hardening by dislocation accumulation and is assumed constant. and  $\theta_t$  is the dynamic recovery rate.

The researchers show that their model is capable of modelling changing strain rates accurately, a feature that would be helpful when modeling a multi-axial in-plane loading test of an FCC metal in the current in plane loader. They were successful in modelling tensile tests of OFHC copper at strain rates from  $10^{-4} \text{ s}^{-1}$  to  $10^4 \text{ s}^{-1}$ . It is noted that above strain rates of  $10^5 \text{ s}^{-1}$  the model shows unrealistic perfect plasticity stress-strain behavior in materials [12]. These strain rates are beyond those focus on in this IPL study.

An Abaqus user-hardening regimen was written by G.J. Jansen Van Rensburg and S. Kok. This is a valuable tool to implement the MTS model in Abaqus. In their paper, the researchers also used strain data of OFHC copper. Van Rensburg and Kok reduce the MTS equation into smaller forms for simplified implementation as a UHARD and Fortran code

[13]. The thermal portion of the equation for MTS are further reduced by noting there are two thermal components to the equation, arriving at Equation 11.

$$\frac{\sigma_y}{\mu} = \frac{\hat{\sigma}_a}{\mu} + S_i(\dot{\epsilon}, T) \frac{\hat{\sigma}_i}{\mu_0} + S_\epsilon(\dot{\epsilon}, T) \frac{\hat{\sigma}_\epsilon}{\mu_0} \quad (11)$$

Here,  $\hat{\sigma}_i$  is the non-evolving thermal portion of yield stress,  $\hat{\sigma}_\epsilon$  is used to account for interaction with mobile dislocations and is the changing component of the equation.  $\mu_0$  is a reference value of the shear modulus. Equation 12 shows the equation for the shear modulus as defined by Van Rensburg and Kok.

$$\mu = \mu_0 - \frac{D_0}{\exp\left(\frac{T_0}{T}\right) - 1} \quad (12)$$

With  $T_0$ , and  $D_0$  are empirically derived constants. To relate to the original formulation of the equation  $\hat{\sigma}_\epsilon$  is equal to Equation 10. This is re-written as the tanh functional form in Equation 13

$$\theta = \theta_0 \left( 1 - \frac{\tanh\left[\frac{\alpha \hat{\sigma}_\epsilon}{\hat{\sigma}_{\epsilon s}}\right]}{\tanh(\alpha)} \right) \quad (13)$$

Where  $\alpha$  is a constant and  $\hat{\sigma}_{\epsilon s}$  is the saturation threshold stress, or a condition of constant flow stress [14]. Saturation threshold stress in Equation 14 is a function of strain rate and time and is expressed as by which another form of the Arrhenius equation is listed above.

$$\ln \frac{\dot{\epsilon}}{\dot{\epsilon}_{\epsilon s 0}} = \frac{g_{0\epsilon s} \mu b^3}{kT} \ln \left( \frac{\hat{\sigma}_{\epsilon s}}{\hat{\sigma}_{\epsilon s 0}} \right) \quad (14)$$

With  $\dot{\epsilon}_{\epsilon s 0}$ ,  $g_{0\epsilon s}$ , and  $\hat{\sigma}_{\epsilon s 0}$  being empirically determined constants.

### Abaqus Implementation of MTS

The Van Rensburg and Koks Abaqus UHARD code is included in appendix A. The Abaqus UHARD is an implicit subroutine that takes user defined variables, Dassault Systemes documentation shows the basic structure of code that the user must follow in order to be input to the FEA model [11]. This is shown in Figure 9.

#### User subroutine interface

```

SUBROUTINE UHARD(SYIELD,HARD,EQPLAS,EQPLASRT,TIME,DTIME,TEMP,
1      DTEMP,NOEL,NPT,LAYER,KSPT,KSTEP,KINC,CMNAME,NSTATV,
2      STATEV,NUMFIELDV,PREDEF,DPRED,NUMPROPS,PROPS)
C
C      INCLUDE 'ABA_PARAM.INC'
C
      CHARACTER*80 CMNAME
      DIMENSION HARD(3),STATEV(NSTATV),TIME(*),
      $          PREDEF(NUMFIELDV),DPRED(*),PROPS(*)

      user coding to define SYIELD,HARD(1),HARD(2),HARD(3)

      RETURN
      END

```

Figure 9. Skeleton code for Abaqus UHARD model.<sup>11</sup>

The UHARD subroutine requires the input of five variables.

- The materials yield stress SYIELD
- The variation of yield stress with respect to equivalent plastic strain  
 $\partial \sigma^0 / \partial \bar{\epsilon}^{pl}$  HARD(1)
- The variation of yield stress with respect to equivalent plastic strain rate  
 $\partial \sigma^0 / \partial \dot{\bar{\epsilon}}^{pl}$  HARD(2)
- the variation of yield with respect to temperature  $\partial \sigma^0 / \partial \theta$  HARD(3)

<sup>11</sup> 13. G.J Jansen van Rensburg, S.K., *Tutorial on state variable based plasticity: An Abaqus UHARD subroutine*, in *Eighth South African Conference on Computational and Applied Mechanics*. 2012. p. 158-165.

- and an array of user defined state variables (NSTATV)

The researchers used midpoint integration to determine  $\hat{\sigma}_\epsilon$  at each time step, this calculated plastic strain rate, duration of the time step, and the change in temperature over each time step, and then calculates the thermal stress component at the next time step. As a consequence of the use of the hyperbolic tangent in Equation 14, and midpoint integration methods, the researchers use the Newton-Raphson method. By using their broken-up forms of the equation, the MTS equation is solved at the end of each time step. Van Rensburg and Koks utilized eight state dependent variables (STATEV) and the definitions for them are shown below in Table 4. The researchers also provide a useful flow chart to illustrate how their UHARD subroutine operates in Figure 10[13].

Table 4. State variables for MTS UHARD subroutine as defined by Van Rensburg and Koks.<sup>12</sup>

| Variable                               | Definition                                                                                           | Allocation |
|----------------------------------------|------------------------------------------------------------------------------------------------------|------------|
| $\hat{\sigma}_\varepsilon^n$           | $\hat{\sigma}_\varepsilon$ at time $t^n$ , the start of the current increment.                       | STATEV (1) |
| $\Delta\hat{\sigma}_\varepsilon^{n+1}$ | Change in $\hat{\sigma}_\varepsilon$ for current increment.                                          | STATEV (2) |
| $\varepsilon_p^n$                      | Equivalent plastic strain $\varepsilon_p$ at the end of the previous increment.                      | STATEV (3) |
| $\varepsilon_p^{n+1}$                  | Equivalent plastic strain $\varepsilon_p$ at the end of the current increment.                       | STATEV (4) |
| $\dot{\varepsilon}_p^n$                | Equivalent plastic strain rate $\dot{\varepsilon}_p$ at the end of the previous increment.           | STATEV (5) |
| $\dot{\varepsilon}_p^{n+1}$            | Equivalent plastic strain rate $\dot{\varepsilon}_p$ at the end of the current increment.            | STATEV (6) |
| KINC                                   | KINC verification counter allowing a single update of the relevant variables                         | STATEV (7) |
| KSTEP                                  | KSTEP verification counter used to reset STATEV (7) should the analysis move on to a different step. | STATEV (8) |

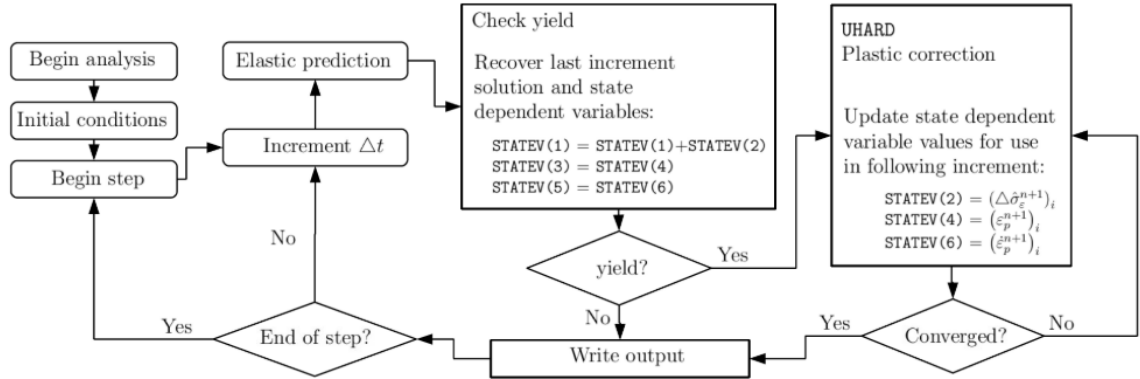


Figure 10. Flowchart for Van Rensburg and Koks UHARD subroutine for MTS constitutive model.<sup>13</sup>

<sup>12</sup> 13. Ibid.

<sup>13</sup> 13. Ibid.

Van Rensburg and Koks MTS code was checked against isothermal, constant strain rate data for OFHC copper, and compared this against the Johnson-Cook model. Their data shows a better match to both constant strain rate data and tests, which include a strain rate jump when compared with the Johnson and Cook model. Their results are show below in Figure 11 Figure 12 [13].

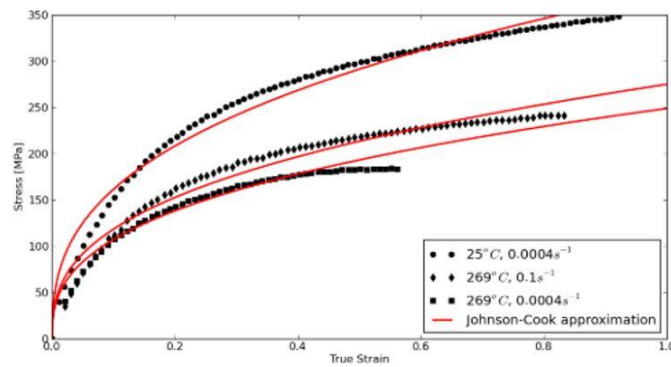


Figure 11. Van Rensburg and Kok's results comparing Johnson-Cook model with their MTS UHARD code. Material simulated was OFHC copper.<sup>14</sup>

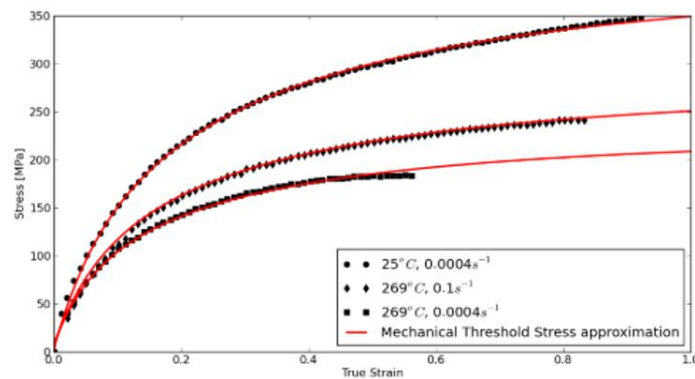


Figure 12. Van Rensburg and Kok's results with their MTS UHARD code. Material simulated was OFHC copper.<sup>15</sup>

<sup>14</sup> 13. Ibid.

<sup>15</sup> 13. Ibid.

### Multiaxial Loading at MSU

Understanding of complex, multi-axial states of stress and strain are an important part of any design process. Typically, a test sample experiences a multi-axial load as a combination of torsion, tension, and/or an internal pressure. Montana State University's In-Plane Loader is a testing unit capable of uniquely putting a testing coupon in a complex state of stress by way of horizontal and vertical displacements (x and y), and rotation about a Z-axis in the X-Y plane. Historically it has been utilized by the MSU composites group to study the effects of placing composite laminates in a multi-axial stress state. The in-plane loader, when combined with the GOM Aramis Digital Image Correlation measurement system is a powerful tool used to better understand a materials behavior, but to this point has only been used for studying the effect of complex loading paths on advanced composite materials at quasi-static testing speeds. Currently there are limited resources available to study multi-axial high strain rate testing. Multi-axial systems will typically combine some combination of tension, compression, pressure, torsion. The Montana State in-plane loader offers the capabilities of loading in tension, compression, translation, and rotations simultaneously in one test.

### Description and History of the Montana State In Plane Loader

The concept of the in-plane loader was born out of a need to better understand fracture mechanics of fiber reinforced composite materials. A team of researchers at Navy Research Labs developed the first IPL to collect data on composites [15]. This multi-axial data would provide design engineers with more insight on a composite laminate's behavior.

The loading system designed by NRL consists of three computer controlled 2-Kip, 6 inch hydraulic actuators which are attached to a crosshead. Linear displacement variable transducers measure displacement. The NRL IPL machine is automatically fed single notched test coupons (1" x 1.5" x 0.1"). The NRL coupons feature a 0.6 inch notch cut parallel to the 1 inch dimension. A schematic of the NRL IPL is found below.

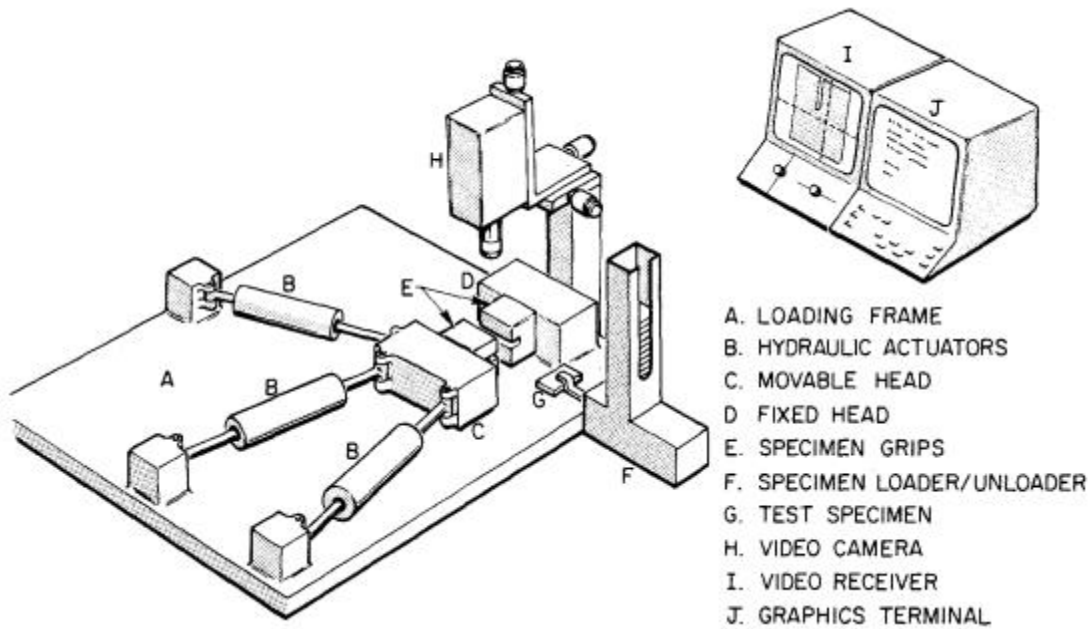


Figure 13. Original In-Plane Loader designed by the Navy Research Labs.<sup>16</sup>

This original IPL is mounted to a table, allowing the 1 1/4" thick steel frame to act a rigid structure. The orientation of the three actuators to carry out X and Y translation, along with in-plane rotation of the gripping head. Measurements are made using a video digitizer set

<sup>16</sup> 16. Mast, P.W., et al., *Characterization of strain-induced damage in composites based on the dissipated energy density part I. Basic scheme and formulation*. Theoretical and Applied Fracture Mechanics, 1995. 22(2); p. 71-96.

above the test piece. Displacements are recorded in spherical space, the main purpose of the NRL in plane loader was to study dissipated energy in composite materials.

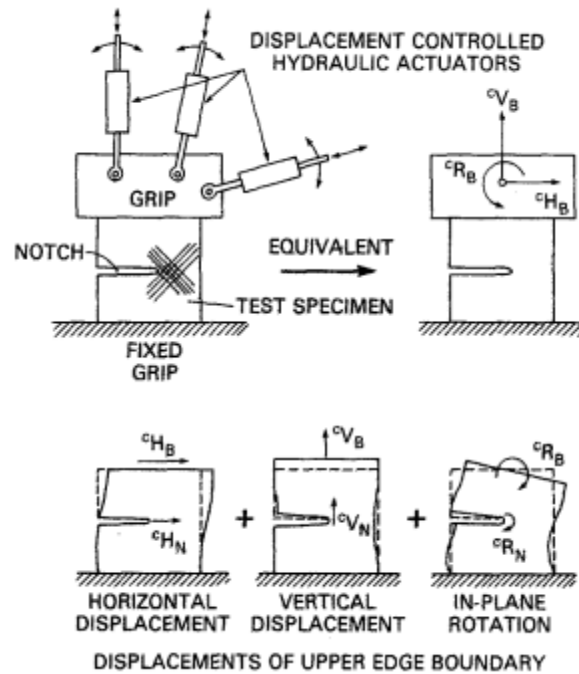


Figure 14. Combined loading conditions that can be applied by the NRL IPL.<sup>17</sup>

### Montana State University IPL

In 2002 Montana State University senior design capstone students constructed a version of the Navy Research Lab's IPL, and since then the machine has undergone several upgrades to its most current iteration. Previous thesis document the IPL and its construction and capabilities [17]. Between 2015 and 2017 the grips of the IPL were improved, to minimize slipping in the coupon. This entailed replacing the cumbersome bolt fastening jaws with hydraulically actuated grips, which keep the test piece centered in the DIC focal plane, and the center of the coupon at the center of actuator motion, regardless

<sup>17</sup> 16. Ibid.

of coupon thickness. While slipping still occurs with certain materials and geometries, these updated grips have been able to successfully run tests with 304L stainless steel with some success. A more detailed description of the changes can be found in the studies conducted from 2005-2009, and 2015-2017[17-21].

### Digital Image Correlation

The GOM Aramis digital image correlation (DIC) software was used in pair with a GOM stereoscopic camera setup as a method non-contact displacement measurement. The Aramis software is used to map the strain field across an area of interest. The camera system is set up on a level tripod, which sets the center of the focal length at the center of the IPL grips. The camera system uses two f2.8/50mm lenses, which are manually focused before calibration. Figure 15 is a schematic provided by GOM showing the measurements needed by the cameras to calculate displacements.

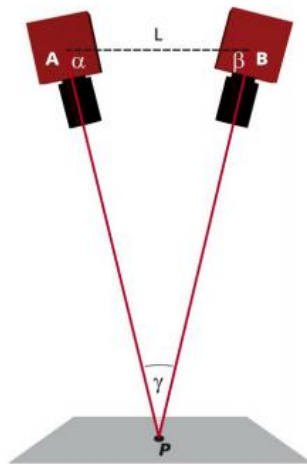


Figure 15. Schematic of DIC camera set-up as used with the In-Plane Loader.<sup>18</sup>

<sup>18</sup> 22. GmbH, G., *Digital Image Correlation and Strain Computation Basics*. 2018.

The strength of DIC analysis is that strain information, when gathered by means of strain gages and extensometers, relies heavily on analytical methods, and assumptions [17]. Furthermore, complex displacement associated with those carried out by the in-plane loader would require a large gage section to accommodate a strain gage rosette. With the actuator load limitation being approximately 2000 lbf, testing of metals and high strength composites requires a thin gage section to induce strain to failure of the material. Strain gages were ruled out, because the DIC aims to capture the full strain field in the gage section. The nature of the strain field in a coupon under multi-axial loading, and the lack of space between the IPL does not allow for an extensometer to be used.

## TESTING PROCEDURE

### Tensile Testing for Verification

Abaqus was used to experiment with the strain rate sensitive terms of a stainless steel using constants in Table 5 determined by Maurel-Pantel et al. These simulations showed that given the coupon geometry, and actuator force and speed limits, strain rate sensitive plastic deformation cannot be observed with this iteration of the IPL. The FEA simulation was run for strain rates from  $10^{-2}$  to  $10^3$  and is shown in Figure 16. Strain rates in the tests from Table 9 show  $10^{-2}$  to  $10^{-1} \text{ s}^{-1}$  rates, which fall well below speeds that allow strain rate sensitivity to affect the materials plasticity curve.

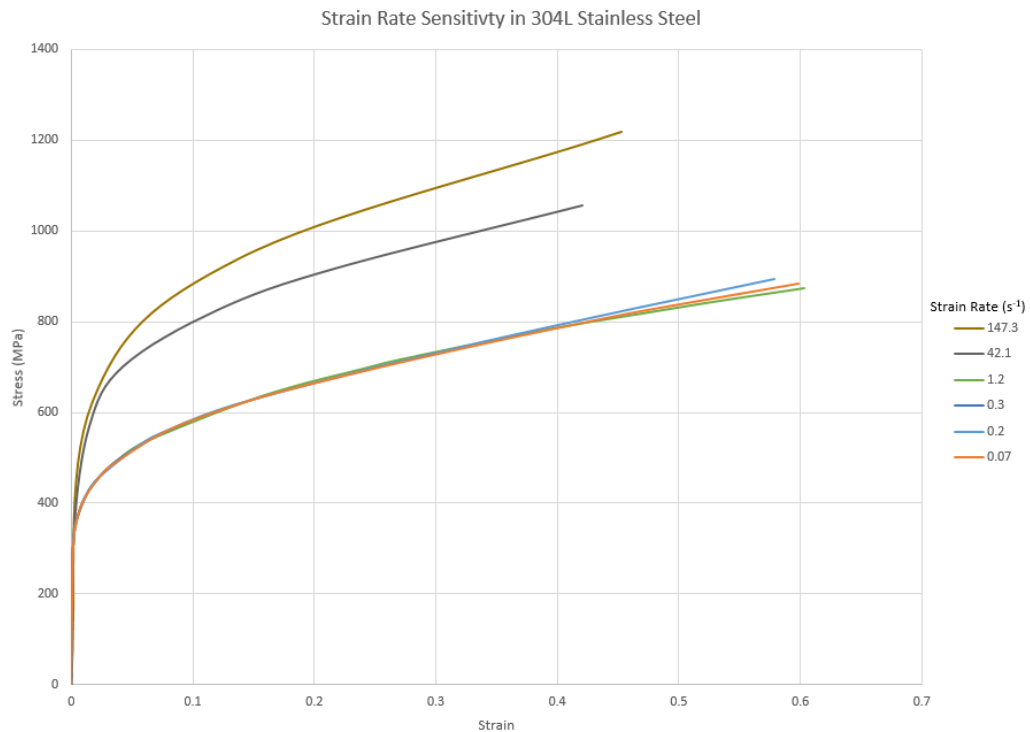


Figure 16. Plot of Abaqus simulations illustrating the Johnson Cook strain rate sensitive plastic deformation in 304L stainless steel. An IPL test falls between  $0.07 \text{ s}^{-1}$  and  $0.3 \text{ s}^{-1}$ .

Table 5. Johnson Cook constants used by A. Maurel-Pantel et al. for 304L stainless steel, showing similar properties to 304 stainless.<sup>19</sup>

| Maurel-Pantel J-C Constants     |        |
|---------------------------------|--------|
| E (GPa)                         | 200    |
| A (MPa)                         | 253.32 |
| B (MPa)                         | 685.1  |
| n (-)                           | 0.3128 |
| C (-)                           | 0.097  |
| m (-)                           | 2.044  |
| $\epsilon_0$ (s <sup>-1</sup> ) | 1      |
| Tf (K)                          | 1698   |
| T0 (K)                          | 296    |

Tensile tests were conducted to verify mechanical properties of the 304 stainless steel used in this research. Tests were conducted on an Instron 8562 servo-electric testing machine. Coupons were loaded at a rate of 8.89 kN / minute. 7 Coupons of 304 stainless steel were used in this work. Force data was collected by the Instron, and an Instron 2620-826 (s/n 251) extensometer was used to measure strain in the sample. Engineering stress and strain were calculated from this experiment.

Tensile data was post processed in MATLAB. A script was written to import raw .csv files containing load, strain as measured from the extensometer, displacement and time. Stress vs. strain curves were created. The data collected from the Instron testing was truncated to linear elastic and plastic portions of the curve. Elastic modulus was evaluated from the test data using a linear regression, this resulted in an average modulus of 196.2

<sup>19</sup> 23. Maurel-Pantel, A., et al., *3D FEM simulations of shoulder milling operations on a 304L stainless steel*. Simulation Modelling Practice and Theory, 2012. 22(C): p. 13-27.

GPa, these values are shown in Table 6. Results were plotted and an example is shown below in Figure 17. The MATLAB plots can be found in Appendix A.

Table 6. Elastic Modulus for 304 Stainless Steel, determined by tensile testing.

| Sample  | E (GPa) | R <sup>2</sup> |
|---------|---------|----------------|
| 1       | 200.4   | 0.9983         |
| 2       | 199.3   | 0.9991         |
| 3       | 188.1   | 0.9998         |
| 4       | 191.1   | 0.9993         |
| 5       | 202.0   | 0.9997         |
| Average | 196.2   |                |

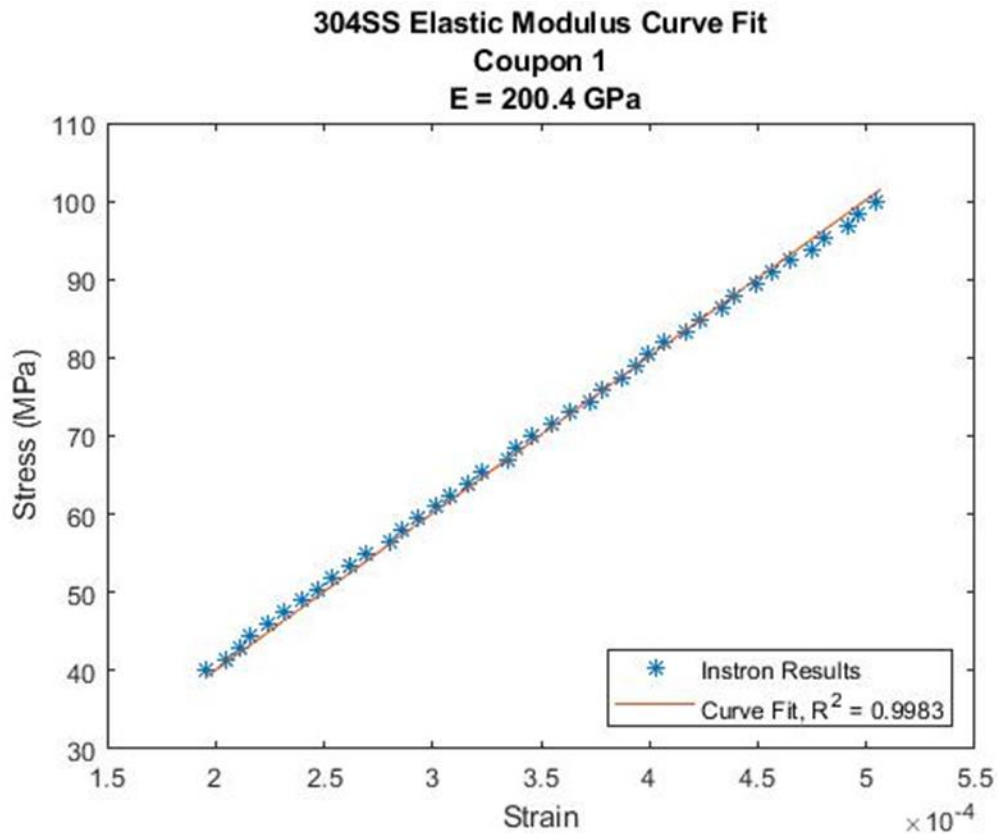


Figure 17. Plot of the elastic modulus curve fit and test data for a 304 stainless steel coupon.

For the more complex plastic portion of the curve the MATLAB curve fitting application was used to determine the Johnson Cook constants, B and n.

As the Abaqus model shown above indicates an IPL test can be approximated as quasi-static and are operated at room temperature, only the first term in the J-C equation, which is also known as the Ludwik-Hollomon equation, were solved for in the curve fit [24]. Given the reason noted above the strain-rate and temperature dependent terms in Equation 3 are set to equal 1. This results in the form found in Equation 16.

$$\sigma = A + B\epsilon^n \quad (16)$$

A is the material's yield stress, Johnson and Cook do not specify what they define as the yield stress in either of their papers detailing the model [7, 25]. For this study, the materials proportional limit was used. This was determined by comparing the materials elastic modulus to the test data. The stress values from the test data were subtracted from the stress as calculated by multiplying strain by the best fit modulus.

this difference value was consistently above 1 MPa, the material was said to have yielded. An example showing the plot of the two values are show below in Figure 18.

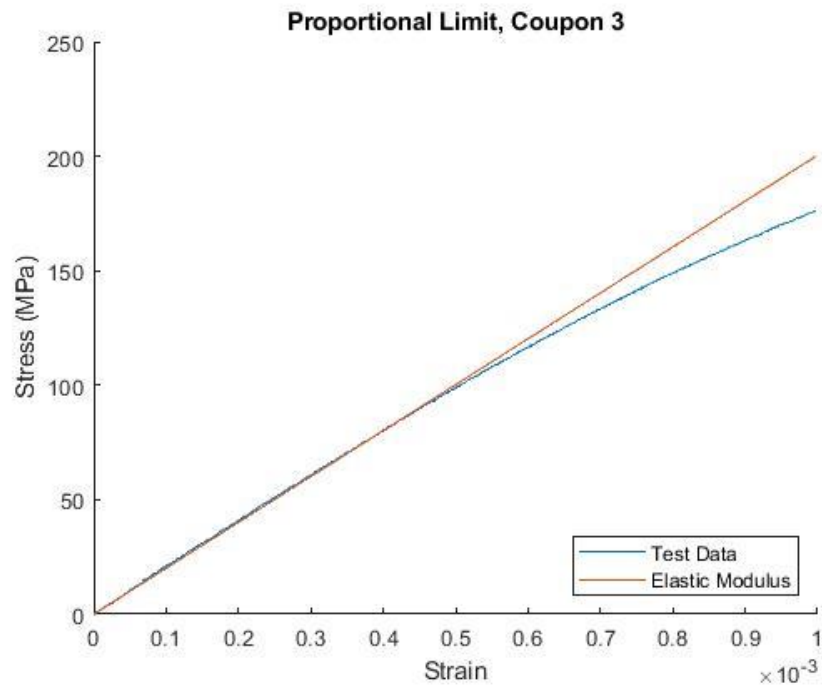


Figure 18. Plot comparing test data with elastic modulus slope, used to determine proportional limit.

Figure 19 was used for each coupon to determine when it's modulus drifts 1 MPa off of the theoretical modulus line.

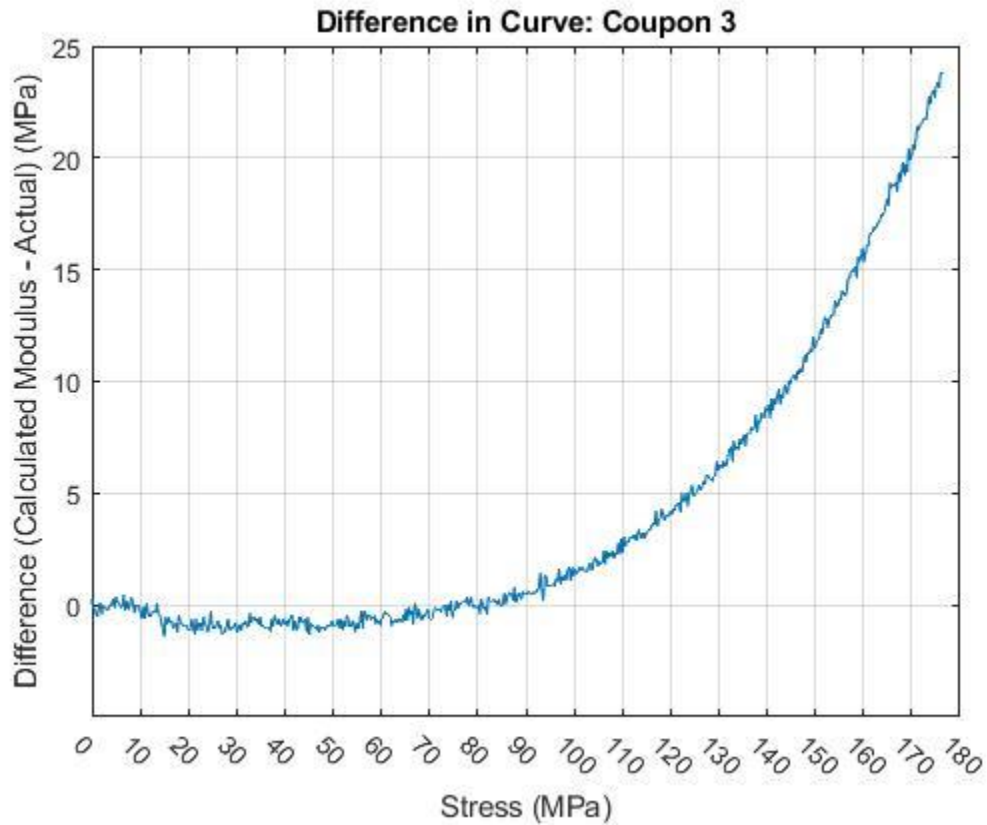


Figure 19. Plot of calculated Stress = ( $E \times \text{Strain}$ ) - test data stress value, plotted against stress. This is used to determine when the material has yielded.

With the yield stress,  $A$ , known,  $B$ , and  $n$  for all tensile datasets was determined by the MATLAB curve fitting function.

Stress and strain data were truncated to plot only plastic deformation, from the proportional limit upward, for the steel samples. The curve-fitting tool was set to use a custom equation shown in Figure 20.



Figure 20. MATLAB Curve fitting app, A is filled with each test's respective yield stress value, B and n are solved for.

Fit options were adjusted to allow the program to run what was deemed enough iterations to arrive at solutions without becoming fixed at the upper or lower bounds. Bounds for these values were estimated by examining Johnson-Cook coefficients as determined by previous research [23, 26-28].

Table 7. Values used to validate Johnson-Cook coefficients.

| <b>E<br/>(GPa)</b> | <b>A<br/>(MPa)</b> | <b>B<br/>(MPa)</b> | <b>n (-)</b> | <b>C (-)</b> | <b>m (-)</b> | <b><math>\epsilon_0</math> (s<sup>-1</sup>)</b> | <b>Tf<br/>(K)</b> | <b>T0<br/>(K)</b> | <b>Source</b> |
|--------------------|--------------------|--------------------|--------------|--------------|--------------|-------------------------------------------------|-------------------|-------------------|---------------|
| 200                | 253.32             | 685.1              | 0.3128       | 0.097        | 2.044        | 1                                               | 1698              | 296               | [21]          |
| 193                | 264                | 1567.33            | 0.703        | 0.067        | -            | 1                                               | -                 | -                 | [22]          |
| 200                | 310                | 1000               | 0.65         | 0.07         | N/A          | 1                                               | -                 | -                 | [23]          |
|                    | 344.73             | 31.26              | 0.3          | 0.24         | 1.03         | 1.00E-06                                        | -                 | -                 | [24]          |

Values from Table 7 were used as a check to set limits on what MATLAB could output for values of B and n. An example of the curve fitting output is seen in Figure 21.

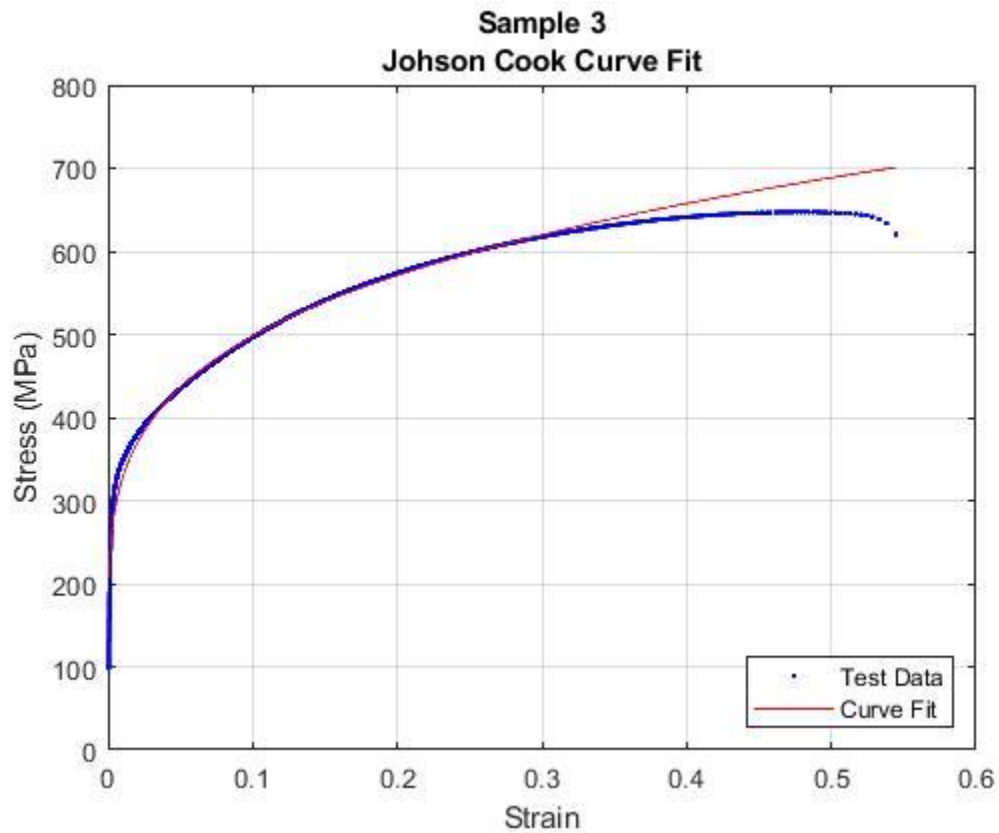


Figure 21. Plot of the MATLAB generated curve fit overlaid onto data from tensile tests.

This process was repeated for all tensile tests these values were averaged and used as inputs for the Abaqus Johnson Cook model found in Table 8.

Table 8. results from elastic and plastic region curve fits.

| Sample  | E (GPa) | A (MPa) | B (MPa) | 95% CI Bounds  | n      | 95% CI Bounds    | R <sup>2</sup> | RMSE  |
|---------|---------|---------|---------|----------------|--------|------------------|----------------|-------|
| 1       | 200.4   | 97.5    | 699.1   | (696.9, 701.2) | 0.2421 | (0.241, 0.2432)  | 0.9942         | 12.28 |
| 2       | 199.3   | 100     | 698     | (697.3, 698.7) | 0.2384 | (0.238, 0.2387)  | 0.9994         | 3.885 |
| 3       | 188.1   | 122.5   | 684.9   | (684.4, 685.3) | 0.2586 | (0.2584, 0.2589) | 0.9998         | 2.302 |
| 4       | 191.1   | 117.5   | 682.7   | (681.7, 683.7) | 0.2473 | (0.2467, 0.2479) | 0.9986         | 5.974 |
| 5       | 202.0   | 112.5   | 692.3   | (691.6, 692.9) | 0.2503 | (0.2499, 0.2506) | 0.9996         | 3.356 |
| Average | 196.2   | 110.0   | 691.4   |                | 0.2473 |                  |                |       |

### IPL Testing Procedure

The IPL system consists of the loading frame, a Windows PC which controls the IPL's movement using LabVIEW and MATLAB scripts, a stereoscopic camera system, and the Aramis computer. IPL coupons must be tested before the stochastic spray paint pattern is fully cured. The testing process is detailed in this section, as the process has been altered from previously established methods[17, 19].

### Coupon Sizing

IPL coupon geometry for stainless steel was determined through experimentation. The face of the gage section should be as large as possible. This allows for a larger area sprayed with the stochastic pattern, enabling Aramis to create more facets in the section of interest. This requirement was balanced with the maximum load the actuators can support, and the gripping force applied to the coupon. The minimum thickness of an IPL coupon is 4.8mm (3/16" nom.), this is due to the steel plates mounted to the grips which constrain lateral motion of the coupon. With these considerations, gage section of 3.8 mm x 7.11 mm

(0.150" by 0.280"  $\pm$  0.005") was arrived at. This geometry provides the minimum area for Aramis to calculate a facet field, while also allowing the actuators of the IPL to apply a stress level that induces plastic deformation in the material. Figure 22 shows the nominal geometry for a stainless steel IPL coupon. A 6.35mm ball end mill was used to cut the reduced section ( $r = 1/8$ ").

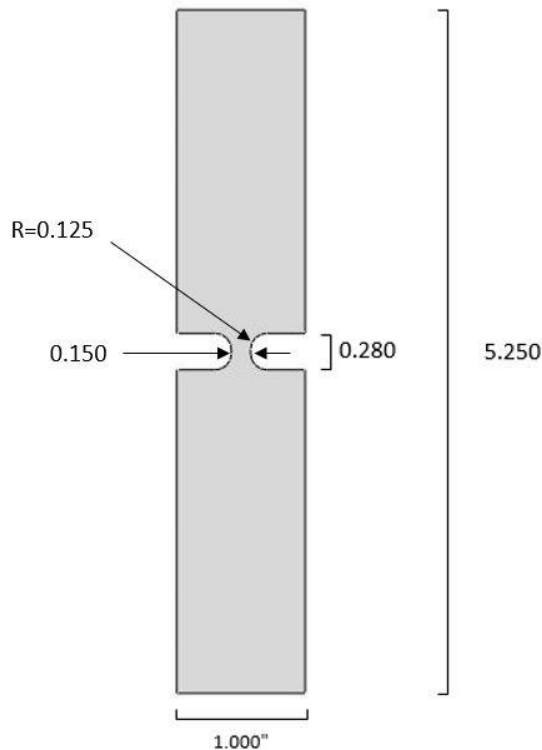


Figure 22. IPL coupon geometry for stainless steel. Drawing dimensions in inches.

#### Aramis Procedure

MSU's Mechanical Engineering department has used DIC as a method of strain measurement during quasi-static materials testing. Due to LANL's desire to obtain high

strain rate, multi axial in-plane material characterization, the methods by which the DIC data is collected is altered slightly from the most recent previous IPL study [17].

Once the camera system is properly calibrated, the Aramis software is set to record in “Fast measurement mode”, this allows for a series of images to be taken and stored directly to the Aramis computer’s RAM. The limitations to this image acquisition method are both the amount of RAM in the computer, the data transfer rate, and the camera systems maximum shutter speed. The shutter speed being the major barrier to higher quality capture of strain rate data. The camera system used had a maximum frame rate of 5 frames per second. The camera assembly used for this project is seen below in Figure 23. The cameras used were 50mm, f2.8 lenses. Two 24V 9W lights are attached to the tripod to illuminate the subject. Both lens and lights were fitted with polarizing filters to eliminate glare.



Figure 23. GOM designed camera set up used for IPL testing; cameras are mounted at a set distance from one another. Lighting elements can be adjusted for optimum position.

Aramis measures strain by tracking a stochastic pattern on the area of interest. The pattern is a field of black speckles laid over a flat white base. The stochastic pattern can be a structured grid or have a random orientation. Pattern dot size and spacing is determined by the focal length of the camera being used, GOM provides a reference card showing acceptable pattern sizing for various lens setups. The pattern medium used in this work was a Krylon flat white spray paint for the background, followed by Krylon flat black spray paint for the stochastic pattern. Figure 24 shows examples of stochastic patterns in an IPL coupon.



Figure 24. Desirable stochastic spray pattern on 304 stainless steel.

With the measurement mode selected, the stochastic pattern must be applied to the coupon. For quasi-static testing, the pattern is sprayed on to the coupons and allowed to cure completely. This method was attempted in early high strain rate tests using the IPL. Problems with this method arose when the base coat of paint began to chip with the material experiencing high elastic strains. To alleviate the chipping of paint from the coupon, the spray pattern was applied quickly and not allowed to dry.

First, a mask is applied to the coupon so that only 1.5 in of the center gage section is exposed, and the white base coat is evenly applied. Typically, a useable stochastic pattern is achieved by holding the black spray can 15-20 in above the coupon and indirectly spraying the can in short ~1-second bursts above the gage section until the pattern resembles those presented by GOM. Care should be taken to ensure the spray nozzle is clean.

### IPL Procedure

Before any test is started, the IPL is calibrated. The top grip should be spaced approximately 38.1 mm (1.5") above the bottom grip. A gage block is used to ensure that both grips are aligned in the X direction, and that the angle of the top grip is set to 0 degrees. Calibration is performed using LabVIEW. The actuator lengths are measured using a metric tape measure, and values are input into the correct dialogue box in centimeters. LDVT voltage is fed to the LabVIEW VI. The IPL software then knows the location of the moveable upper crosshead.

With the coupon painted, IPL calibrated, the cameras prepared for image collection, and the top and bottom grips evenly aligned, the coupon is placed in the grips; care must

be taken to ensure that the stochastic paint pattern is undamaged. The hydraulic pump is then used to apply slight pressure to the coupon. The side constraints are then lightly tapped into place and bolted firm. With the side constraints in place, the hydraulic pump is then used until the top and bottom jaws are each applying 35 kN (8000 lbf) of pressure on the coupon. Once the coupon is secure, the desired displacements, rotation, acceleration, and speeds are entered into the IPL LabVIEW VI, and the test is started. Raw load, actuator length, and grip displacements are recorded and stored in a .csv file on the IPL computer. The LabVIEW VI also runs a MATLAB script that resolves these forces into x forces, y forces, and z moment. These are exported to Aramis and can be plotted and/or sent to a .csv file. When a test is complete, the coupon is removed, and grips are moved back to their initial position. Table 9 contains the test matrix for 304 stainless steel IPL tests studied in this work.

Table 9. Steel coupon test matrix for the IPL. D1 is notch width, D2 is the reduced thickness at the coupon's midgauge. Dimensions in inches IAW IPL input parameters.

| Sample | D1 (in) | D2 (in) | Thickness (in) | dx (in) | dy (in) | dtheta (in) | speed (in/min) | accel (in/m <sup>2</sup> ) |
|--------|---------|---------|----------------|---------|---------|-------------|----------------|----------------------------|
| 1      | 0.282   | 0.150   | 0.201          | 0       | 1       | 0           | 15             | 10                         |
| 2      | 0.285   | 0.146   | 0.200          | 1       | 0       | 0           | 15             | 10                         |
| 3      | 0.282   | 0.148   | 0.201          | 0       | 0       | 10          | 15             | 10                         |
| 4      | 0.279   | 0.148   | 0.201          | 0       | 1       | 0           | 30             | 20                         |
| 5      | 0.284   | 0.151   | 0.201          | 0.5     | 0.5     | 0           | 30             | 20                         |
| 6      | 0.280   | 0.152   | 0.200          | -0.5    | 0.5     | 0           | 30             | 30                         |

## ANALYSIS PROCEDURE

### Abaqus

#### Background

While IPL testing was reproduced utilizing ANSYS in previous work completed in 2017, The Abaqus FEA software was chosen for this analysis as it offers more versatile methods of implementing user defined strain rate and temperature dependent plasticity models [17]. Abaqus 2017 includes a Johnson-Cook plasticity model [11]. Abaqus can implement the Johnson Cook model as a plastic hardening regime, a strain rate dependent hardening and a damage fracture model as defined by Johnson and Cook and outlined in the previous section. Use of these Johnson-Cook models can be controlled through the Abaqus CAE user interface and does not require knowledge of programming a custom user subroutine (UHARD) code using FORTRAN. Previous research work into Zerilli-Armstrong and Mechanical Threshold Stress plasticity models has been found, and code is published for more complex rate and temperature dependent hardening models[10, 13]. These model requires UHARD and is fed into the Abaqus simulation as FORTRAN code [11].

### Abaqus Model

#### Solid Model

The IPL test coupons were modeled in Abaqus, the geometry was modeled as it approximates the portion of the coupon being measured by the DIC system. Measurements taken before testing ensure that geometry of the cuts in each coupon accurately represent

the coupon being tested. A typical sketch used to create the solid model is shown below in Figure 25.

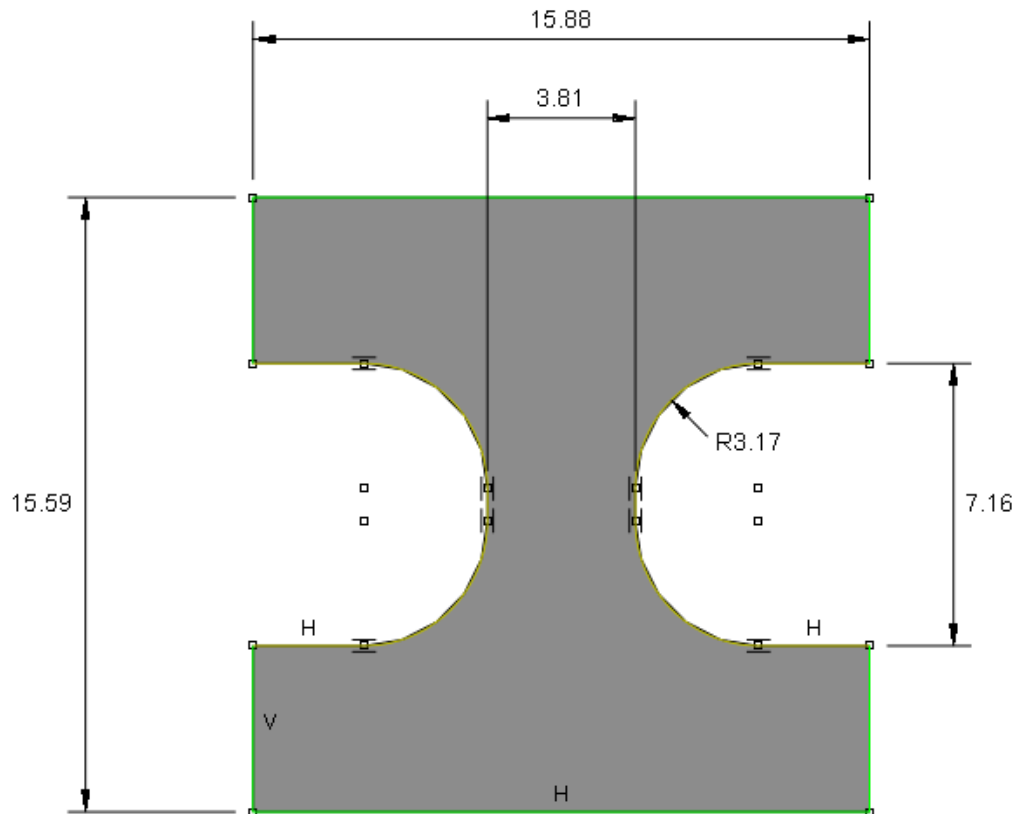


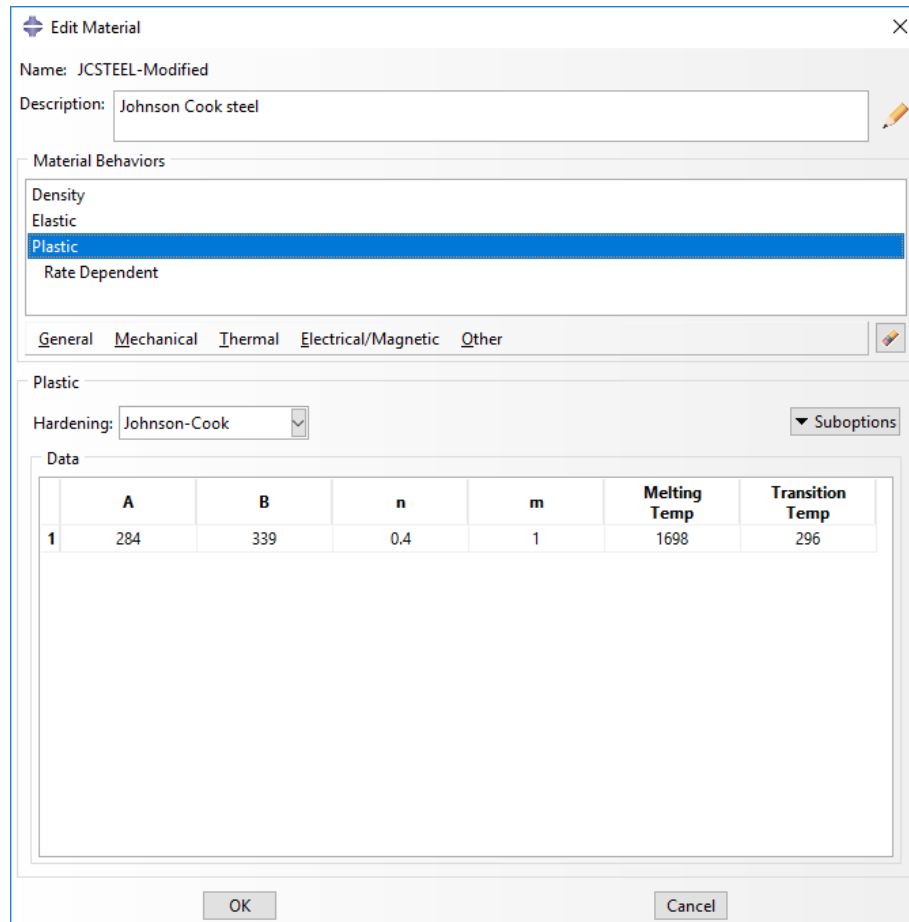
Figure 25. IPL Coupon geometry as modeled in Abaqus/CAE 2017 (dimensions in millimeters)

The part is then given a solid, homogenous section assignment, thickness was measured before the test and input as the extrusion thickness for the 3D solid model.

### Material Model

For 304 Steel that was purchased in hot rolled bar stock from McMaster Carr (p/n 5992K497), density was supplied as  $8000 \text{ kg/m}^3$ . As previously mentioned, Johnson Cook

parameters, and elastic modulus were found by a curve fitting script in MATLAB. To model plastic deformation in the FEM, Abaqus includes a Johnson-Cook rate dependent plasticity function.



**Edit Material**

Name: JCSTEEL-Modified

Description: Johnson Cook steel

**Material Behaviors**

Density

Elastic

**Plastic**

Rate Dependent

General Mechanical Thermal Electrical/Magnetic Other

**Plastic**

Hardening: Johnson-Cook

Suboptions

**Data**

|   | A   | B   | n   | m | Melting Temp | Transition Temp |
|---|-----|-----|-----|---|--------------|-----------------|
| 1 | 284 | 339 | 0.4 | 1 | 1698         | 296             |

OK Cancel

Figure 26. Initial Johnson-Cook material parameters as input into Abaqus/CAE

### Mesh

Abaqus was input to use a hexahedral mesh through the entire model. To properly simulate the square facets of the Aramis software partitions were used to control element shape and size in the gage section. Element size in the dog-boned section was defined to be approximately 0.215 mm, as this is the average size of an Aramis facet. To control this,

partitions are used on the front face of the coupon. The “seed edges” command is used along these partitions to refine the mesh. To improve computation times, element size is increased to a global value of 1 mm in the rest of the solid model. This size increase was deemed acceptable as the dog bone geometry acts to concentrate higher strains in the desired area.

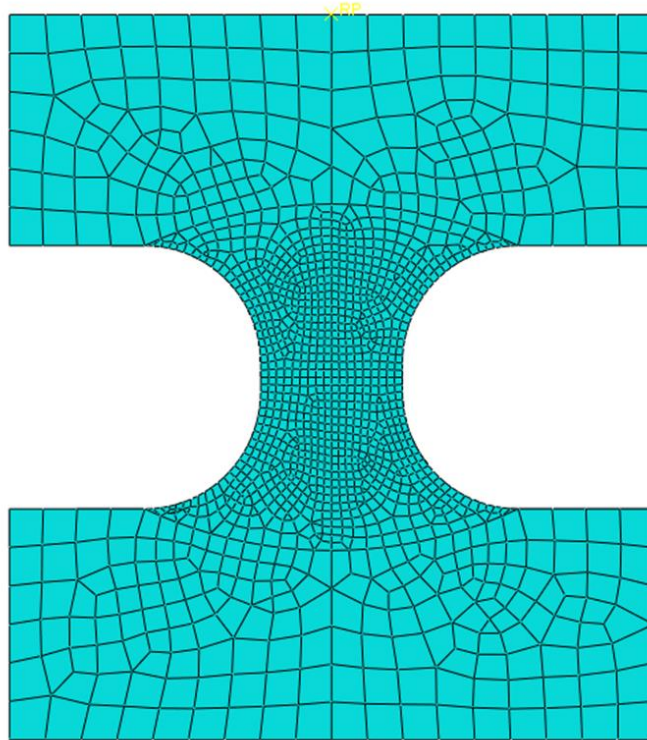


Figure 27. Meshed IPL sample geometry in Abaqus.

#### Dynamic, Implicit Loading

The user hardening subroutines require an implicit dynamic FEA model to operate. As such, all models were run in this setting, which allows the models to retain the utility of a custom user hardening routine. Because this study is interested in non-linear plastic deformation of materials, an implicit dynamic analysis was used due to the transient nature

and 6-20s duration of an IPL test. Attempts were made to run the analysis as an explicit dynamic analysis, this resulted in wave speed errors in the material, causing deformations to only occur in the first row of elements, or no deformation in the reduced thickness gage section. The settings for the analysis are shown in figure 17. The implicit dynamic step is given its prescribed time (as taken from the Aramis test being modeled), maximum number of increments can be specified, as a well as initial and minimum increment size. Increment size and number of increments were tuned to improve computation time. A typical IPL test simulation in Abaqus requires 10-20 minutes to complete while running on “Sphinx” a quad-core computer dedicated to running Abaqus simulations.

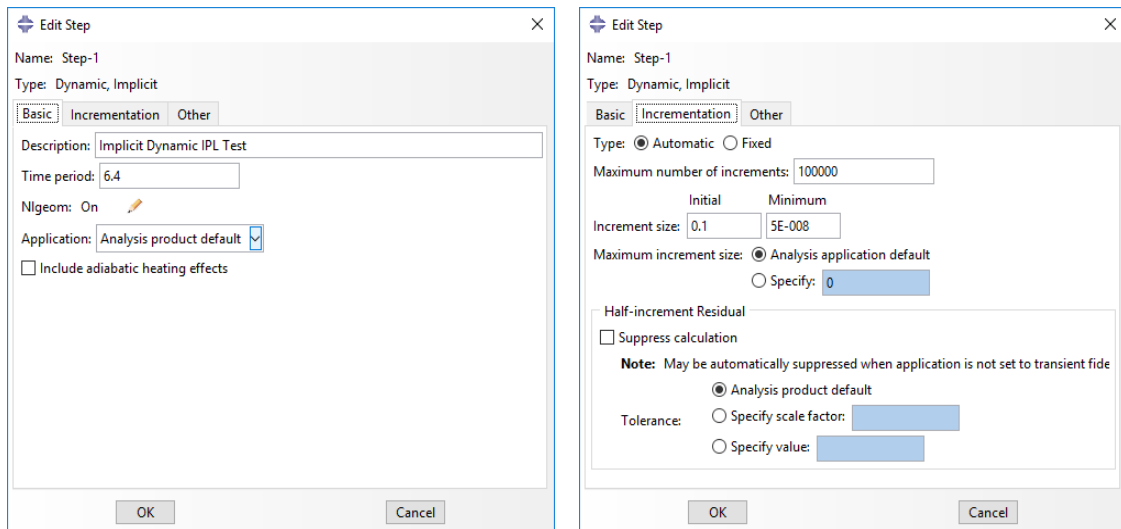


Figure 28. Abaqus dialog box showing parameters used in the implicit dynamic step.

### Boundary Conditions

The implicit, dynamic analysis is run in two steps. The initial step is used to prescribe a boundary condition simulating the lower, stationary portion of an IPL coupon. This is accomplished using 3 separate boundary condition assignments, one each for the x,

y, and z directions in the model. First, motion in the y is constrained on the entire bottom surface of the model. To constrain translations in the x and z directions, partitions are created across the center of the bottom surface along both the x and z directions. Zero-displacement boundary conditions are then applied in the z direction along the x partition, and in the x direction along the z partition. This combination of zero displacement conditions also inhibits out of plane rotation in the coupon. These boundary conditions allow for the coupon to contract in the z and x direction due to the materials Poisson's ratio. Figure 29. Boundary conditions applied to the bottom surface of the coupon. shows the applied boundary conditions.

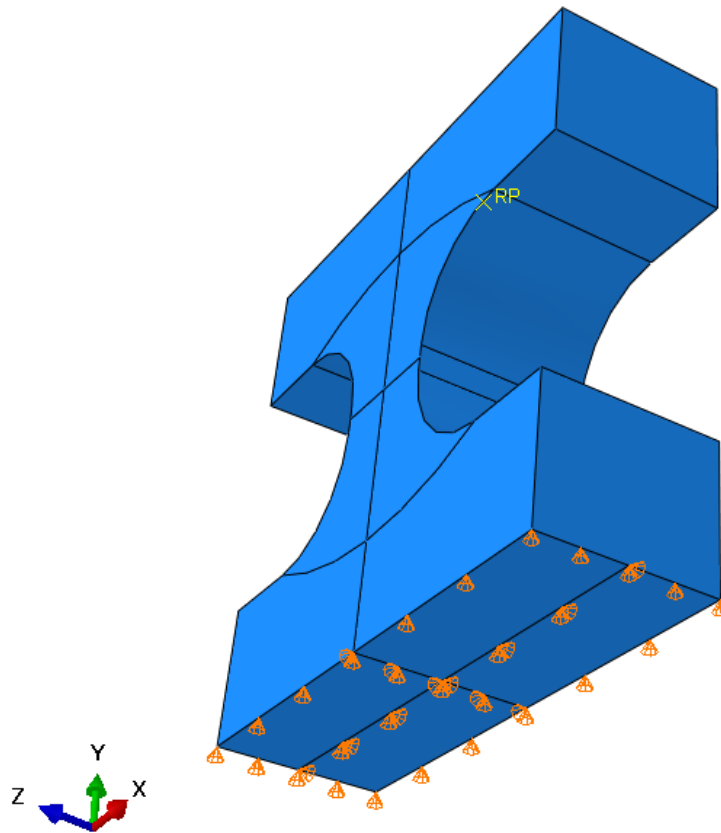


Figure 29. Boundary conditions applied to the bottom surface of the coupon.

To simulate a multiaxial IPL test, a reference point is created and placed on the center of the top face of the coupon model, the desired objective of this process is to take x, y, and angular displacements of a point as recorded by the Aramis cameras, and repeat the same displacements in Abaqus. In this method, all displacements are applied to the Reference Point.

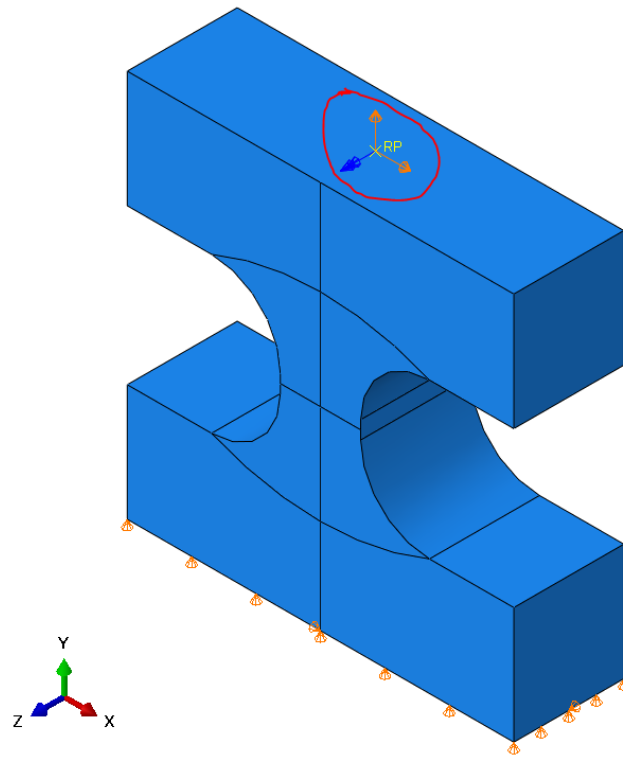


Figure 30. Depiction of reference point (in red circle) location on the 3D solid model.

A kinematic coupling constraint connects displacements of the reference point to the top surface of the model. Figure 30 is a detail view of the reference point, and Figure 31 is the Abaqus coupling dialogue box used to link reference point motion to the surface.

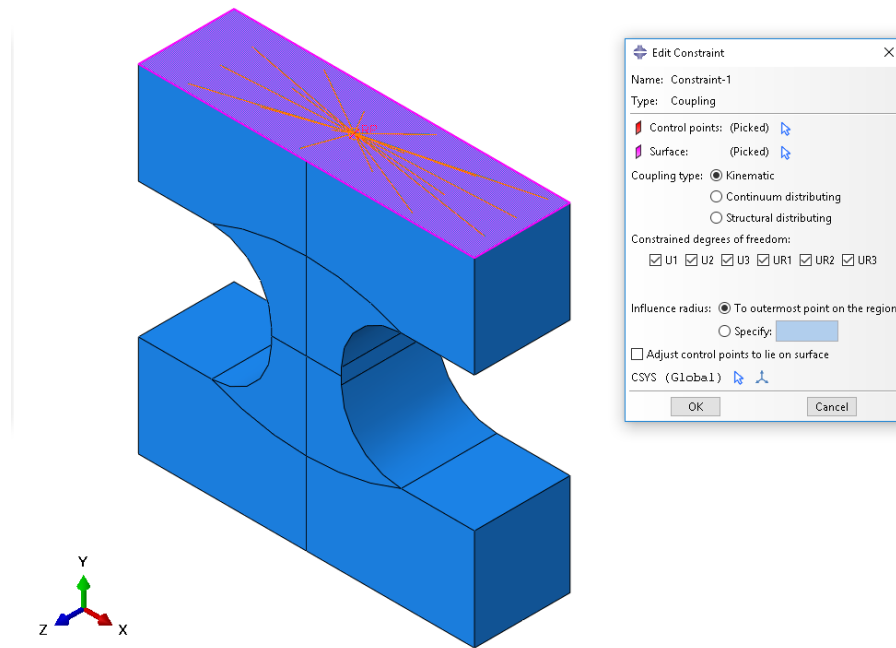
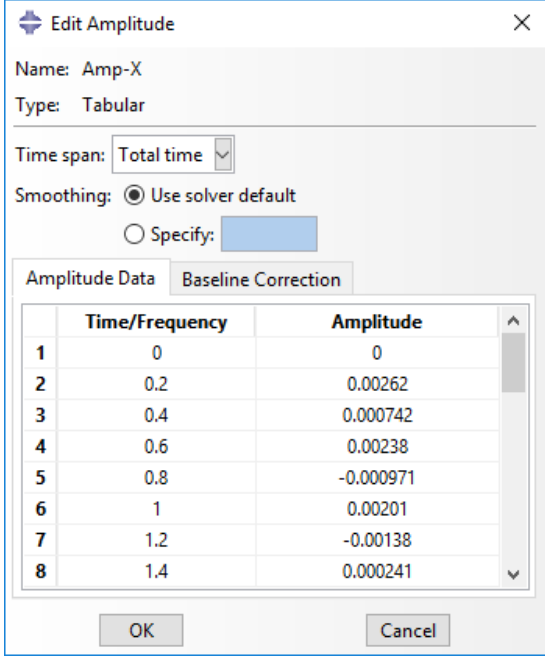


Figure 31. A Coupling Constraint is used to couple displacements of a control point (RP) to a surface (top surface of coupon). Displacement of the surface is dictated by the reference point in all directions.

Next, three amplitude tables are created; these tables store data for time, and either x, y displacement in millimeters, or angular displacement in radians. The time and displacement data input into these tables is imported from Aramis, which exports stage data as a .csv file.

Data is copy and pasted from the .csv file to the Abaqus table as shown in Figure 32. Table of time and displacements, in millimeters (displacement) or radians (rotation) as exported from Aramis and imported into Abaqus.



|   | Time/Frequency | Amplitude |
|---|----------------|-----------|
| 1 | 0              | 0         |
| 2 | 0.2            | 0.00262   |
| 3 | 0.4            | 0.000742  |
| 4 | 0.6            | 0.00238   |
| 5 | 0.8            | -0.000971 |
| 6 | 1              | 0.00201   |
| 7 | 1.2            | -0.00138  |
| 8 | 1.4            | 0.000241  |

Figure 32. Table of time and displacements, in millimeters (displacement) or radians (rotation) as exported from Aramis and imported into Abaqus.

Three displacement boundary conditions are created, one for each degree of freedom permitted by the IPL motion. U1 and U2 are x and y respectively, UR3 is a positive clockwise rotation. As Aramis displacements are input in each respective table, each displacement is given a value of 1, with a uniform distribution, its respective amplitude is selected from the dropdown menu. The boundary conditions are assigned to the Reference Point created previously.

Figure 33 is the dialogue box for the motion in the x direction, linking the amplitudes from Figure 32 to the reference point.

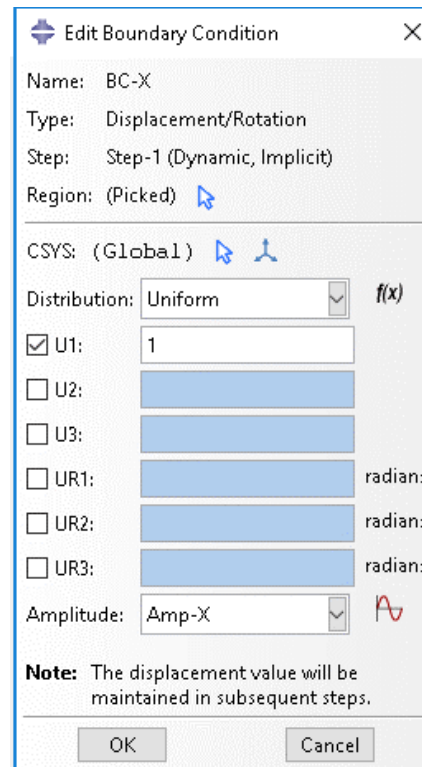


Figure 33. Boundary condition dialogue box showing the X displacement applied to the reference point. This is repeated for Y and rotation displacements (U2, UR3).

Before created in running the job in Abaqus, a field output request is created. This feature is used to store a variety of force, displacement, and energy data throughout the model. In this case stress, strains, displacements, and reaction forces. These can later be accessed as XY data, exported as an excel or .csv file, and plotted using Abaqus or another plotting software.

Finally, the Abaqus input file is created and the simulation is run. Results are stored in an odb file, which can be viewed in the CAE user interface.

Initially, a two-dimensional plane-stress element was chosen in attempt to reproduce test results. A plane stress element does not allow stress to act in the Z direction, given that the X and Y dimensions of an IPL coupon are larger than the Z direction thickness, the IPL only applies loads in X, Y, and a moment about Z. This assumption was determined to be inaccurate, so the 3D model described above was used. It is important to note here that the Aramis system only collects data on the face of the coupon.

### Post Processing Data

The Aramis software generates a strain field by tracking differences in the stochastic pattern from frame to frame. Strain data can be viewed in primary directions,  $\epsilon_x$ ,  $\epsilon_y$  and  $\epsilon_{xy}$  ( $\epsilon_{11}$ ,  $\epsilon_{22}$ , and  $\epsilon_{12}$  in Abaqus). While strain output can be provided in various transformations, the primary directions were chosen as they provide a clear picture of the raw strain data and noting that for stress and strain transformations to be accurate, the values should be accurate in the x, y, and z directions. For an IPL test up and right are positive for x and y respectively, positive rotations follow the right-hand rule.

Using measured coupon geometry, the coordinate system is centered in the gage section of a coupon. From here, Aramis is used to generate a section from points at each facet intersection across the surface, running through the center of the gage section across the x and y directions. Time, strain, and point location are output to a .csv file for each image in the image series.

Abaqus creates an odb file, which contains requested field output variables of interest. Postprocessing for the Abaqus output file entails creating a “path” along the coupon geometry at the section of interest. “XY data” is stored in a table at each element

that intersects the path for any requested field variable. Variables output by both Abaqus and Aramis that were deemed important for this work are: initial x and y coordinates of each facet or element, and logarithmic (log) strain in each primary direction. Log strain is defined in the Abaqus documentation as Equation 16 [11]

$$\epsilon^L = \sum_{i=1}^3 \ln \lambda_i \mathbf{n}_i \mathbf{n}_i^T \quad (16)$$

Where  $\lambda_i$  are the principal stretches, and  $\mathbf{n}_i$  are the principal stretch directions [11]. Logarithmic strain was chosen for its usefulness in calculating strain in small increments. Log strain accounts for strain history. This makes it to a useful method for path dependent loads, and strains [29].

Both programs generate 2D plots of data, Microsoft Excel is used to combine the experimental Aramis data with the data generated by the Abaqus FEA model to allow for direct comparison.

Both Abaqus and Aramis produce colored contour plots to depict strains, displacements, and velocities. An example of this can be seen below in Figure 34 and Figure 35.

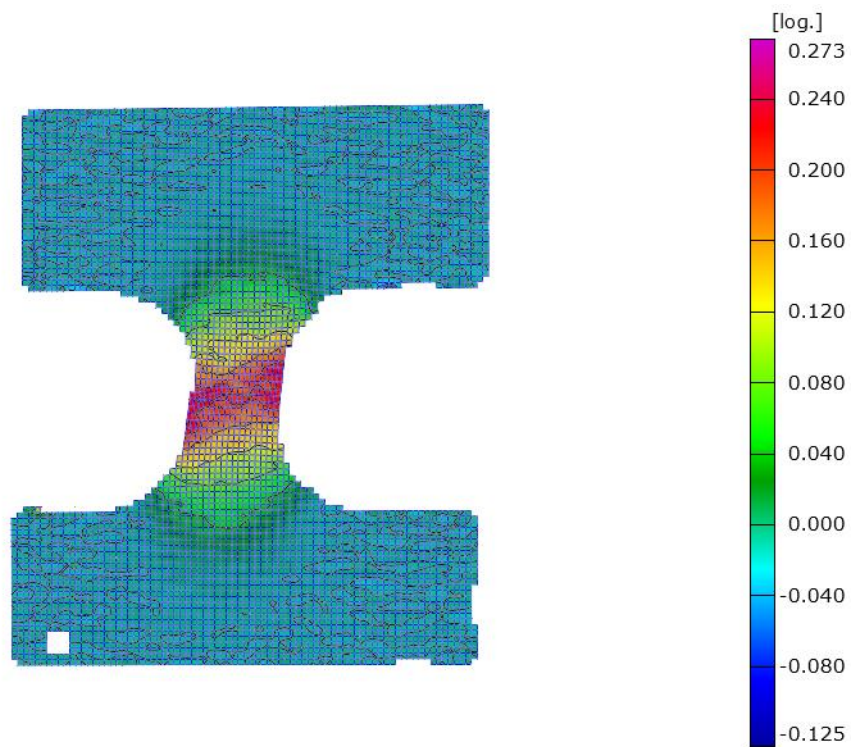


Figure 34. Aramis contour surface showing  $\epsilon_{22}$  for a stainless steel coupon, facet grid is shown. Note the hole in the bottom left corner.

The surface is a useful approach for visualizing a two-dimensional strain field. In the example above its strength is showing the general shape of the gradient, but it does not provide a clear quantitative analysis of strain at specific points on the surface.

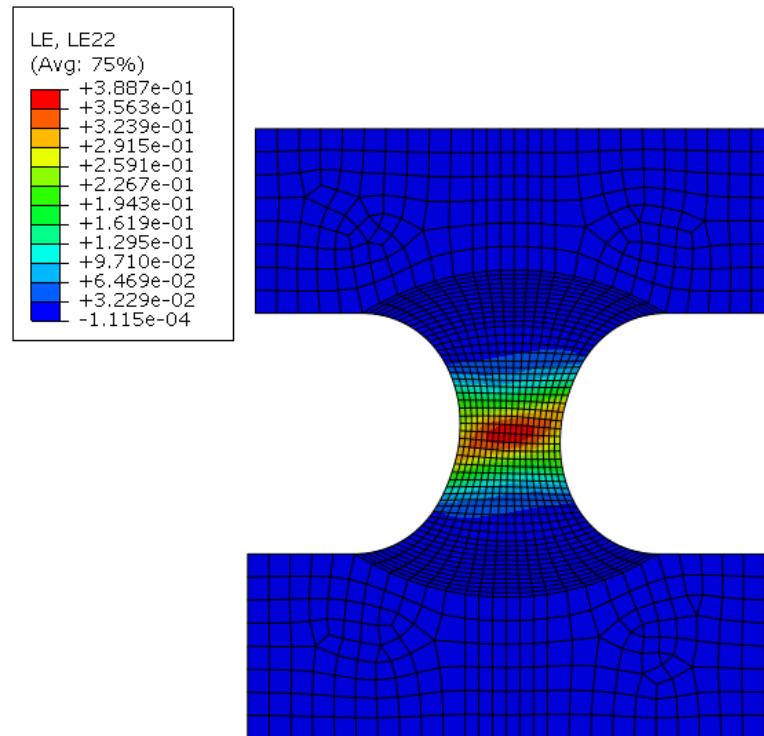


Figure 35. Abaqus contour surface showing  $\epsilon_{22}$  for a stainless steel coupon, elements in the center of the model are approximately the size of an Aramis facet.

To better study differences between experimental and the FEA model, values were collected along cross sections of interest in Aramis and Abaqus. This allows for a direct comparison of strain along the coupons gage section. These sections can be seen in Figure 36 and Figure 37.

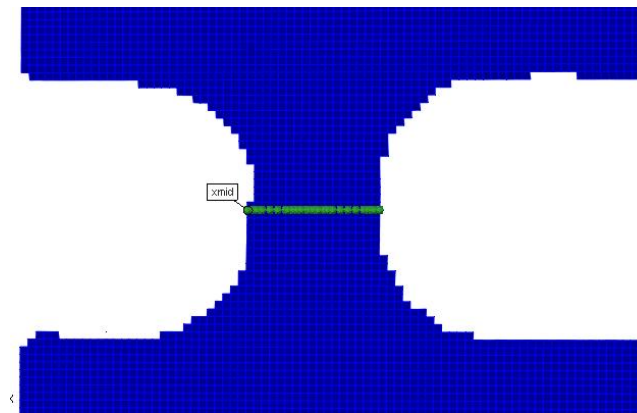


Figure 36. Aramis cross sectional path on an IPL coupon.

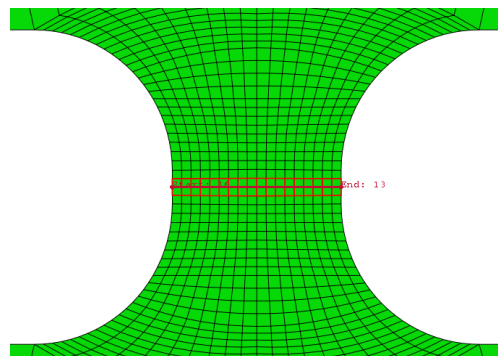


Figure 37. Highlighted Abaqus cross sectional path.

The sections deform with the coupon, meaning they track data for the same facet/element as time progresses. This feature is illustrated in Figure 38 and Figure 39.

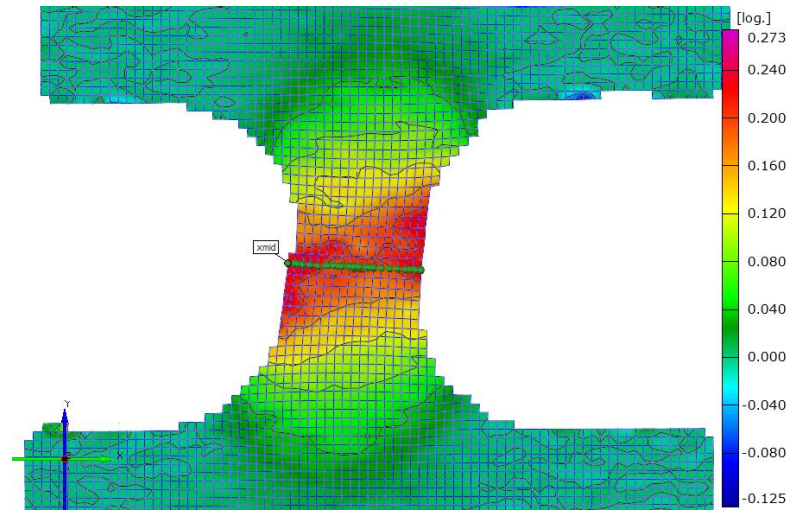


Figure 38. Deformed shape of a center section in Aramis.  $\epsilon_{22}$ .

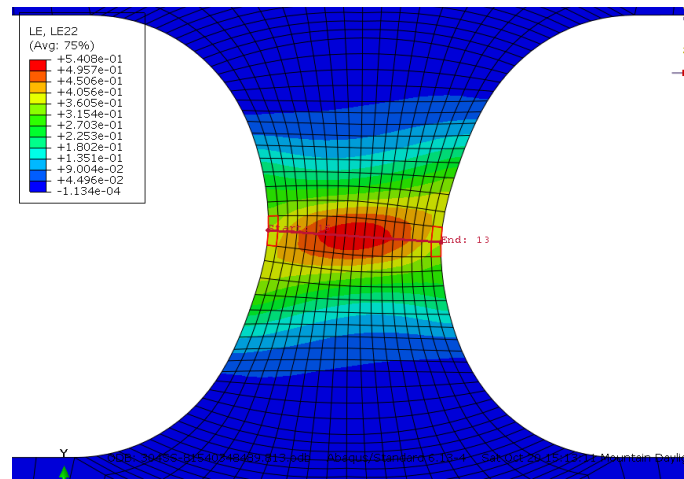


Figure 39. Deformed shape of a center section in Abaqus.  $\epsilon_{22}$

The section strain data for each time step from Aramis and Abaqus are combined in a common excel file. The Excel file is then imported to MATLAB for plotting.

## RESULTS AND DISCUSSION

### Strain Rate Sensitive Characterization of Materials

The initial goal of this work was to validate the IPL's ability to test and characterize strain rate sensitive materials. Initial testing with 304 stainless steel in the summer of 2017 led to the current steel coupon geometry as seen in Figure 22. A testing matrix for stainless steel coupons at varying speeds is shown in Table 9.

A series of tests were run prior to those found in Table 9, these were used to qualitatively analyze the IPL's capabilities. Testing at speeds above 10 inches per minute resulted in notable cases of grip slippage. At this point the slipping appears to be dependent on both load rate and load path.

Even though geometry was optimized in this process to minimize slipping it should be noted that certain load paths and speeds continued to show coupon to slip in the lower IPL grip during testing. Figure 40 illustrates grip slip for two IPL test coupons listed above.

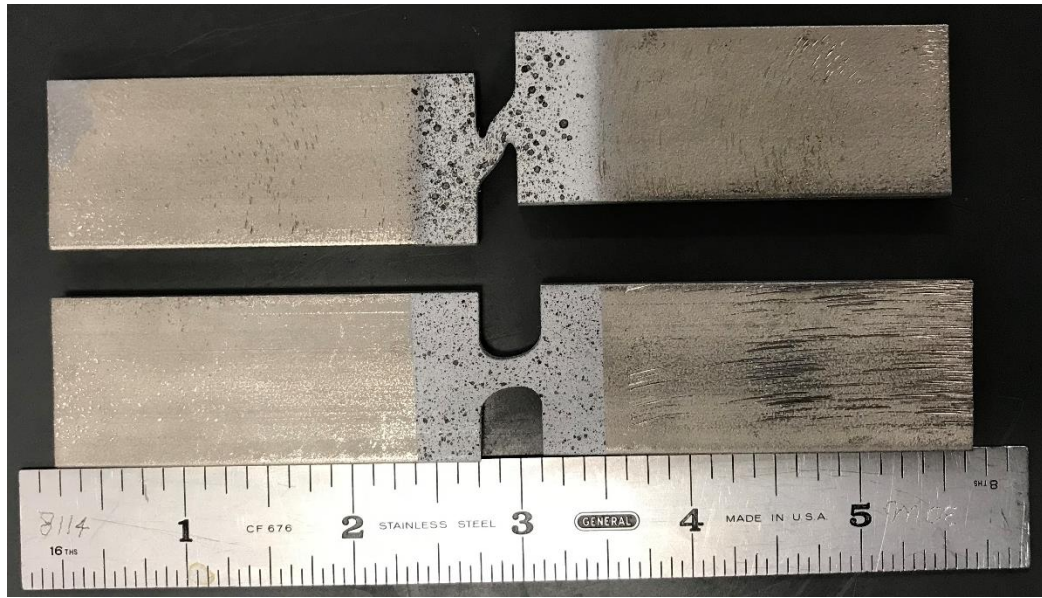


Figure 40. Samples showing striations on the right half of the coupons indicating severe grip slip. Rotation (top) and Vertical (bottom)

### Comparison of Results

Given that the initial interest is in characterizing multi-axial, strain rate sensitive plasticity models, results are dependent on 2 dimensional displacements and time. To clearly compare experimental DIC results with an FEA model, a method was developed which allowing for a researcher to show the evolution of stress and strain in a coupon throughout time.

As previously outlined in the testing procedure section, Abaqus is given inputs for the Johnson-Cook plasticity model that were determined by quasi-static tensile testing. The

results of the 5 tensile tests were averaged and can be seen in Table 8. These coefficients were then fed into the Abaqus model, which was run to simulate the quasi-static tensile tests. Stress and strain at the center of the coupon were then plotted and are compared against experimental tensile data in Figure 41.

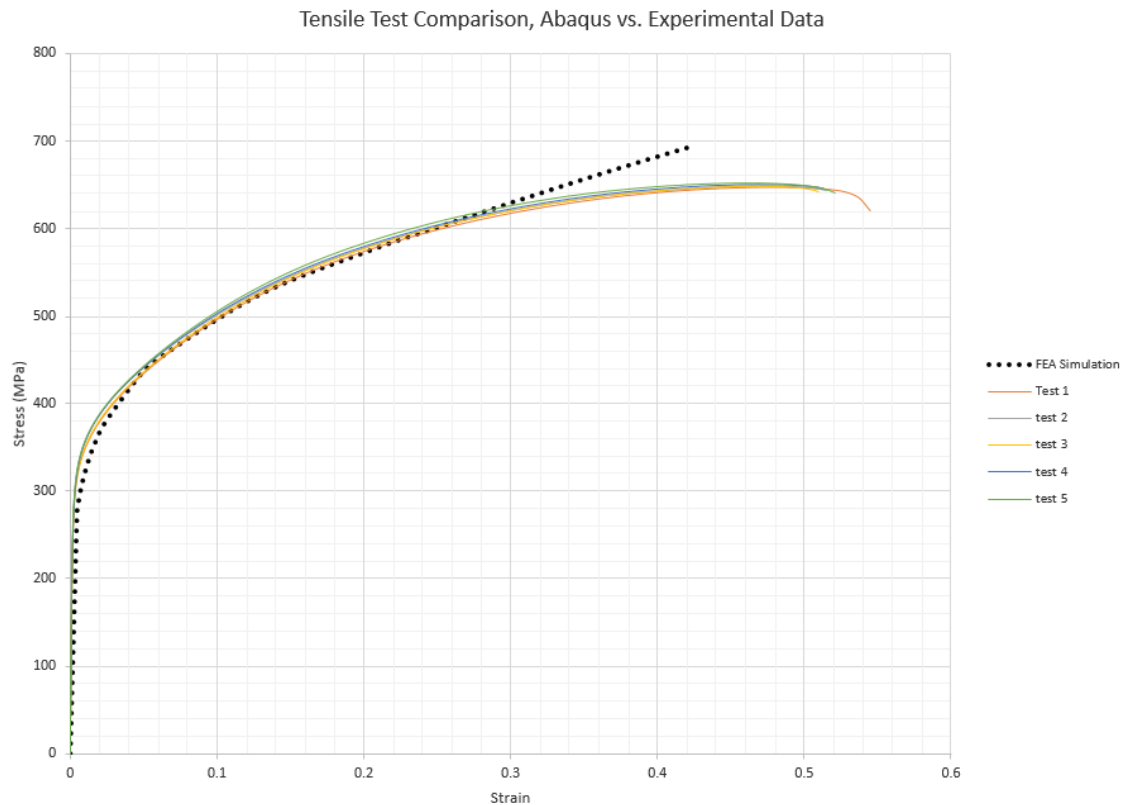


Figure 41. Plot comparing the J-C model determined in Table 4 with experimental tensile data.

The simulations fit to the experimental data shows that the implicit/dynamic Abaqus model can accurately model stress and strain in a coupon when fed one dimensional displacement boundary conditions. The tensile tests show a strain to failure of between 50% and 60%. The Johnson Cook FEA model shows the simulation deviating

from experimental results at 30% strain, this value was set as the limit for which Abaqus was used to predict mechanical behavior of 304 stainless steel.

With the FEA model verified for tensile testing, the focus is changed to comparing FEA with DIC results. The DIC collects data at 5 Hz, and the average IPL test runs between 5 and 20 seconds. Each coupon contains approximately 1000 individual facets, Aramis produces a tremendous .csv files containing load and displacement data for each facet at each time step. The raw section strain data is then plotted for the 3 primary strains,  $\epsilon_{11}$ ,  $\epsilon_{22}$ , and  $\epsilon_{p1}$  ( $\epsilon_x$ ,  $\epsilon_y$ , and maximum principal strain, respectively). An example of this is shown in Figure 42, Figure 43, and Figure 44.

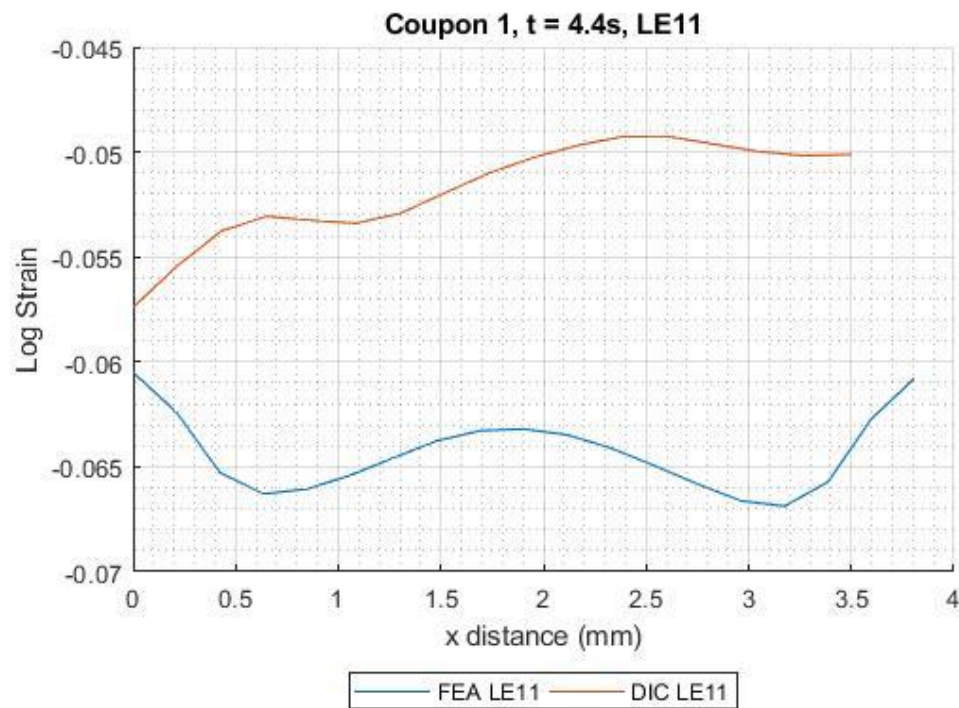


Figure 42. Plot of  $\epsilon_{11}$  along center of an IPL coupon 4.4 seconds into a test.

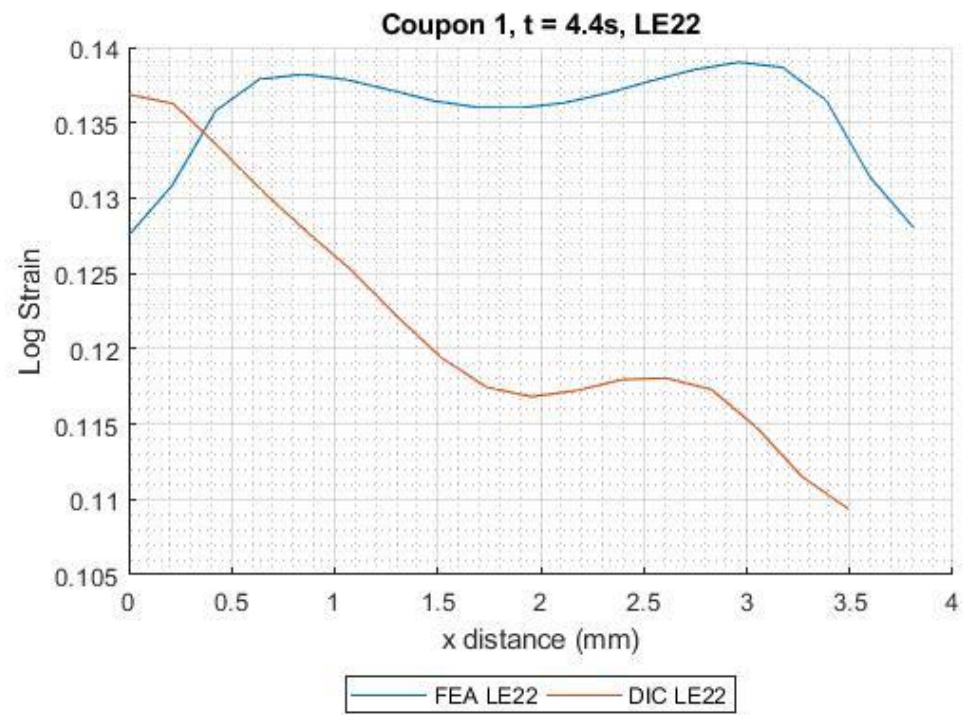


Figure 43. Plot of  $\epsilon_{22}$  along center of an IPL coupon, 4.4 seconds into a test.

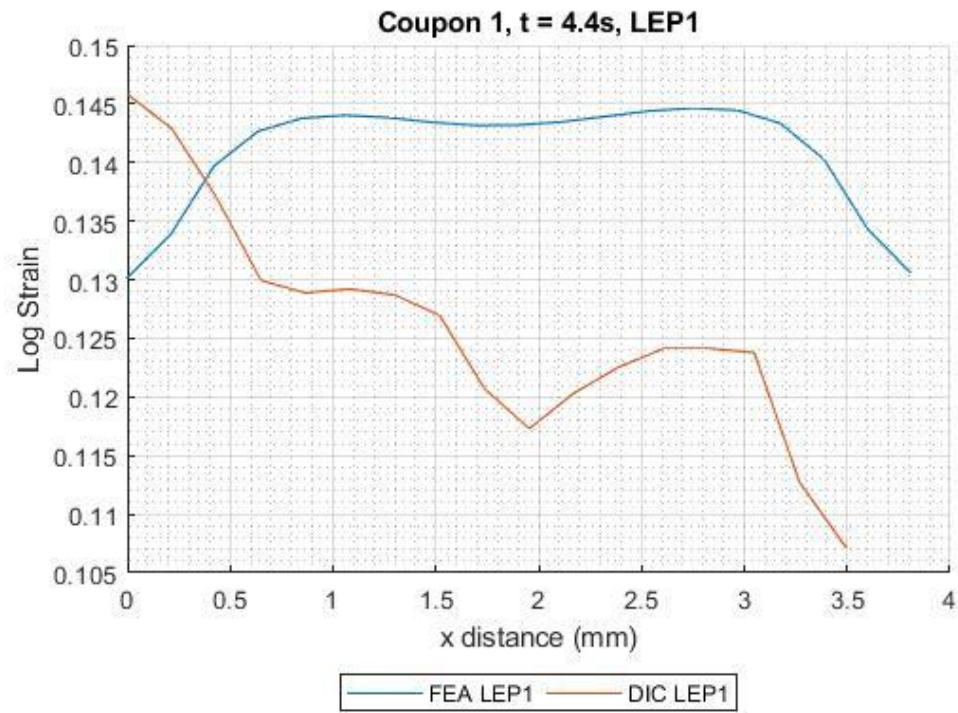


Figure 44. Plot of  $\epsilon_{P1}$  (maximum principal strain) along center of an IPL coupon, 4.4 seconds into a test.

These plots are further refined by selecting points of interest along the cross sections, strain at these points is input into the Johnson Cook curve fit equation graphed in Figure 41. Figure 45 shows the location used for the examples.

Figure 46, Figure 47, and Figure 48 depict the FEA and experimental data fit to the Johnson Cook curve at a point 2mm into the coupons gage section. As stress data was not collected during IPL testing, location on the line is based purely off the maximum principal strain in the sample. This is done to depict which portion of the Johnson-Cook stress vs. strain curve the sample is expected to be at during the test, based on tensile test data.

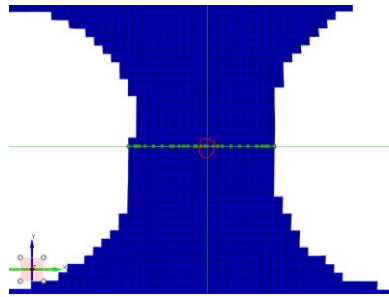


Figure 45. 2mm into coupons gage section. ( $x = 2\text{mm}$ ,  $y = 0\text{mm}$ ).

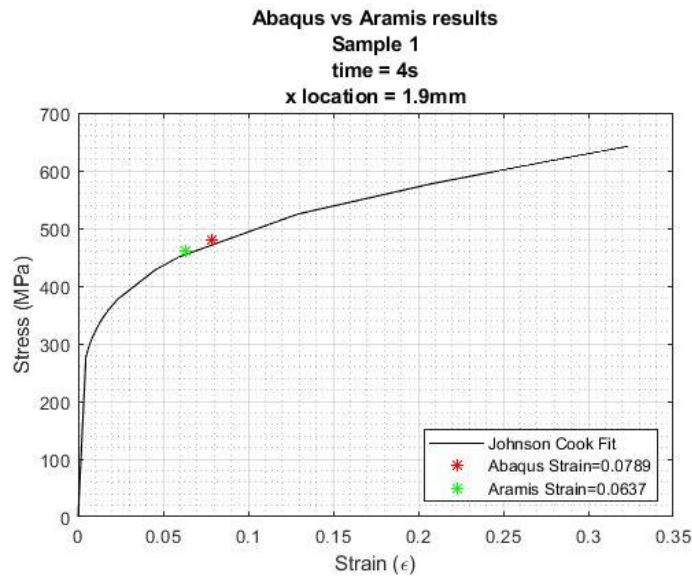


Figure 46. Plot of maximum principal strain for FEA and DIC strain results, appx. 2 mm into a coupon

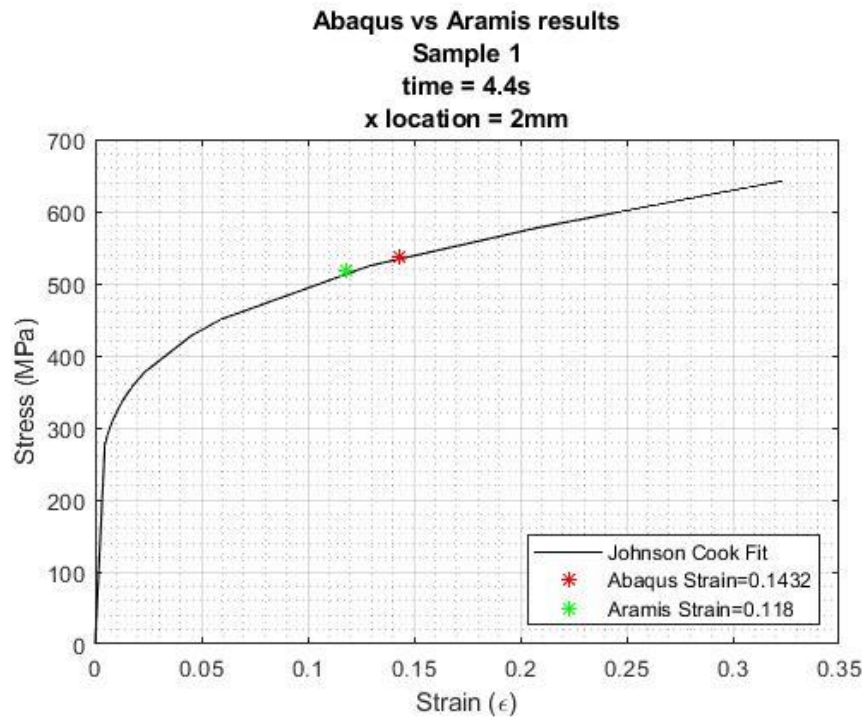


Figure 47. Plot of maximum principal strain for FEA and DIC strain results, appx. 2 mm into a coupon.

The stress vs. strain plots combined with the 2D strain section plots allow for a clear visualization of the strain in the material extracted from the contour plots. These 3 plots combined can be used to compare the accuracy of the strain field between the simulated model and experimental data.

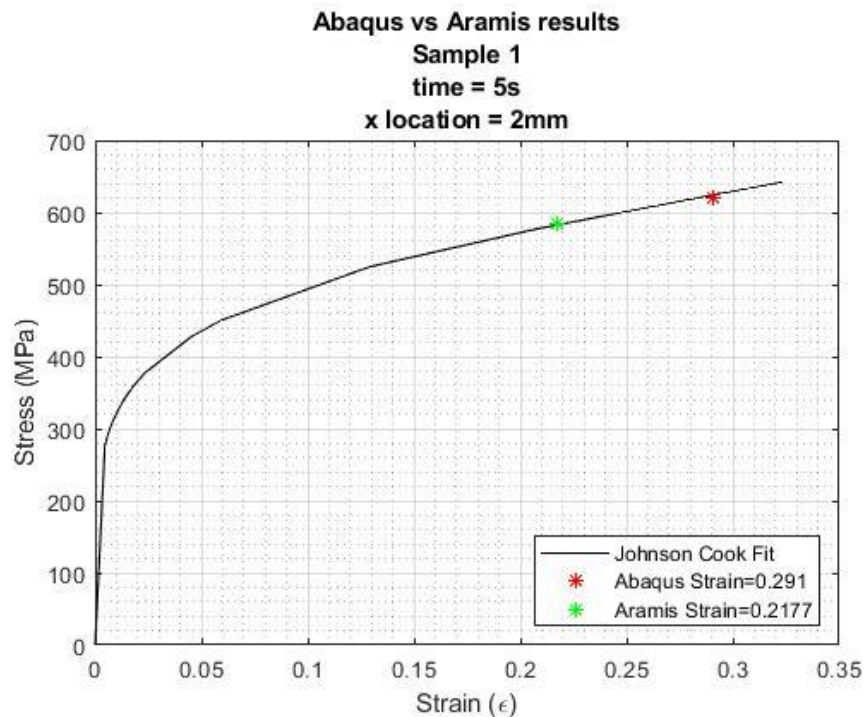


Figure 48. Plot of maximum principal strain for FEA and DIC strain results, appx. 2 mm into a coupon.

#### IPL Sample 4 -304 Stainless Steel

Sample 4 in Table 9 raised questions in the accuracy of the data collection processes and calibrations. Of the tests ran, this was the closest example to a tensile test being run in the IPL. Displacement of the coupon at failure was reported by Aramis to be 2.508 mm in the y direction and 0.138 mm in the x. Stage times that will be examined in detail for this

experiment are 2.0 seconds, 3.4 seconds, 4.0 seconds, and 4.8 seconds, as they provide a wide range of strains from the linear elastic region into the plastic strain region.

In Figure 49 the 2D contour surface at 2.6 seconds in Abaqus shows that at a displacement of 0.005mm x, and 0.016mm y and applied the coupon should be experiencing a 0.25% strain in concentrated areas. In comparison, the Aramis camera is not detecting a defined strain field this is most likely due to facet sizing, and camera settings. This occurs in the 11 and 12 directions as well.

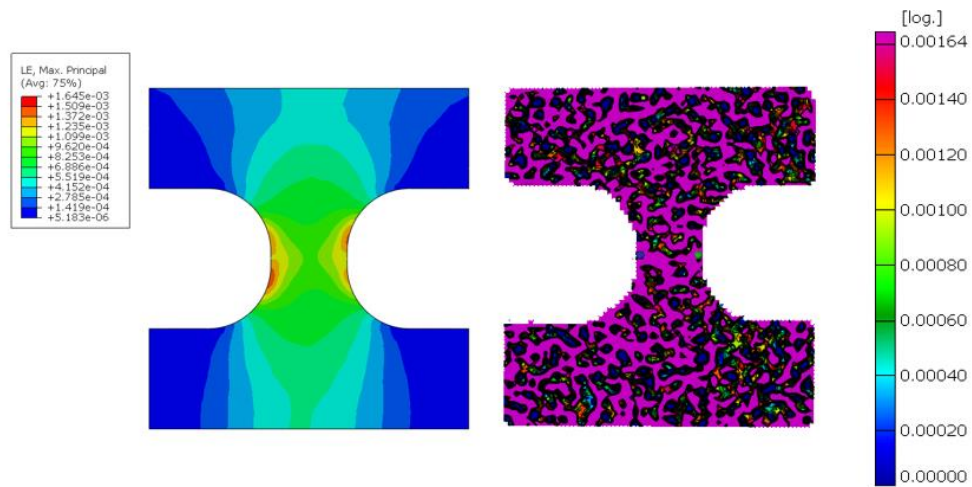


Figure 49. Comparison of strain fields at 2 seconds, coupon 4,  $\epsilon_{22}$ . (L: FEA, R: DIC)

Further analysis at this timestep along the cross section highlights the discrepancy between the FEA model and the DIC data.

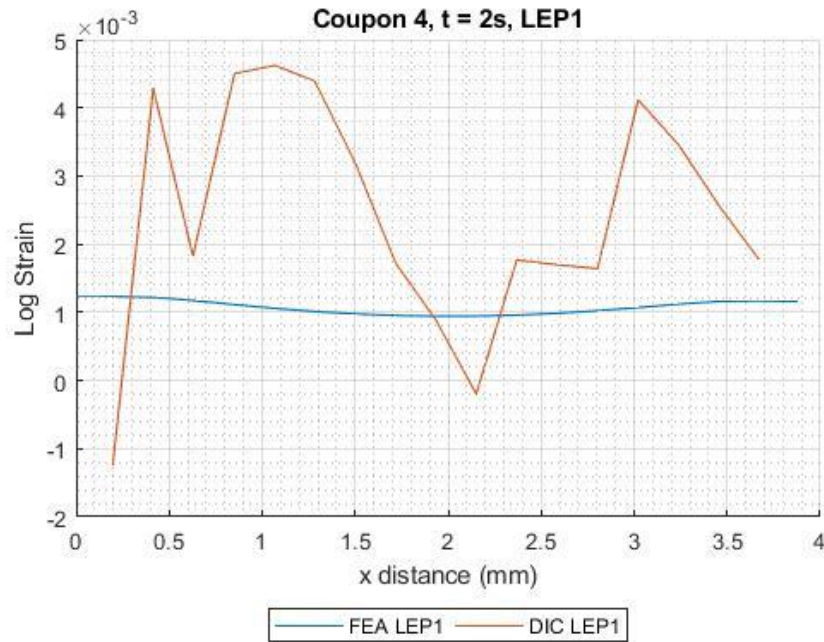


Figure 50. Cross sectional strain at the center of sample 5 at 2.6s,  $\epsilon_{P1}$

The large variation in the strain for the DIC results indicates that the sensor is not able to distinguish displacement from signal noise.

Table 10 contains the percent differences between maximum principal strain between the FEA model and the Aramis measurements. At small strains, above the proportional limit strain (0.0005) the percent differences show a large variation, with differences ranging from 6.5% to 338% difference in reading between the two.

Table 10. Percent differences between the maximum principal strain in the FEA and DIC results along the center of the gage section.  $t=2s$

| Max Principal Strain, $t = 2s$ |            |        |           |         |
|--------------------------------|------------|--------|-----------|---------|
| FEA                            |            | DIC    |           |         |
| x(mm)                          | Log Strain | x (mm) | P1 Strain | %diff   |
| 0.22                           | 0.0012     | 0.20   | -0.0012   | 199.96  |
| 0.43                           | 0.0012     | 0.41   | 0.0043    | -252.26 |
| 0.65                           | 0.0012     | 0.63   | 0.0018    | -55.91  |
| 0.86                           | 0.0011     | 0.85   | 0.0045    | -305.63 |
| 1.08                           | 0.0011     | 1.07   | 0.0046    | -338.06 |
| 1.30                           | 0.0010     | 1.28   | 0.0044    | -335.25 |
| 1.51                           | 0.0010     | 1.50   | 0.0032    | -226.94 |
| 1.73                           | 0.0010     | 1.72   | 0.0017    | -80.09  |
| 1.94                           | 0.0009     | 1.94   | 0.0009    | 6.52    |
| 2.16                           | 0.0009     | 2.15   | -0.0002   | 120.83  |
| 2.37                           | 0.0010     | 2.37   | 0.0018    | -84.17  |
| 2.59                           | 0.0010     | 2.59   | 0.0017    | -72.13  |
| 2.81                           | 0.0010     | 2.80   | 0.0016    | -60.20  |
| 3.02                           | 0.0011     | 3.02   | 0.0041    | -284.75 |
| 3.24                           | 0.0011     | 3.24   | 0.0035    | -208.17 |
| 3.45                           | 0.0012     | 3.46   | 0.0025    | -118.88 |
| 3.67                           | 0.0012     | 3.67   | 0.0018    | -50.97  |

At a time of 3.4 seconds into the test, the coupon is under displacements of 0.002 mm in the x, and 0.037 mm in the y. The DIC system begins to show variation in the strain field but does not show this as clearly as the FEA simulation does.

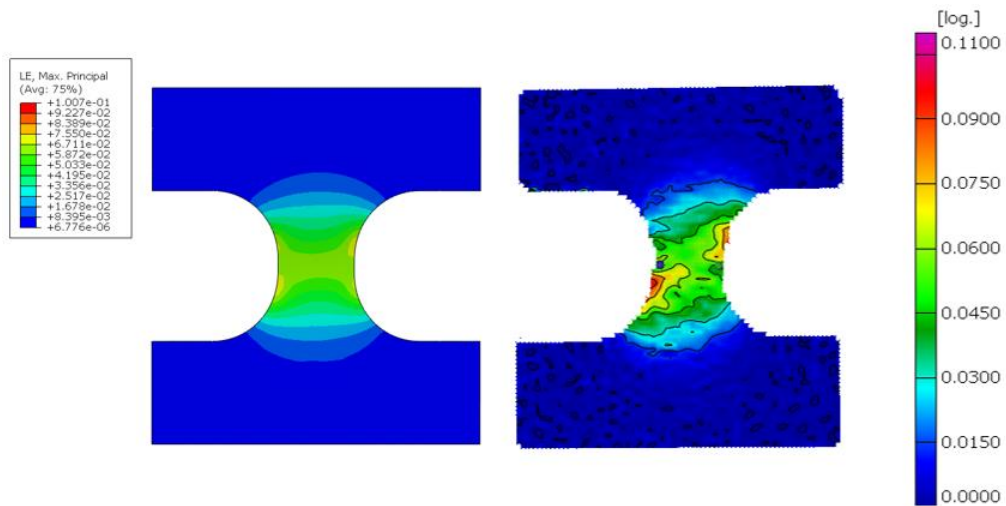


Figure 51. Comparison of strain fields at 3.4 seconds, coupon 4,  $\epsilon_{p1}$  (L: FEA, R: DIC)

The 2D cross section in Figure 52 can again be used to highlight the strain differences along the gage section between the two.

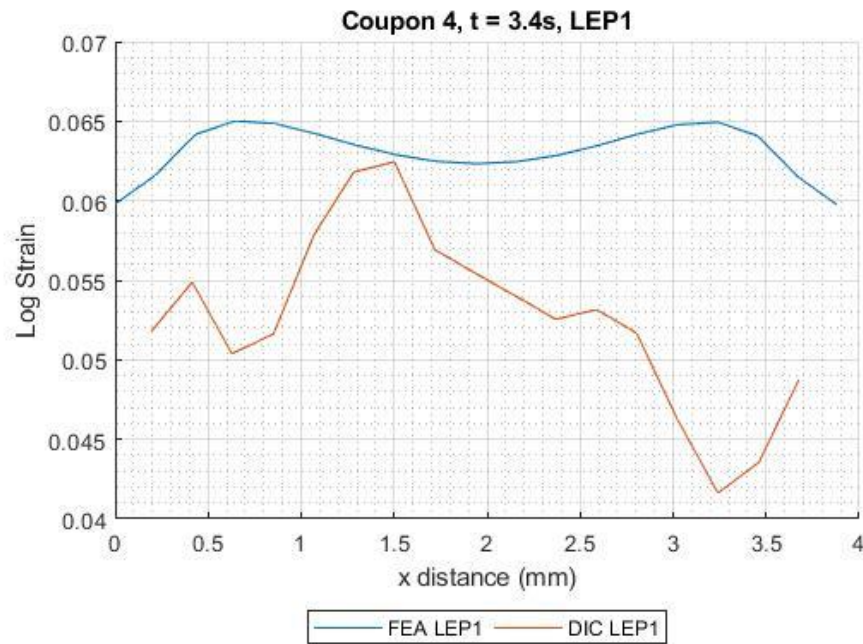


Figure 52. Cross sectional strain at the center of sample 4 at  $t=3.4s$ ,  $\epsilon_{p1}$

To more clearly visualize the differences between the two, points of interest are plotted along the Johnson-Cook curve fit equation.

Looking at a point in the cross section 1.94 mm into the material, Figure 53 is used here to show the difference between FEA and DIC along the stress-strain curve.

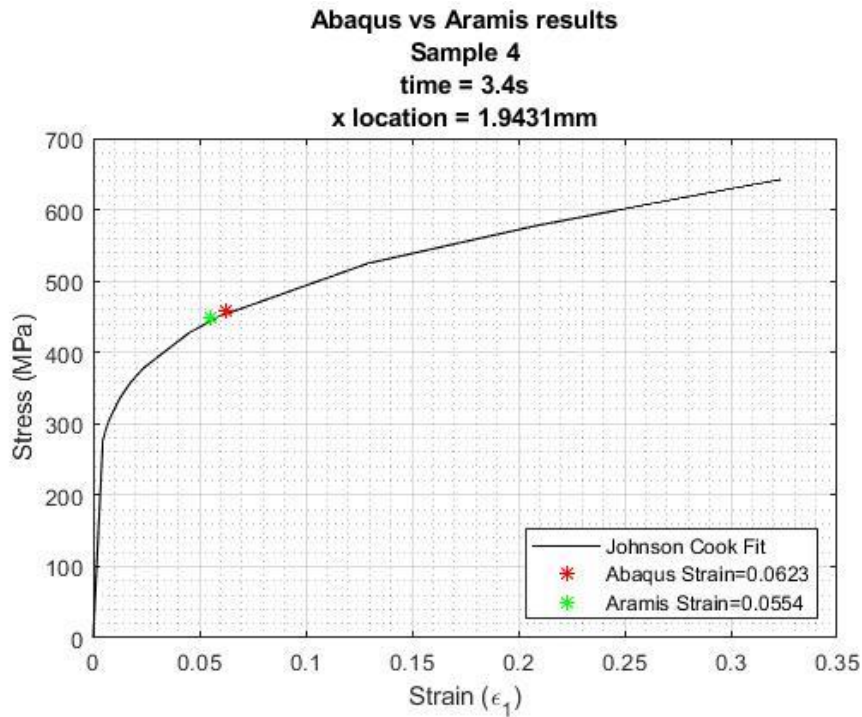


Figure 53. Plot relating  $\epsilon_{P1}$  from the FEA model and experimental to the Johnson Cook curve fit. At 3.4 seconds, 1.94 mm into the gage section. Plot illustrates expected stress value at measured strain.

In an ideal case, these points would move along the stress-strain curve together, this is occurring in the 1-1 and 1-2 directions as well.

With the coupon now into its plastic region as depicted in Figure 53, percent difference between the two values range between 0.69% and 35%. While the difference values appear to have leveled out from the lower strain measurements, they are still rather large differences between the FEA and DIC results.

Table 11. Percent differences between the maximum principal strain in the FEA and DIC results along the center of the gage section.  $t = 3.4s$

| Max Principal Strain, $t = 3.4s$ |           |        |           |       |
|----------------------------------|-----------|--------|-----------|-------|
| FEA                              |           | DIC    |           |       |
| x(mm)                            | P1 Strain | x (mm) | P1 Strain | %diff |
| 0.22                             | 0.0616    | 0.20   | 0.0518    | 15.86 |
| 0.43                             | 0.0642    | 0.41   | 0.0549    | 14.49 |
| 0.65                             | 0.0650    | 0.63   | 0.0504    | 22.51 |
| 0.86                             | 0.0648    | 0.85   | 0.0516    | 20.36 |
| 1.08                             | 0.0642    | 1.07   | 0.0578    | 9.91  |
| 1.30                             | 0.0635    | 1.28   | 0.0618    | 2.68  |
| 1.51                             | 0.0629    | 1.50   | 0.0625    | 0.69  |
| 1.73                             | 0.0625    | 1.72   | 0.0569    | 8.88  |
| 1.94                             | 0.0623    | 1.94   | 0.0554    | 11.03 |
| 2.16                             | 0.0625    | 2.15   | 0.0540    | 13.49 |
| 2.37                             | 0.0628    | 2.37   | 0.0525    | 16.38 |
| 2.59                             | 0.0635    | 2.59   | 0.0532    | 16.23 |
| 2.81                             | 0.0642    | 2.80   | 0.0517    | 19.48 |
| 3.02                             | 0.0648    | 3.02   | 0.0463    | 28.54 |
| 3.24                             | 0.0649    | 3.24   | 0.0416    | 35.89 |
| 3.45                             | 0.0641    | 3.46   | 0.0436    | 32.03 |
| 3.67                             | 0.0615    | 3.67   | 0.0487    | 20.77 |

At 4 seconds into the test, the coupon is under a 0.032mm x, and 0.458 mm y displacement. Here, Aramis can now pick up and plot a developed strain field in the coupon as is seen below in Figure 54.

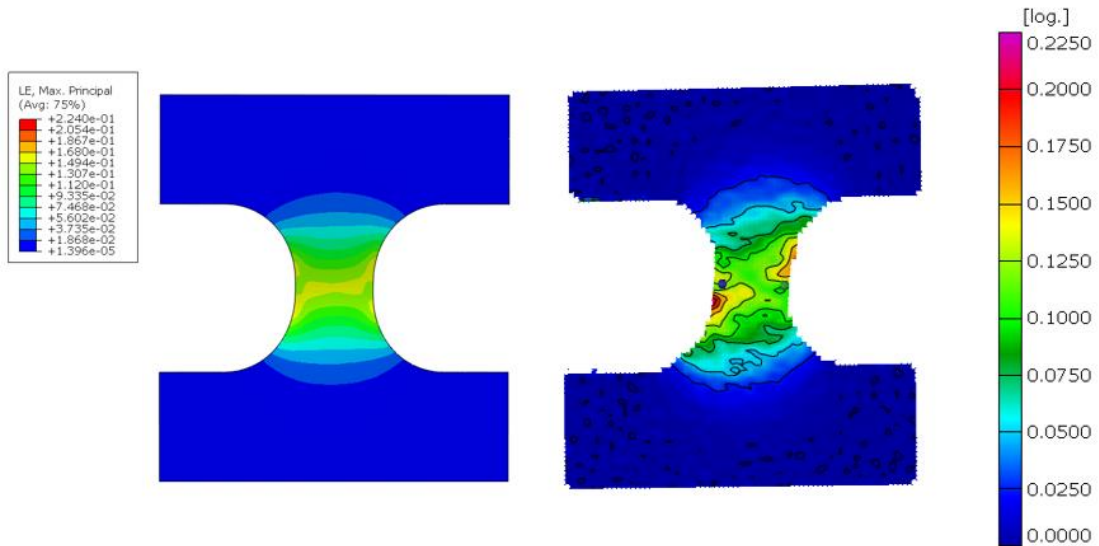


Figure 54. Comparison of strain fields at 4.0 seconds, coupon 4,  $\epsilon_{P1}$  (L: FEA, R: DIC)

This comparison is useful in pointing out the difference in the gradient shape, where both models are showing a slight asymmetry in the field about a y axis in the center of the gage section.

Moving to the cross-section plot, a direct comparison of the field again is used to highlight discrepancies. As the coupon transitions into the plastic region of the stress-strain curve, the lines do show the same shape, however at different magnitudes.

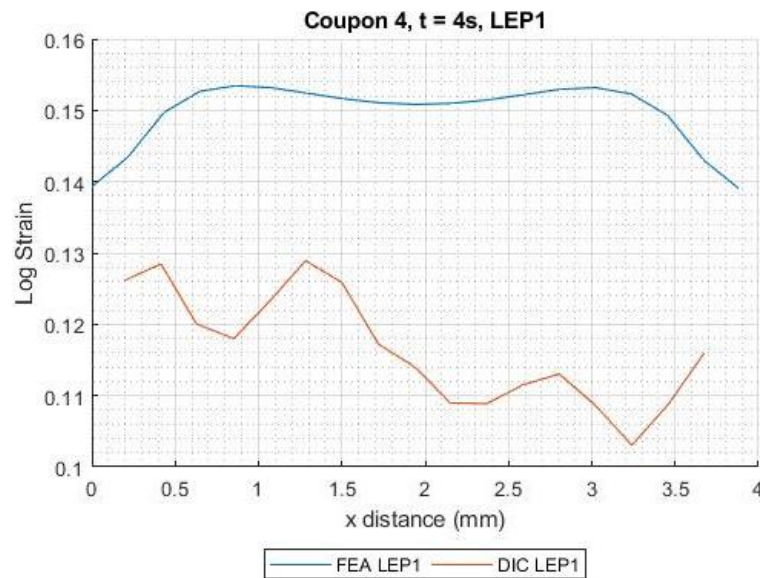


Figure 55. Cross sectional strain at the center of Coupon 4 at t=4s,  $\epsilon_{P1}$

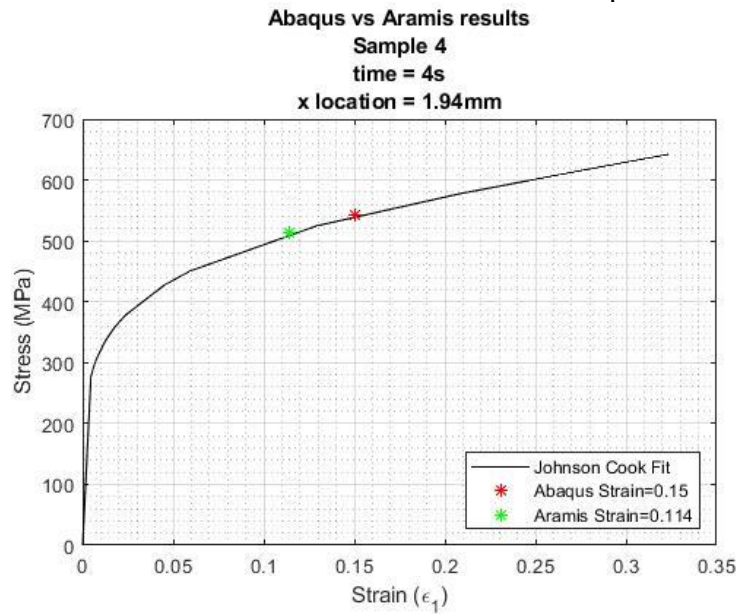


Figure 56. Plot relating  $\epsilon_{P1}$  from the FEA model and experimental to the Johnson Cook curve fit. At 4 seconds, 2mm into the gage section.

Looking at the percent difference between the experimental with the simulation shows similar results to the previous step at 3.4 seconds. At 4 seconds, the difference between strain values along the cross section range from 12% to 32%.

Table 12. Percent differences between the maximum principal strain in the FEA and DIC results along the center of the gage section.  $t=4s$ .

| Max Principal Strain, $t=4s$ |           |        |           |       |
|------------------------------|-----------|--------|-----------|-------|
| FEA                          |           | DIC    |           |       |
| x(mm)                        | P1 Strain | x (mm) | P1 Strain | %diff |
| 0.22                         | 0.1434    | 0.20   | 0.1262    | 12.03 |
| 0.43                         | 0.1497    | 0.41   | 0.1285    | 14.18 |
| 0.65                         | 0.1527    | 0.63   | 0.1200    | 21.37 |
| 0.86                         | 0.1535    | 0.85   | 0.1180    | 23.11 |
| 1.08                         | 0.1532    | 1.07   | 0.1233    | 19.50 |
| 1.30                         | 0.1524    | 1.28   | 0.1289    | 15.41 |
| 1.51                         | 0.1516    | 1.50   | 0.1259    | 16.99 |
| 1.73                         | 0.1511    | 1.72   | 0.1172    | 22.39 |
| 1.94                         | 0.1508    | 1.94   | 0.1141    | 24.38 |
| 2.16                         | 0.1510    | 2.15   | 0.1090    | 27.81 |
| 2.37                         | 0.1515    | 2.37   | 0.1089    | 28.13 |
| 2.59                         | 0.1522    | 2.59   | 0.1115    | 26.72 |
| 2.81                         | 0.1529    | 2.80   | 0.1130    | 26.10 |
| 3.02                         | 0.1532    | 3.02   | 0.1086    | 29.08 |
| 3.24                         | 0.1523    | 3.24   | 0.1030    | 32.35 |
| 3.45                         | 0.1493    | 3.46   | 0.1089    | 27.09 |
| 3.67                         | 0.1430    | 3.67   | 0.1160    | 18.90 |

At 4.8 seconds into the test, the material is well into its plastic deformation region. The FEA model is predicting 32% to 36% strains, where the DIC is measuring strains between 22% and 28%.

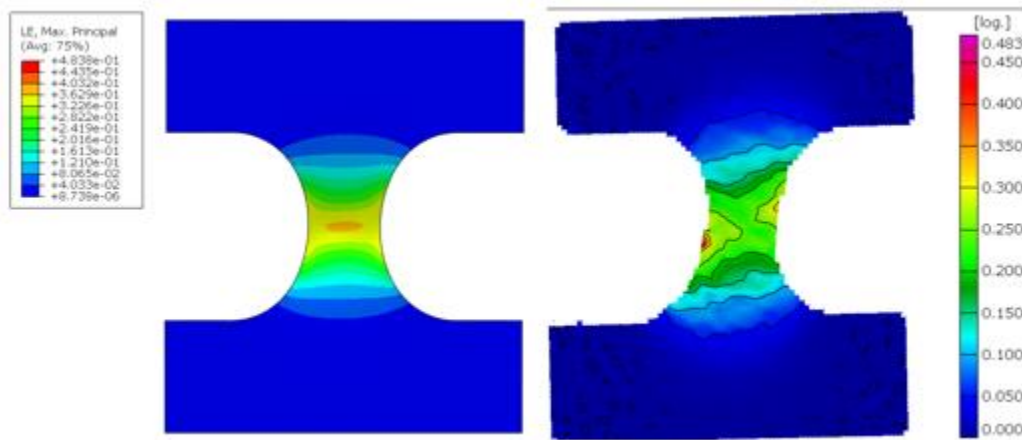


Figure 57. Comparison of strain fields at 4.8 seconds, coupon 4,  $\epsilon_{p1}$  (L: FEA, R: DIC)

Grip slip is noticeable here by inspection of the DIC image, however the Aramis software does remove the effects that rigid body displacement has on calculating strain in the gage section.

While these 2D surfaces seem to generally agree with each other, a comparison of the maximum principal strain highlights differences in the maximum principal strains between the experimental from the simulation is below in Figure 58.

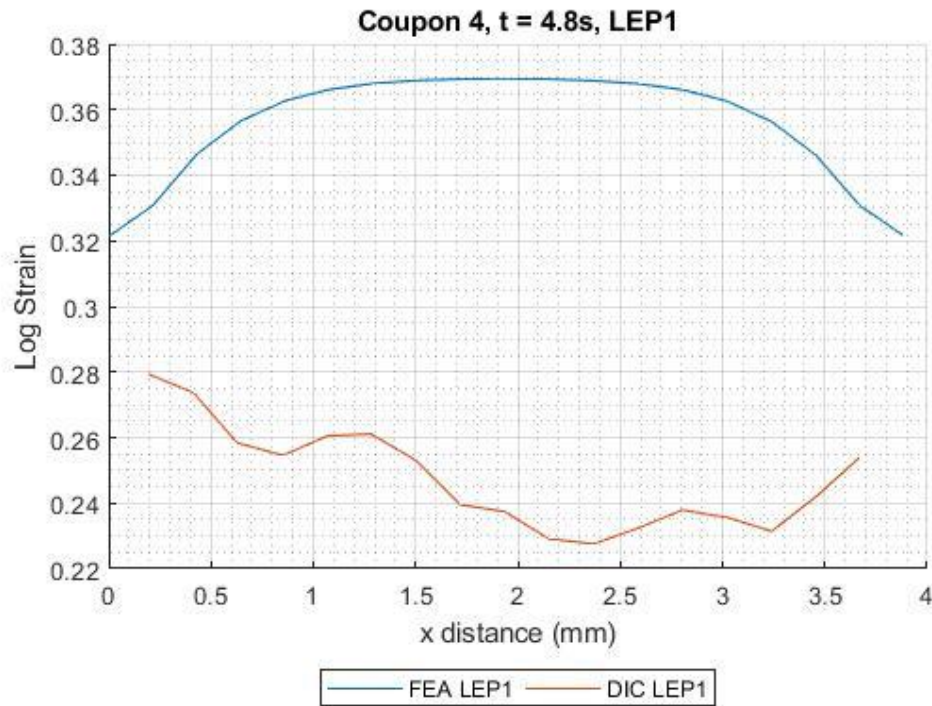


Figure 58. Cross sectional strain at the center of Coupon 4 at  $t=4.8s$ ,  $\epsilon_{p1}$ .

Again, this plot illustrates a cause for concern in the data, as not only are the values not in agreement, but there is a difference in the shape of the line with distance. Where the FEA model predicts higher strains at the center of the coupon when compared to the edges, the DIC results show lower values in the center, and higher at the top.

The strain values are plotted on the 304 stainless steel Johnson-Cook curve in Figure 59. While the curve was only plotted out to approximately 32% strain, the stress values are still below the ultimate strength, but the coupon is well into its plastic region.

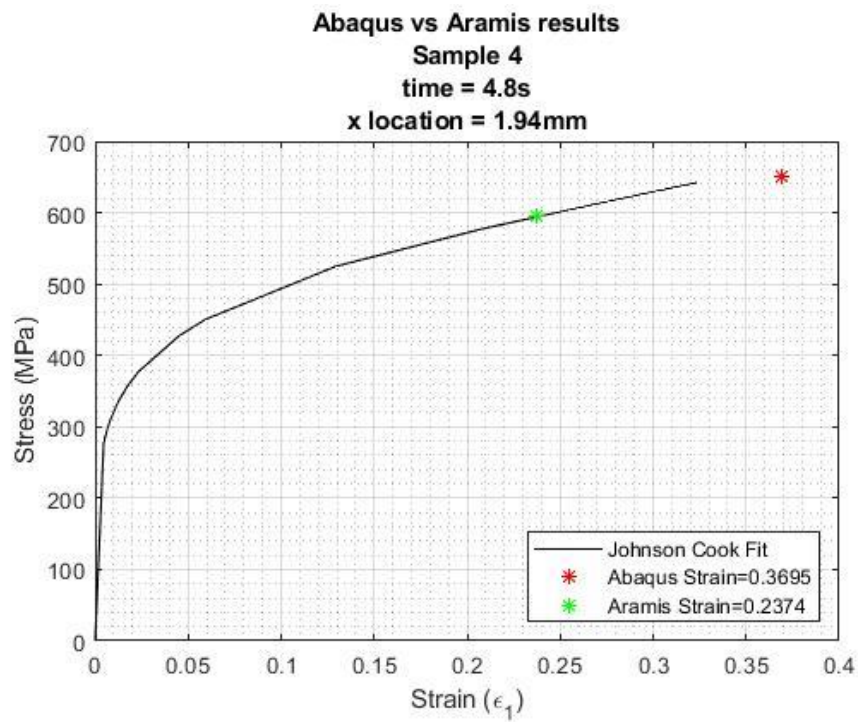


Figure 59. Plot relating  $\epsilon_{p1}$  from the FEA model and experimental to the Johnson Cook curve fit. At 4.8 seconds, appx. 2mm into the gage section.

Table 13. Percent differences between the maximum principal strain in the FEA and DIC results along the center of the gage section.  $t=4.8s$ .

| Max Principal Strain, $t=4.8s$ |           |        |           |       |
|--------------------------------|-----------|--------|-----------|-------|
| FEA                            |           | DIC    |           |       |
| x(mm)                          | P1 Strain | x (mm) | P1 Strain | %diff |
| 0.22                           | 0.3308    | 0.20   | 0.2793    | 15.56 |
| 0.43                           | 0.3465    | 0.41   | 0.2737    | 21.01 |
| 0.65                           | 0.3566    | 0.63   | 0.2584    | 27.55 |
| 0.86                           | 0.3627    | 0.85   | 0.2546    | 29.81 |
| 1.08                           | 0.3662    | 1.07   | 0.2605    | 28.85 |
| 1.30                           | 0.3680    | 1.28   | 0.2611    | 29.05 |
| 1.51                           | 0.3689    | 1.50   | 0.2531    | 31.40 |
| 1.73                           | 0.3693    | 1.72   | 0.2395    | 35.15 |
| 1.94                           | 0.3695    | 1.94   | 0.2374    | 35.73 |
| 2.16                           | 0.3693    | 2.15   | 0.2291    | 37.96 |
| 2.37                           | 0.3688    | 2.37   | 0.2276    | 38.29 |
| 2.59                           | 0.3679    | 2.59   | 0.2324    | 36.82 |
| 2.81                           | 0.3661    | 2.80   | 0.2379    | 35.01 |
| 3.02                           | 0.3626    | 3.02   | 0.2356    | 35.01 |
| 3.24                           | 0.3564    | 3.24   | 0.2315    | 35.05 |
| 3.45                           | 0.3462    | 3.46   | 0.2423    | 30.03 |
| 3.67                           | 0.3307    | 3.67   | 0.2542    | 23.15 |

Table 13 highlights even at the best case, the difference between the FEA model and the DIC data shows differences in strain values between 15% and 38% across the coupon. The data presented above illuminates the notion that for a simple quasi-tensile load path on the IPL, the method used does not to an accurate job of predicting the behavior in the plastic region.

To further explore the differences between the two methods, the conservation of volume during plastic deformation should enforce Equation 17.

$$\Delta V = \epsilon_{11} + \epsilon_{22} + \epsilon_{33} = 0 \quad (17)$$

Where the change in volume which is equal to the sum of the strains in the x, y, and z directions is equal to 0 in the portion of the material being deformed. Plots were created

for the time steps shown above, at 2, 3.4, 4, and 4.8 seconds. The volume is always conserved in the FEA model, plots were made for the DIC data as a check. Aramis was not used to collect strain in the z direction (into the page), however, it was deemed acceptable to say that  $\epsilon_{11}$  is equal to  $\epsilon_{33}$  in the reduced thickness section. For those reasons, Figure 60, Figure 61, and Figure 62 depict  $\epsilon_{22}$  against  $-2*(\epsilon_{11})$ .

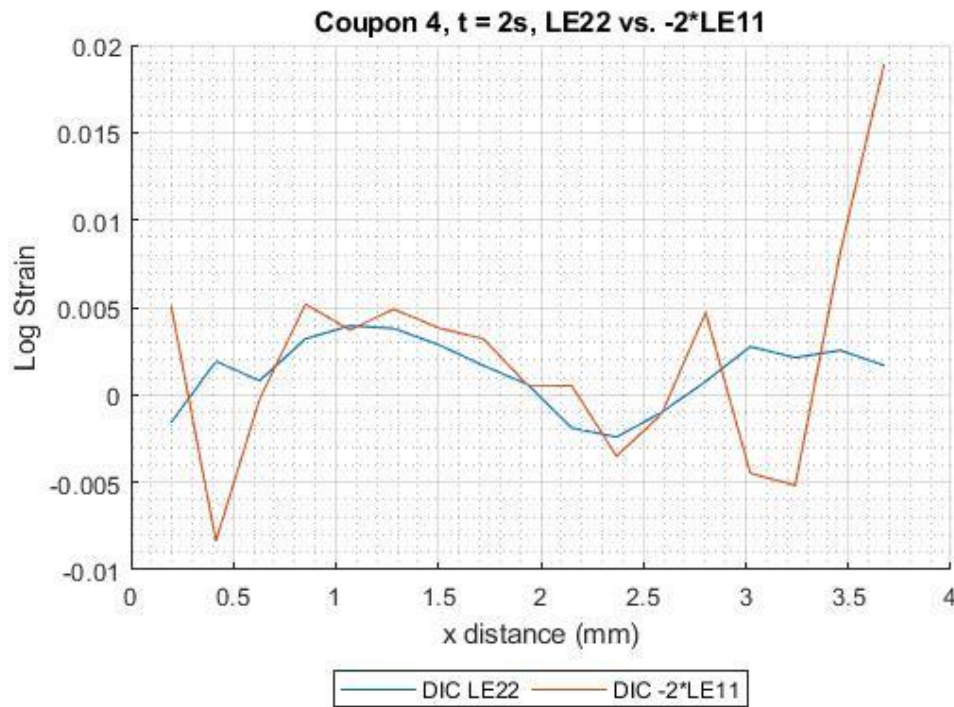


Figure 60. Plot comparing strain in the  $\epsilon_{22}$  direction against  $-2*(\epsilon_{11})$ .  $t = 2s$ .

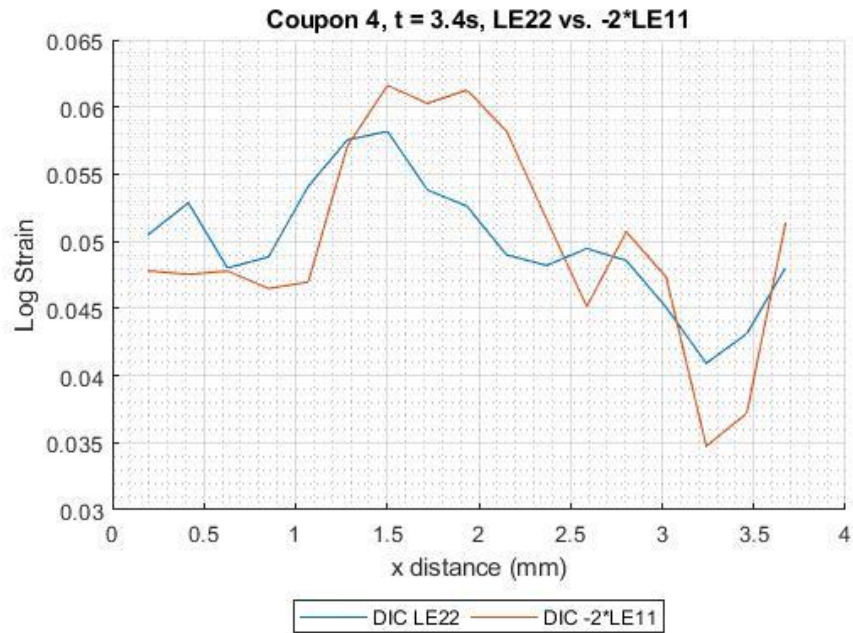


Figure 61. Plot comparing strain in the  $\epsilon_{22}$  direction against  $-2*(\epsilon_{11})$ .  $t = 3.4s$ .

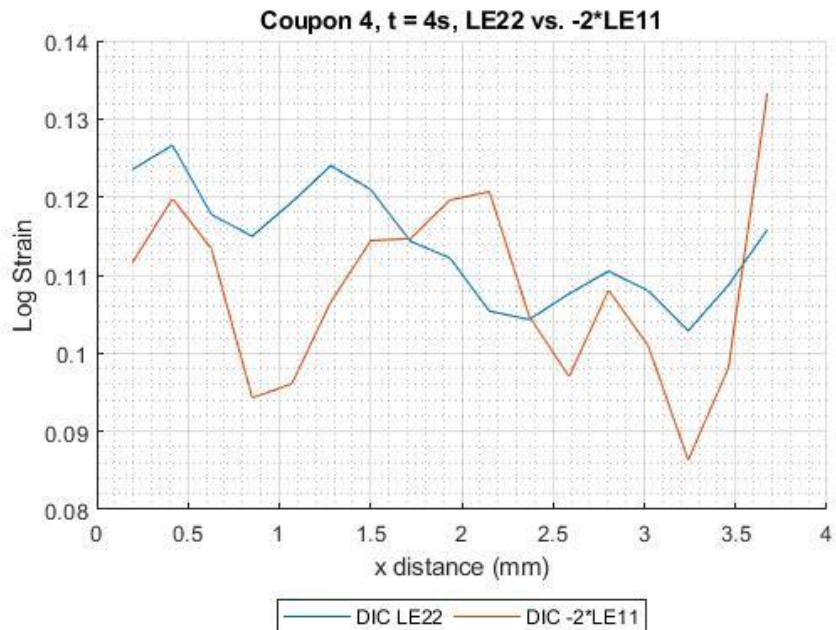


Figure 62. Plot comparing strain in the  $\epsilon_{22}$  direction against  $-2*(\epsilon_{11})$ .  $t = 4.0s$ .

Figure 60, Figure 61, Figure 62, and Figure 63 show general agreement between the two data sets values, percent errors in all three plots are in the 10-25% range. This appears to be due to the irregular peaks in valleys between points in the DIC data. FEA results for the same plots show an ideal case where the strains are almost exactly equal as Equation 17 would dictate.

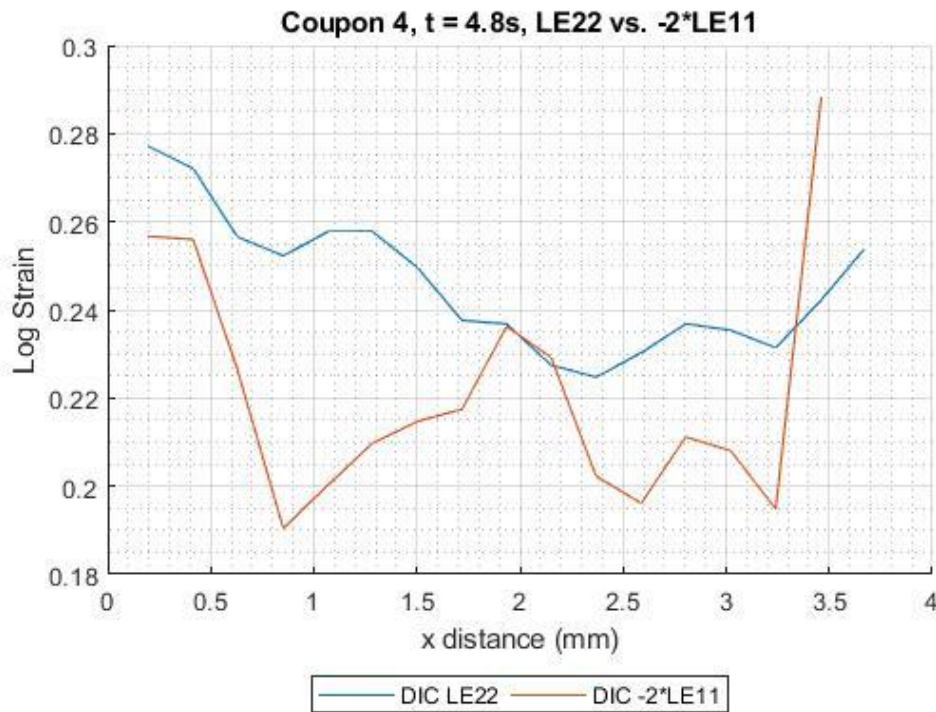


Figure 63. Plot comparing strain in the  $\epsilon_{22}$  direction against  $-2*(\epsilon_{11})$ .  $t = 4.8s$ .

### Coupon 3- Multiaxial Case

Coupon 3 was examined as it acts as a true multiaxial load with input displacements of 0 mm x and 0 mm y, and a counter clockwise rotation of 10 degrees. While not given multiaxial inputs, to be able to rotate the IPL actuators jog the coupon in x and y during the rotation motion. The results here are shown for  $\epsilon_{p1}$ . The following points were collected at times 2.4s, 3.0s, and 15.8s. As the previous test showed that there is noise in the DIC data

when in the linear elastic region, these time steps were chosen as they represent increasing plastic strain in the gage section.

At 2.4 seconds, the coupon is depicted in Figure 64 is starting to show a defined strain field. A red flag in this figure shows the stress concentrations on opposite sides of the gage section. This is most likely due to tabular input of displacements at every 0.2 seconds into the Abaqus displacement boundary conditions, as this method can sometimes cause the coupon to jump in displacement between frames. At this time the coupon is under an x displacement of -0.029 mm and a y displacement of 0.056 mm, the top surface of the coupon is rotated -0.336 degrees from the horizontal bottom edge.

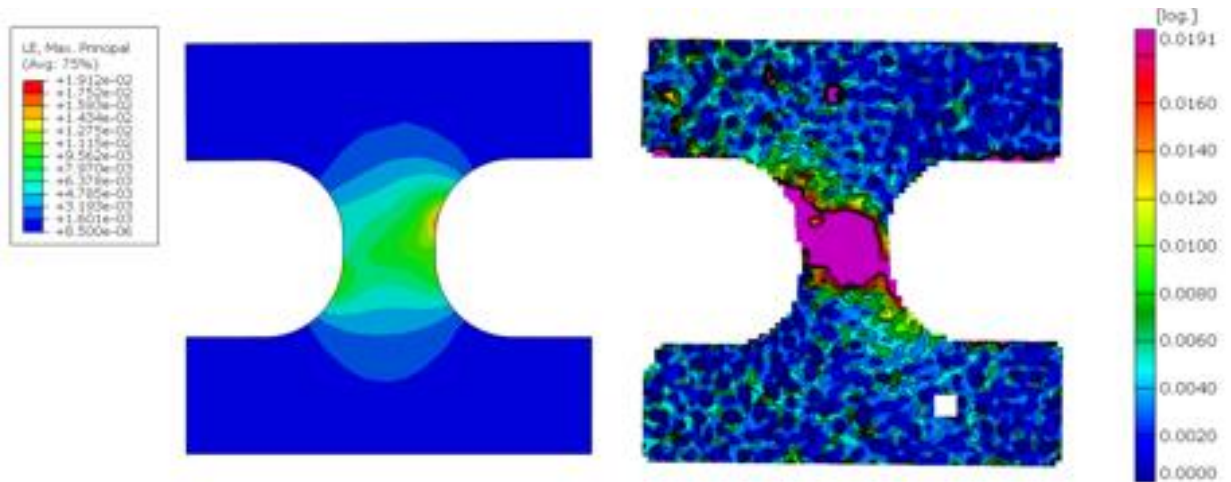


Figure 64. Comparison of strain fields at 2.4 seconds, coupon 3,  $\epsilon_{P1}$  (L: FEA, R: DIC)

Moving to a comparison of the strains in Figure 65, the cross section across the center of the gage section in the x direction, provides a visualization of the large differences between the FEA and DIC results for a multiaxial load.

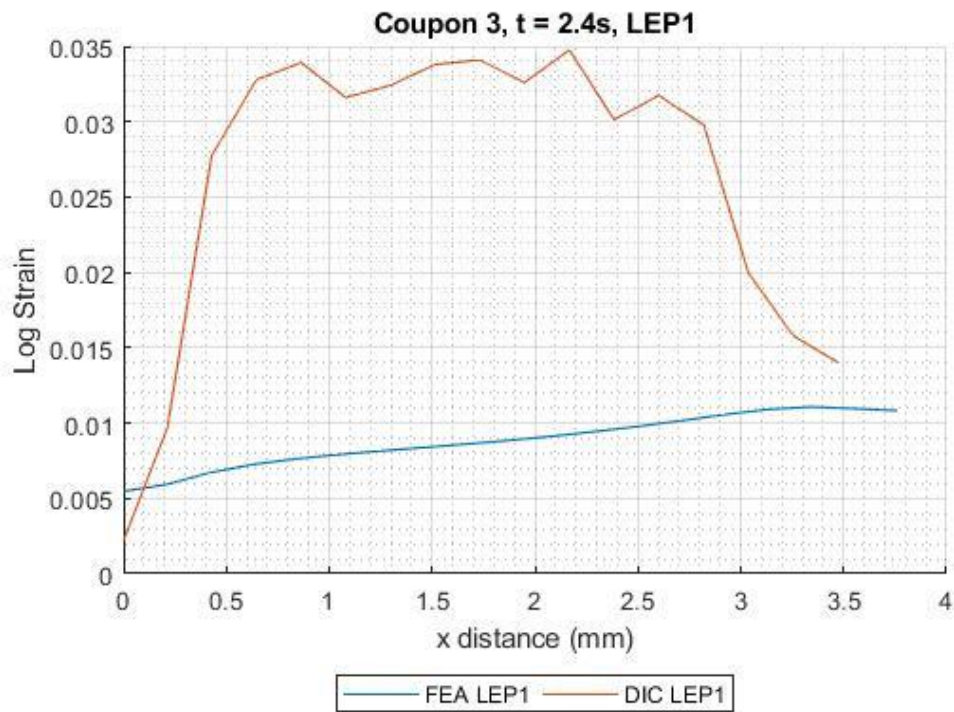


Figure 65. Cross sectional strain at the center of coupon 3, at  $t = 2.6\text{s}$ ,  $\epsilon_{p1}$

Figure 66 is used to plot  $\epsilon_{P1}$  for both the FEA and the DIC measurements, in the center of the gage section. At 2.6 seconds into the test, the material is transitioning from its elastic to plastic deformation region, both the simulation and the experimental results show at that point the material is undergoing plastic deformation.

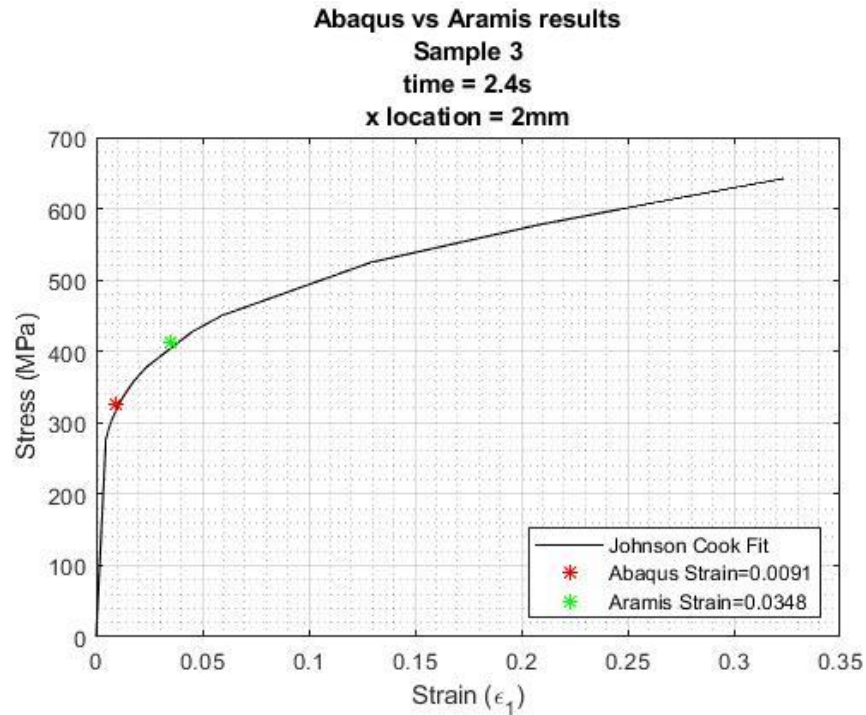


Figure 66. Plot relating  $\epsilon_{P1}$  from the FEA model and experimental to the Johnson Cook curve fit. At 2.4 seconds, in the center of the gage section.

When looking at percent differences across this gage section in Table 14, values range from 27% to over 350%, where the FEA is predicting far lower principal strains in the coupon than the DIC is measuring.

Table 14. Percent differences between the maximum principal strain in the FEA and DIC results along the center of the gage section.  $t=4.8s$ .

| Max Principal Strain, $t = 2.4s$ |           |        |           |         |
|----------------------------------|-----------|--------|-----------|---------|
| FEA                              |           | DIC    |           | %diff   |
| x(mm)                            | P1 Strain | x (mm) | P1 Strain |         |
| 0.00                             | 0.0055    | 0.00   | 0.0022    | 60.18   |
| 0.21                             | 0.0059    | 0.21   | 0.0097    | -63.25  |
| 0.42                             | 0.0067    | 0.43   | 0.0277    | -313.60 |
| 0.63                             | 0.0072    | 0.65   | 0.0328    | -352.29 |
| 0.84                             | 0.0076    | 0.86   | 0.0339    | -344.96 |
| 1.04                             | 0.0079    | 1.08   | 0.0316    | -299.39 |
| 1.25                             | 0.0082    | 1.30   | 0.0324    | -297.43 |
| 1.46                             | 0.0084    | 1.51   | 0.0338    | -303.25 |
| 1.67                             | 0.0086    | 1.73   | 0.0341    | -296.09 |
| 1.88                             | 0.0089    | 1.95   | 0.0326    | -267.95 |
| 2.09                             | 0.0091    | 2.17   | 0.0348    | -280.54 |
| 2.30                             | 0.0094    | 2.38   | 0.0301    | -219.08 |
| 2.51                             | 0.0098    | 2.49   | 0.0309    | -215.57 |
| 2.71                             | 0.0102    | 2.82   | 0.0298    | -192.87 |
| 3.13                             | 0.0109    | 3.04   | 0.0200    | -82.99  |
| 3.34                             | 0.0111    | 3.26   | 0.0158    | -42.65  |
| 3.55                             | 0.0110    | 3.48   | 0.0140    | -27.73  |

At a time of 5 seconds, the displacement of the coupons top edge is -0.0047 mm in the x and 0.098 mm in the y. The rotation of the top edge with respect to the bottom edge is 0.382 degrees. The 2D surface generated by both shown at the same scale indicates that both models are showing the same general shape of the strain field, however there is a difference in the scale of the computed strains. Asymmetric pockets of strain are measured near the corners of the gage section.

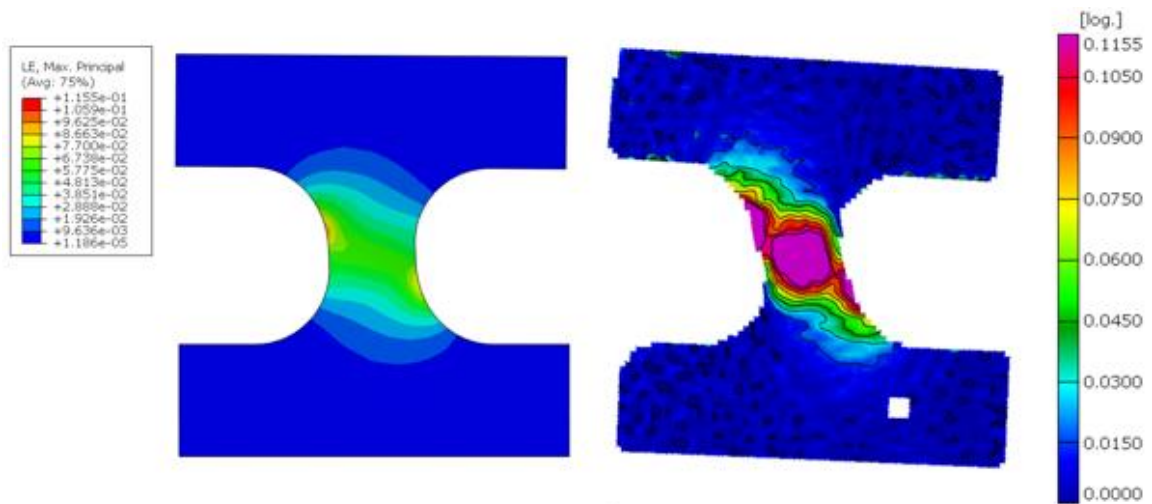


Figure 67. Comparison of strain fields at 5 seconds, coupon 3,  $\epsilon_{p1}$  (L: FEA, R: DIC)

In Figure 68 the cross-sectional comparison of FEA and DIC shows results that show an extremely large difference in strain data at this step. While both plots show a parabolic arc with minimum values at the edges, the magnitude of the strain is much larger in the Aramis measurements than in the FEA results.

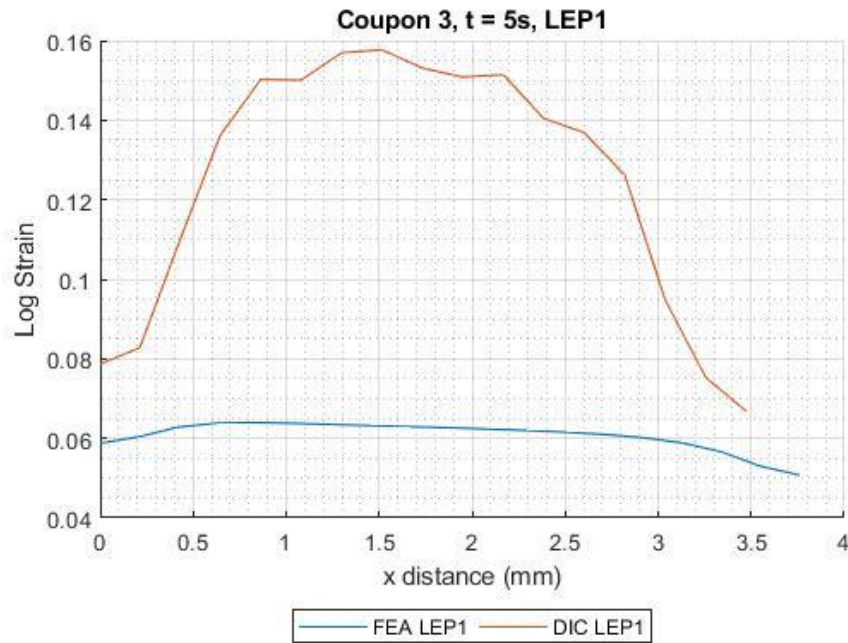


Figure 68. Cross sectional strain at the center of sample 3 at  $t=5.0$  s,  $\epsilon_{P1}$

The difference in strain on the surface at the midpoint of the gage section is again used to illustrate the state of strain in the coupon, related to the uniaxial tensile test. Figure 69 shows the degree of plastic deformation predicted by the FEA and DIC results.

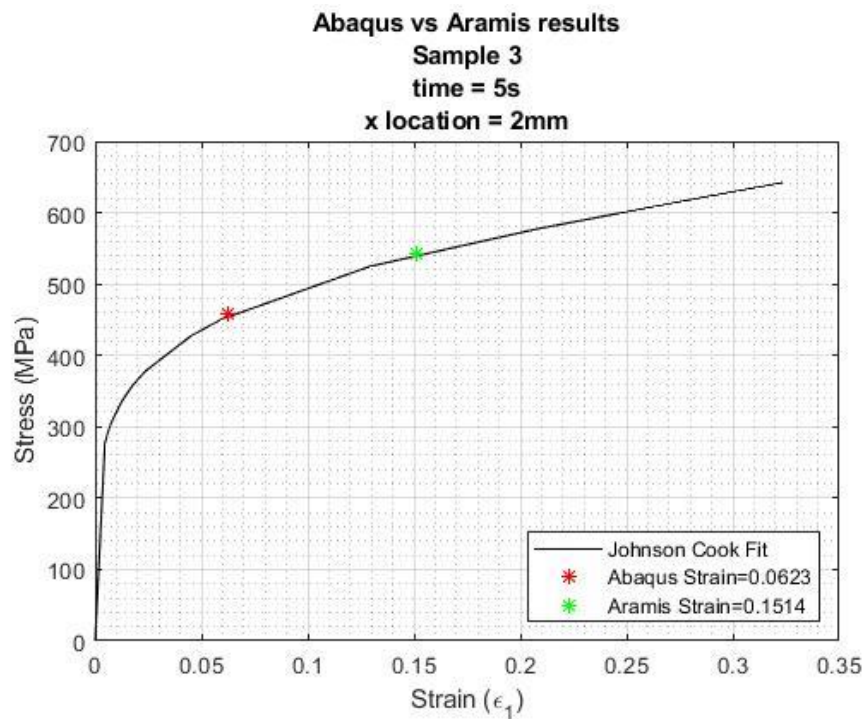


Figure 69. Plot relating  $\epsilon_{p1}$  from the FEA model and experimental to the Johnson Cook curve fit. At 5 seconds, 2 mm into the gage section.

Again, in Table 15 when the percent differences of points in the cross section are analyzed, the drastic difference in values indicates that there may be something amiss in either one of the datasets. Percent differences at this time step range from 26% to 150%.

Table 15. Percent differences between the maximum principal strain in the FEA and DIC results along the center of the gage section.  $t=5.0s$ .

| Max Principal Strain, $t = 5s$ |           |        |           |         |
|--------------------------------|-----------|--------|-----------|---------|
| FEA                            |           | DIC    |           | %diff   |
| x(mm)                          | P1 Strain | x (mm) | P1 Strain |         |
| 0.00                           | 0.0588    | 0.00   | 0.0787    | -33.92  |
| 0.21                           | 0.0604    | 0.21   | 0.0828    | -37.07  |
| 0.42                           | 0.0628    | 0.43   | 0.1098    | -74.74  |
| 0.63                           | 0.0638    | 0.65   | 0.1362    | -113.41 |
| 0.84                           | 0.0640    | 0.86   | 0.1502    | -134.87 |
| 1.04                           | 0.0638    | 1.08   | 0.1501    | -135.36 |
| 1.25                           | 0.0635    | 1.30   | 0.1569    | -147.22 |
| 1.46                           | 0.0632    | 1.51   | 0.1577    | -149.51 |
| 1.67                           | 0.0629    | 1.73   | 0.1531    | -143.33 |
| 1.88                           | 0.0626    | 1.95   | 0.1508    | -140.78 |
| 2.09                           | 0.0623    | 2.17   | 0.1514    | -142.89 |
| 2.30                           | 0.0620    | 2.38   | 0.1405    | -126.63 |
| 2.51                           | 0.0615    | 2.49   | 0.1388    | -125.49 |
| 2.71                           | 0.0610    | 2.82   | 0.1262    | -106.93 |
| 3.13                           | 0.0588    | 3.04   | 0.0949    | -61.29  |
| 3.34                           | 0.0566    | 3.26   | 0.0753    | -33.14  |
| 3.55                           | 0.0530    | 3.48   | 0.0668    | -26.01  |

At a time of 15.8 seconds the models continue to show a similar shape, again the scaling between the two models in Figure 70 is a concern. At this point in the experiment, the sample is displaced -0.530 mm in the x, 0.494 mm in the y, and has rotated 5 degrees from horizontal.

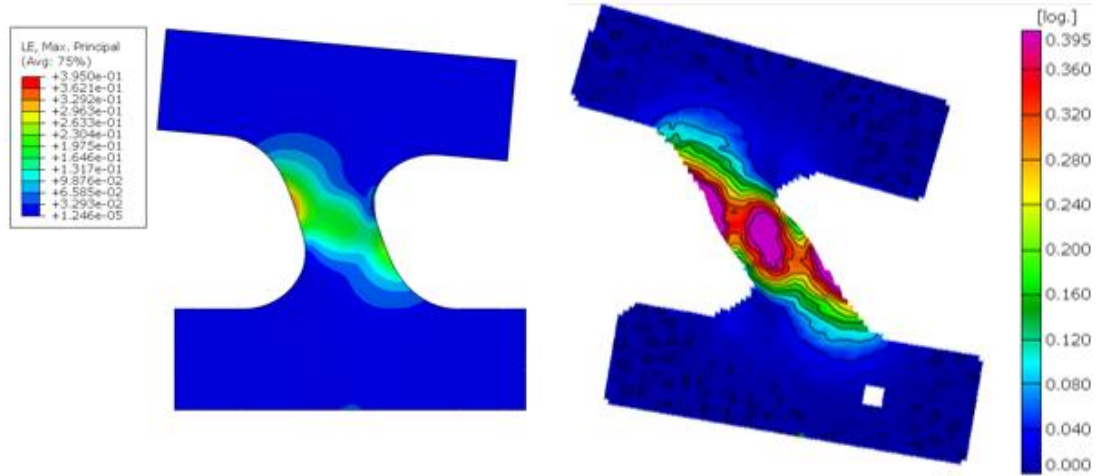


Figure 70. Comparison of strain fields at 4.8 seconds, coupon 7,  $\epsilon_{12}$  (L: FEA, R: DIC)

The growth in the difference between the experimental and FEA prediction is further highlighted when viewed as a function of strain in the principal direction across the center of the gage section. Also visible in the Aramis “3D View” is a severe about slipping of the coupon within the grips. As has been seen at the previous two time steps. The DIC measurements are reading far more strain than the FEA simulation

The strain plotted in the 304 stainless Johnson Cook equation is shown in Figure 73. into the gage section show that under plastic deformation the difference between stress in the FEA model and stress calculated from DIC values continues to grow.

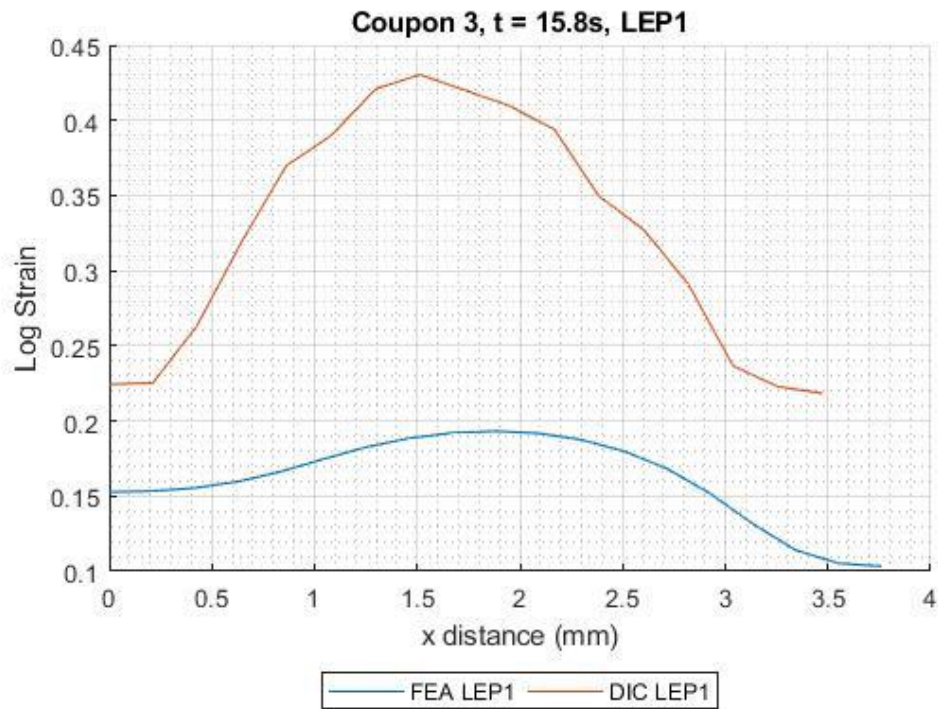


Figure 71. Figure 72. Cross sectional strain at the center of sample 3 at t=15.8 s,  $\epsilon_{P1}$

Figure 73 further illustrates the differences in the readings, at a point in the center of the coupon. The Aramis value is approaching 40% strain, where Abaqus is predicting 19%

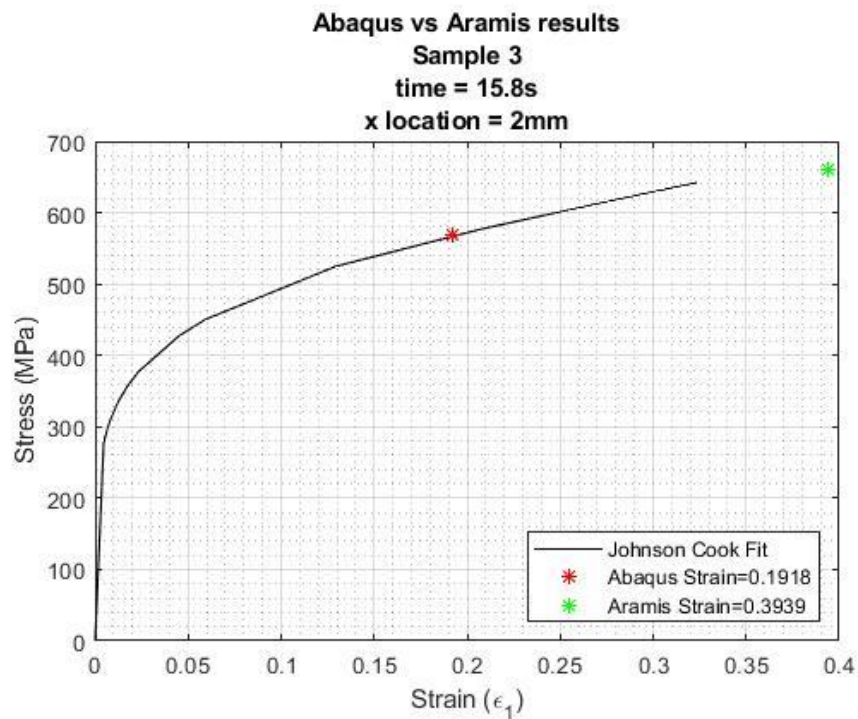


Figure 73. Plot relating  $\epsilon_{p1}$  from the FEA model and experimental to the Johnson Cook curve fit. At 5 seconds, 2 mm into the gage section

Again, the percent differences between the max principal strain values for this multiaxial test are found below in Table 16. As was seen in the two previous time steps, the FEA simulation is predicting smaller strains than the DIC experimental results. The differences range from 46% to over 130% across the surface at the center of the gage section.

Table 16. Percent differences between the maximum principal strain in the FEA and DIC results along the center of the gage section.  $t = 15.8s$ .

| Max Principal Strain, $t = 15.8$ |           |        |           |         |
|----------------------------------|-----------|--------|-----------|---------|
| FEA                              |           | DIC    |           | %diff   |
| x(mm)                            | P1 Strain | x (mm) | P1 Strain |         |
| 0.00                             | 0.1528    | 0.00   | 0.2245    | -46.96  |
| 0.21                             | 0.1533    | 0.21   | 0.2253    | -46.98  |
| 0.42                             | 0.1554    | 0.43   | 0.2635    | -69.55  |
| 0.63                             | 0.1597    | 0.65   | 0.3194    | -100.01 |
| 0.84                             | 0.1663    | 0.86   | 0.3700    | -122.53 |
| 1.04                             | 0.1747    | 1.08   | 0.3897    | -123.08 |
| 1.25                             | 0.1827    | 1.30   | 0.4210    | -130.48 |
| 1.46                             | 0.1885    | 1.51   | 0.4304    | -128.31 |
| 1.67                             | 0.1921    | 1.73   | 0.4199    | -118.65 |
| 1.88                             | 0.1933    | 1.95   | 0.4097    | -111.99 |
| 2.09                             | 0.1918    | 2.17   | 0.3939    | -105.36 |
| 2.30                             | 0.1876    | 2.38   | 0.3496    | -86.38  |
| 2.51                             | 0.1799    | 2.49   | 0.3390    | -88.42  |
| 2.71                             | 0.1683    | 2.82   | 0.2908    | -72.76  |
| 3.13                             | 0.1317    | 3.04   | 0.2368    | -79.77  |
| 3.34                             | 0.1142    | 3.26   | 0.2228    | -95.21  |
| 3.55                             | 0.1053    | 3.48   | 0.2184    | -107.41 |

While these results only present a few time steps of two experiments conducted for this work, this method can be repeated for any sample at any time-step. While the method of distilling the FEA and DIC data into forms which can be compared with one another is a very involved process, strain data can be collected at any facet in an Aramis file, and at any node in the FEA model.

Recalling Equation 17 to check the whether or not the Aramis system is measuring a 0 change in volume, Figures 73, 74, and 75 contain plots measuring the strain in the y direction vs strain in the transverse direction.

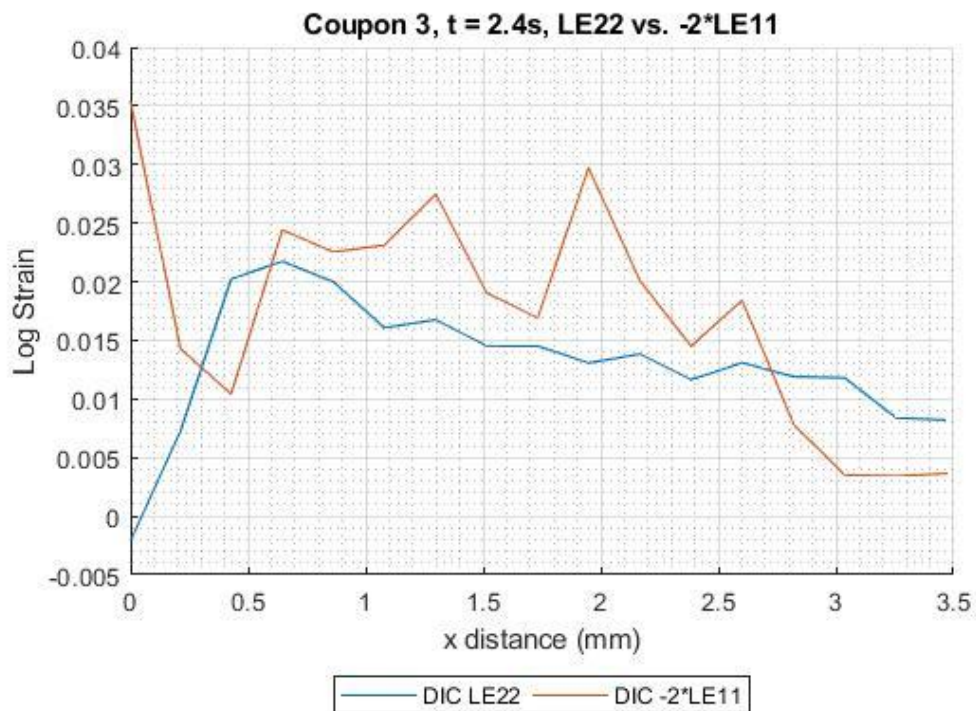


Figure 74. Plot comparing strain in the  $\epsilon_{22}$  direction against  $-2*(\epsilon_{11})$ .  $t = 2.4s$ .

The plots again indicate that volume conservation is not being measured by the DIC, and there appears to be some noise in the data collected.

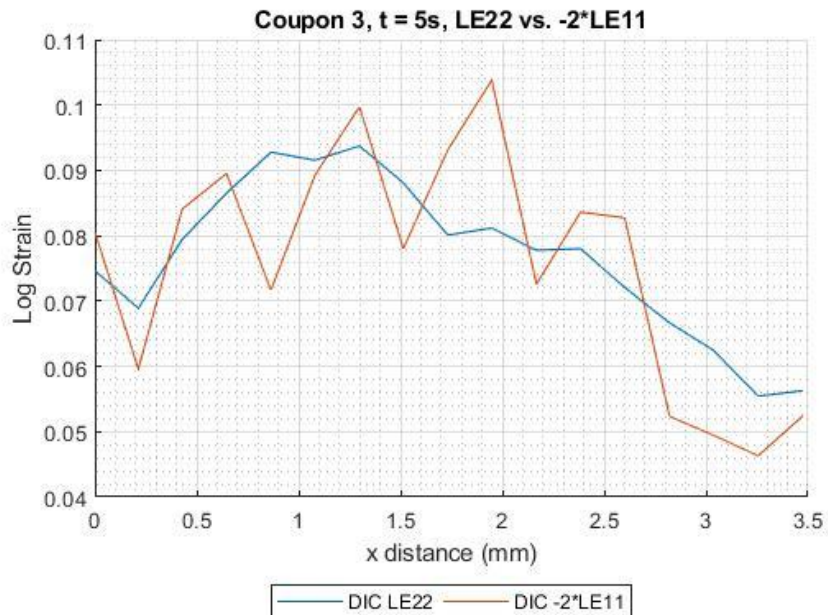


Figure 75. Plot comparing strain in the  $\epsilon_{22}$  direction against  $-2*(\epsilon_{11})$ .  $t = 5s$ .



Figure 76. Plot comparing strain in the  $\epsilon_{22}$  direction against  $-2*(\epsilon_{11})$ .  $t = 15.8s$ .

At 2.4 seconds in Figure 74. Plot comparing strain in the  $\epsilon_{22}$  direction against  $-2*(\epsilon_{11})$ .  $t = 2.4s$ . a pattern is starting to develop between the strain in the y and the transverse strain, but there is noise in the signal. In Figure 75, at 5 seconds there appears to be a general agreement between the two, however there is still a large variation in strain values in the transverse points. Finally, Figure 76 the values drift further apart and no clear pattern can be seen between the two sets of data.

Appendix B contains slides comparing Aramis and FEA data side by side for select time steps for the tests listed in Table 9. Data for all other time steps in 0.2 increments for the tests listed above can be pulled from the Aramis and FEA files.

## CONCLUSIONS

The comparison between the simulations and experimental data presented in the previous section work to demonstrate that there are still unknown causes to the disagreement between the FEA simulation results and the experimental data collected by the Aramis DIC system.

With the initial focus of characterizing strain rate sensitivity effects being an unobtainable goal as shown by the FEA simulations at the IPL's testing speeds, it was found early on in through experimenting with testing methodology that strain rate sensitivity could not be explored on the IPL with 304 stainless steel at this time.

In the quasi-tensile test, for stainless steels experiencing 5% to 30% strains, the percent errors between the FEA model were within 25% to 30% of the experimental results. The failure to reproduce the elastic region of a quasi-tensile test was an unexpected outcome, as the FEA model was able to reproduce static tensile tests accurately. This indicates that there may be errors involved in the collection of the DIC data. Whether this is in calibration of the cameras, resolution in the elastic region, or the method by which the data was collected, or a byproduct of postprocessing is not yet known at this point.

While the methods and models used require further optimization to reduce the differences measured between the FEA and DIC results, it is worth noting that the methods developed in the previous section are a suitable means of presenting multiaxial strain data of an asymmetric strain field on the surface of a coupon experiencing high levels of plastic deformation.

As the IPL has only been used by NRL and MSU to test composites, there is no published data for metals testing on an In-Plane Loader. With the work outlined in the sections above methods now exist and can be improved upon for future materials testing using the IPL.

### Future Work and Recommendations

From the results presented it was determined strain rate sensitivity could not be explored using the IPL due to a variety of limiting factors. For the IPL load frame itself, the recommendations for a machine that can place a metal coupon in a high strain rate multi-axial test are:

- Redesign the frame with load cells, actuators, and LDVT's in a closed loop design, with measurements being taken closer to the grips.
- Redesign the IPL grips to:
  - take a wider variety of coupon geometries which allow for strain gages and extensometer placement
  - eliminate the issues the grip slipping.
  - Allow for larger gage sections and a larger DIC image area
  - Employ self-centering wedge grips that keep the coupon centered in the X-Y plane of the loader.
- Use screw actuators that allow for backlash prevention, have a higher maximum load output, and ideally are hydraulically operated.

Another cause for concern, is that the IPL does resolve forces in the X, Y, and a moment about Z for each test. During testing of stainless steel coupons, moments as high

as 15,000 in-lbf were reported by the machine. These are unrealistically high for the material and geometry being tested. An example of this is seen below for coupon 5, at 5 seconds into the test the IPL reports a moment about the Z axis of 9641 in-lbf.

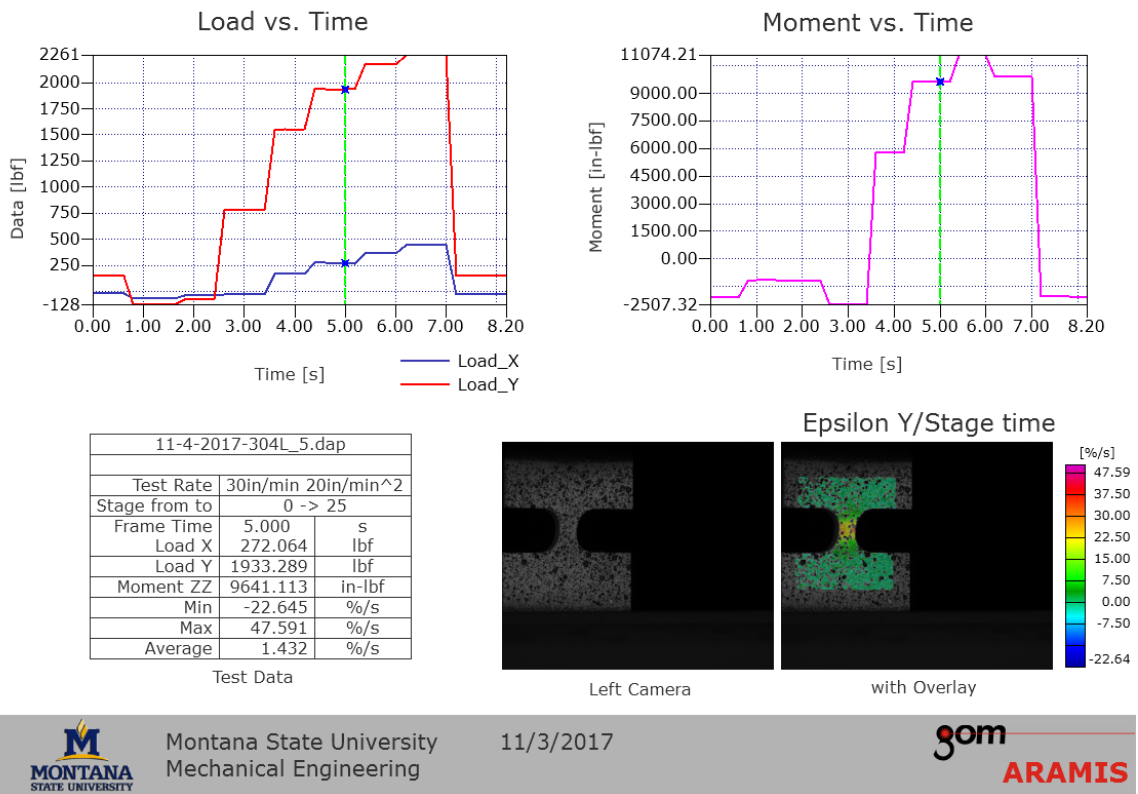


Figure 77. IPL stage report generated by Aramis for sample 5, 5s into the test. Note moment ZZ.

As the FEA model was proved accurate in tensile testing, the discrepancy between DIC and FEA results is most likely lies in the calibration or data collection methods used in Aramis DIC. To remedy this, the next recommended steps are

- Repeat the experiments using a high-speed camera with a sampling rate higher than 5 fps.

- Run tensile testing using Aramis DIC and compare against an FEA model, along with extensometer and strain gage readings.
- Verify with GOM that the Aramis DIC calibration is being performed correctly
- Explore smoothing and filtering of DIC results.
- Experiment with facet sizing and the effect it has on producing an accurate strain field. The method used here was adapted from a quasi-static testing procedure and adjusted to produce useable images.

Currently, work is being done to explore the issues listed above, starting by working to solve the erroneous moment being measured by the system. With the above lists, the FEA model, and comparison methods provided in this work the IPL will be a useful tool in characterizing high-strain rate behavior of plastics and metals. The methods described, with the recommendations made, should improve the IPL's usefulness especially when paired with Zerilli Armstrong and MTS Abaqus UHARD subroutines for verification.

## REFERENCES CITED

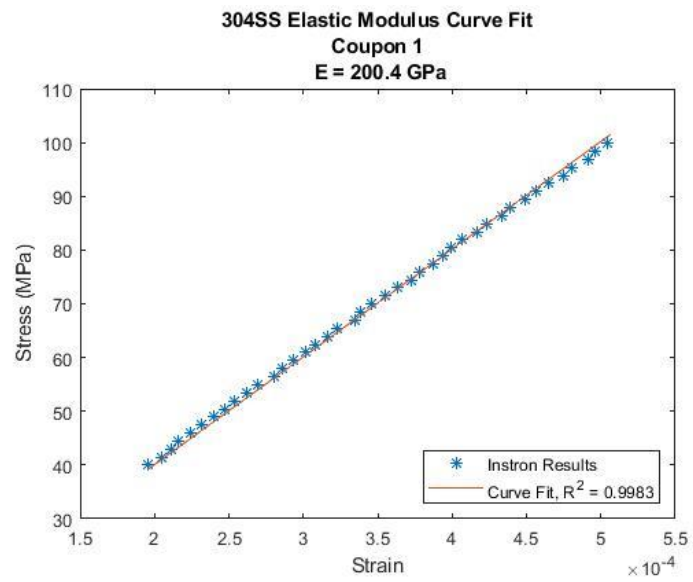
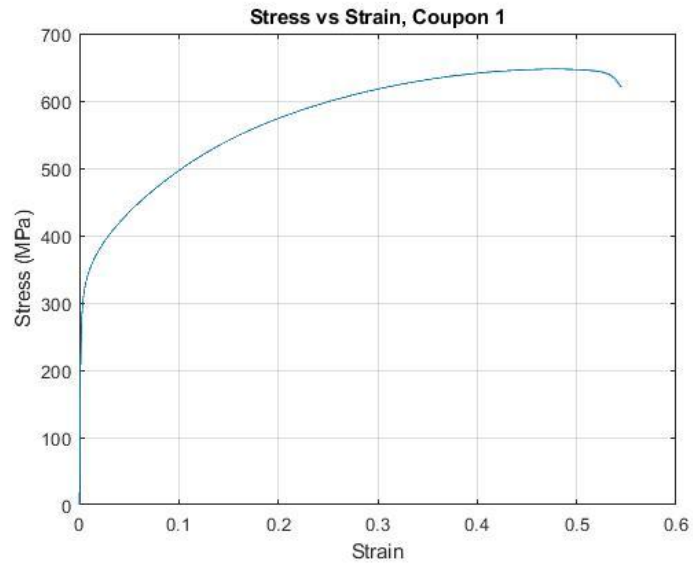
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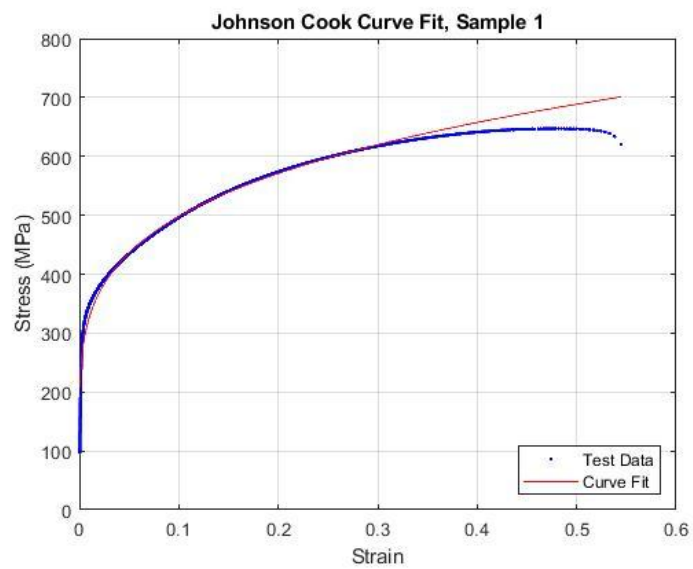
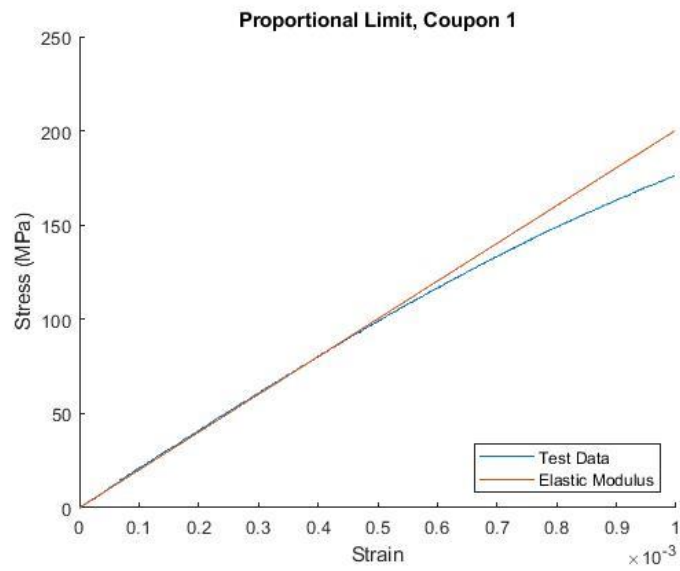
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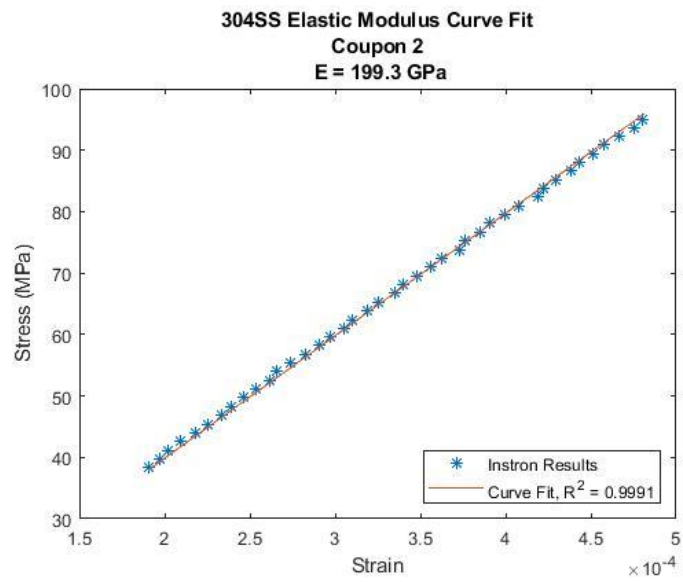
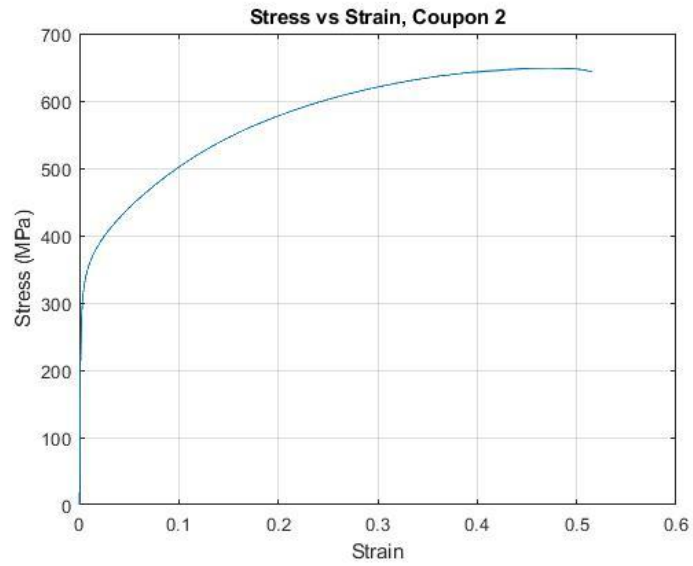
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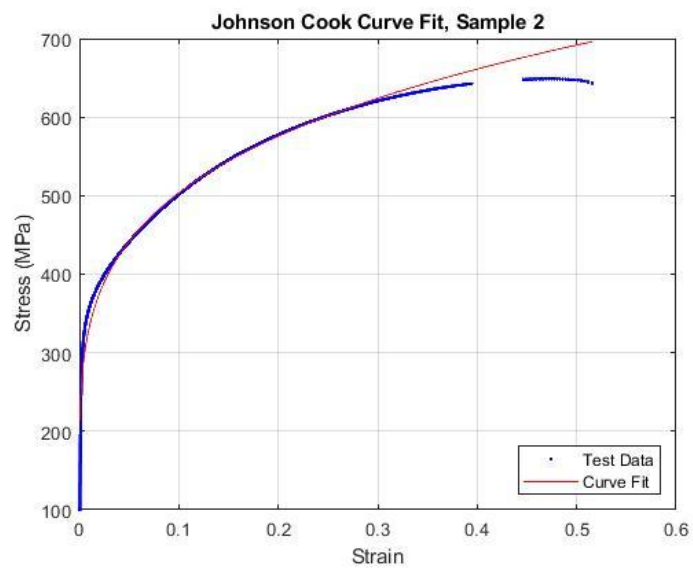
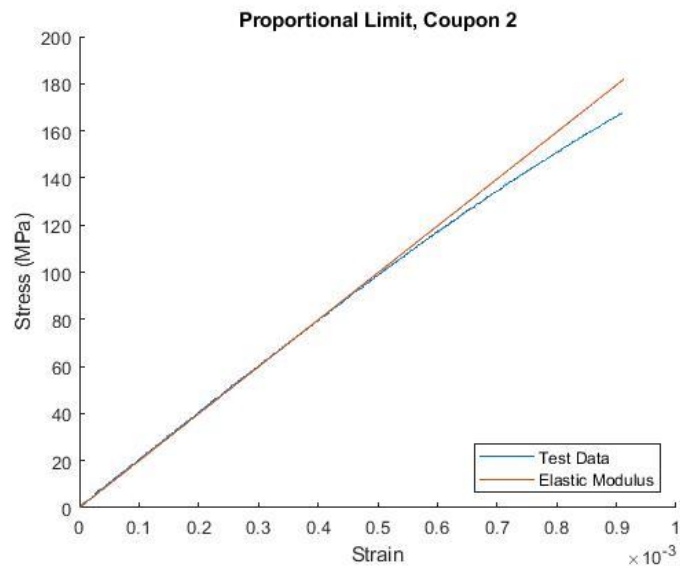
## APPENDICES

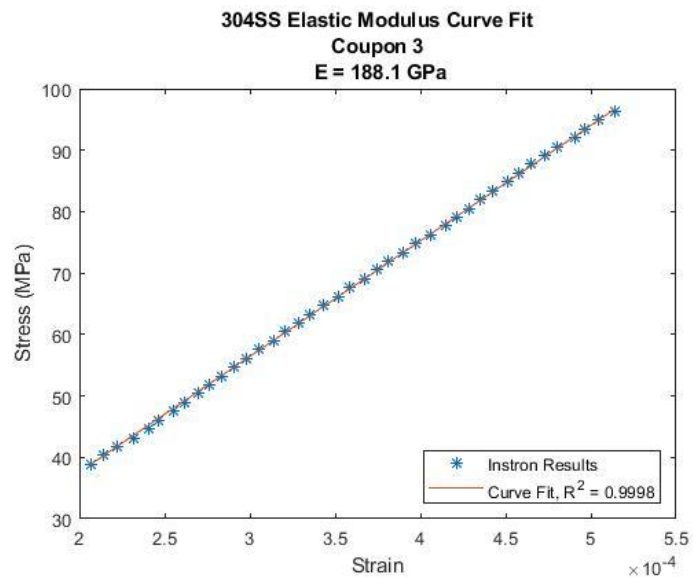
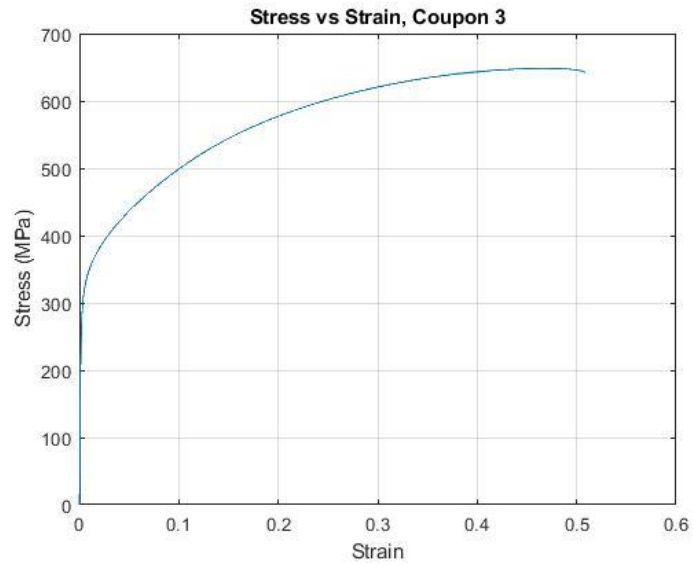
## APPENDIX A: MATLAB CURVE FITTING OF TENSILE DATA

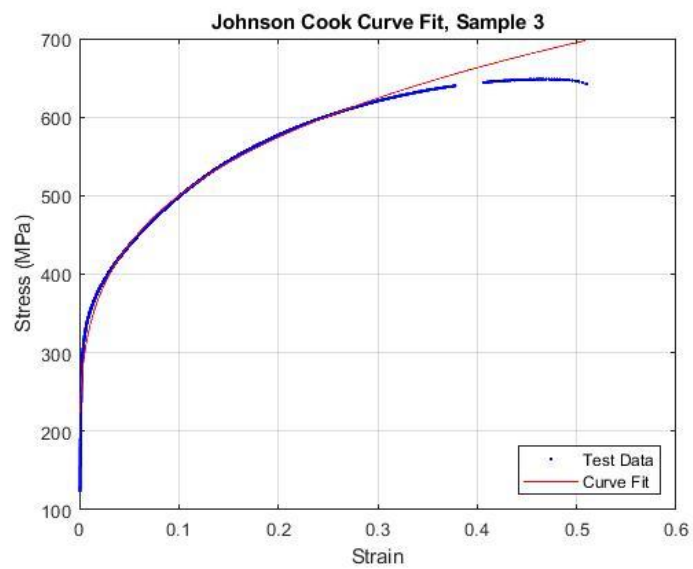
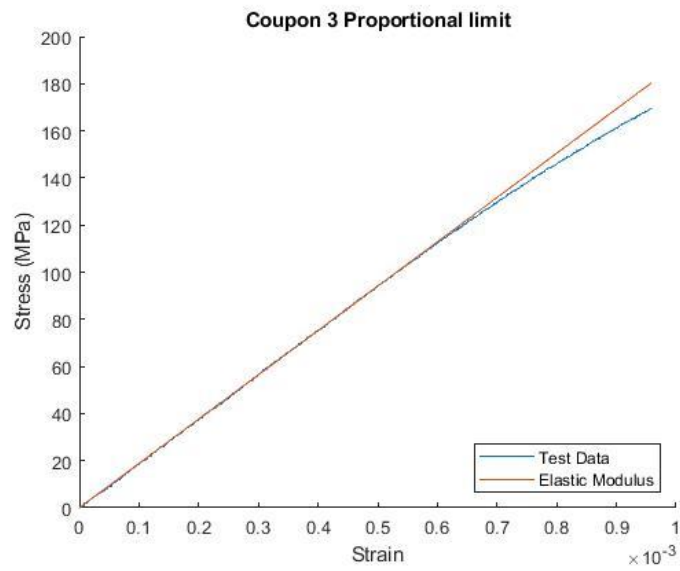


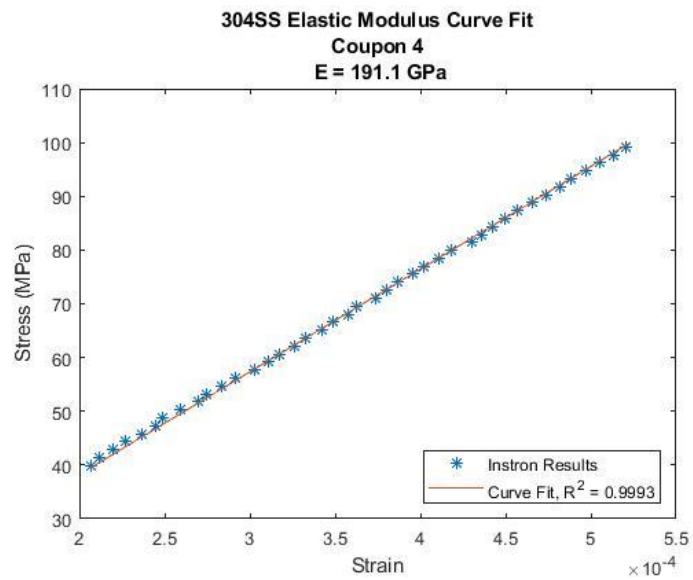
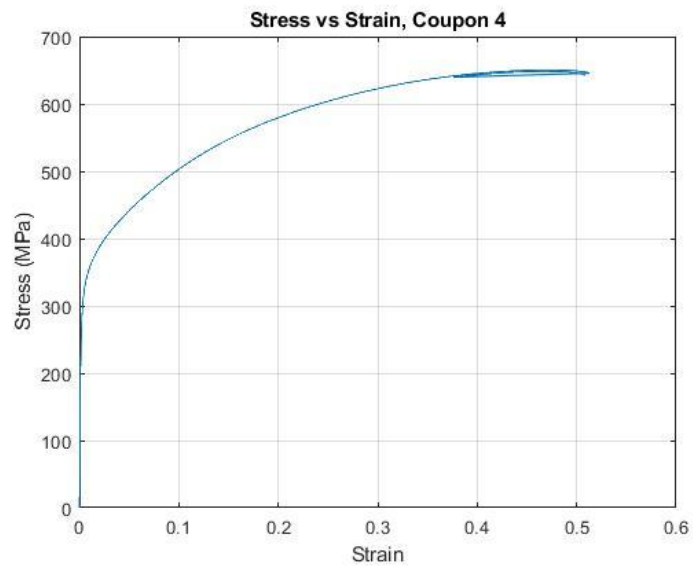


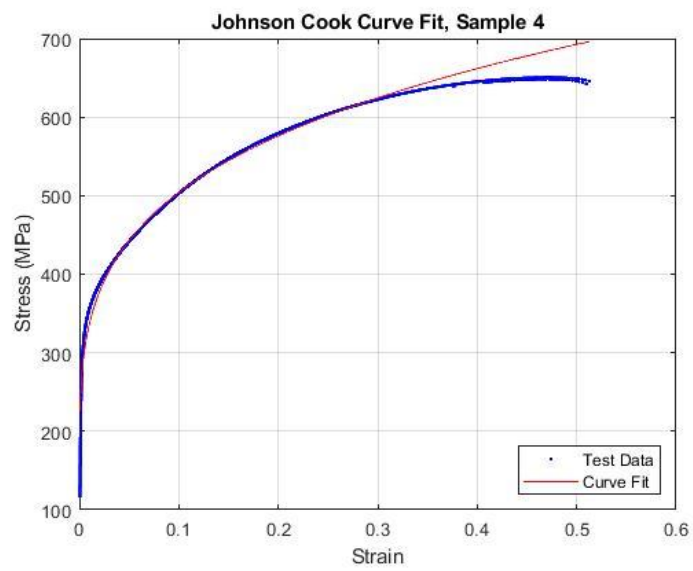
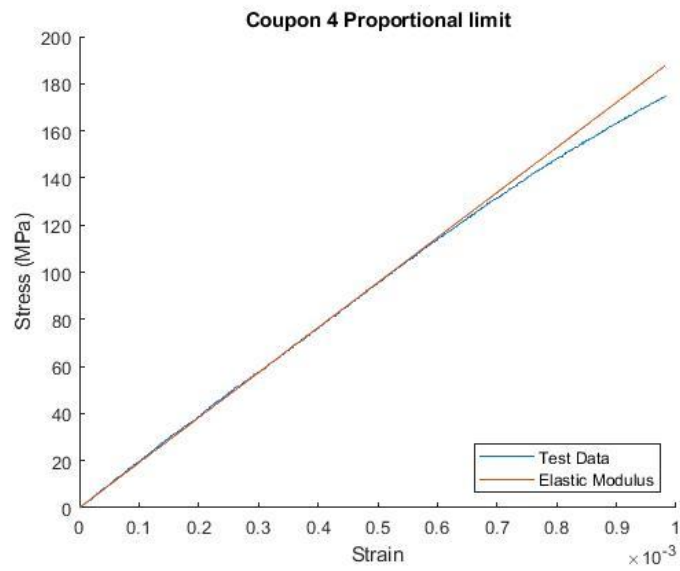


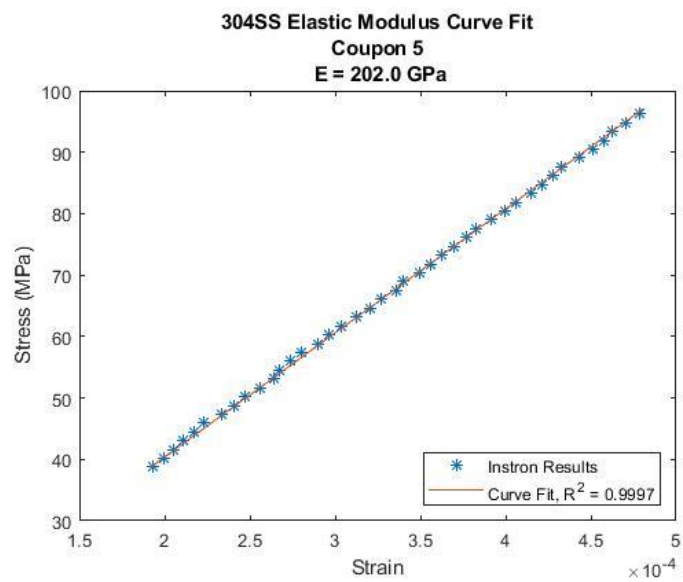
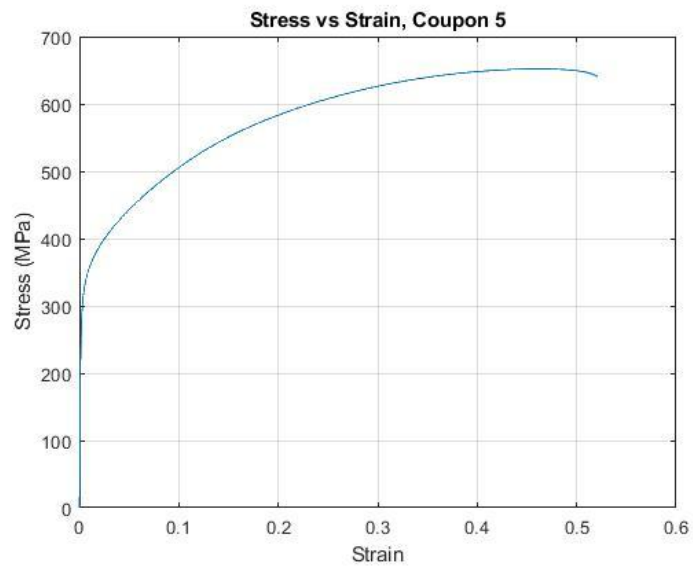


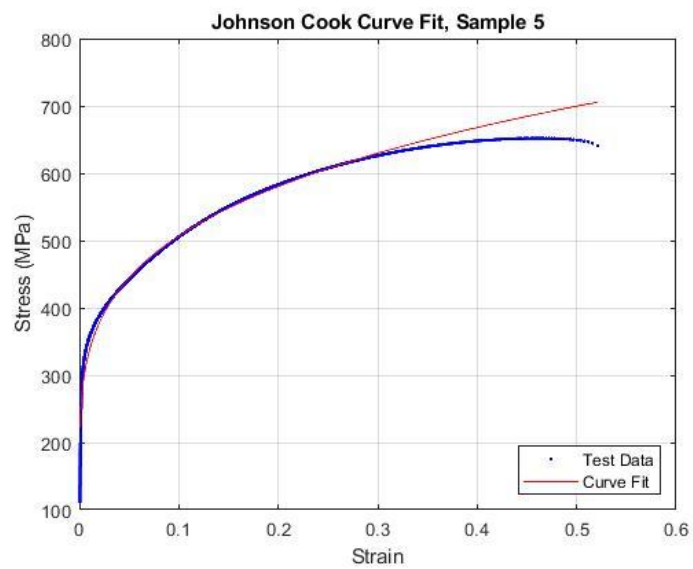
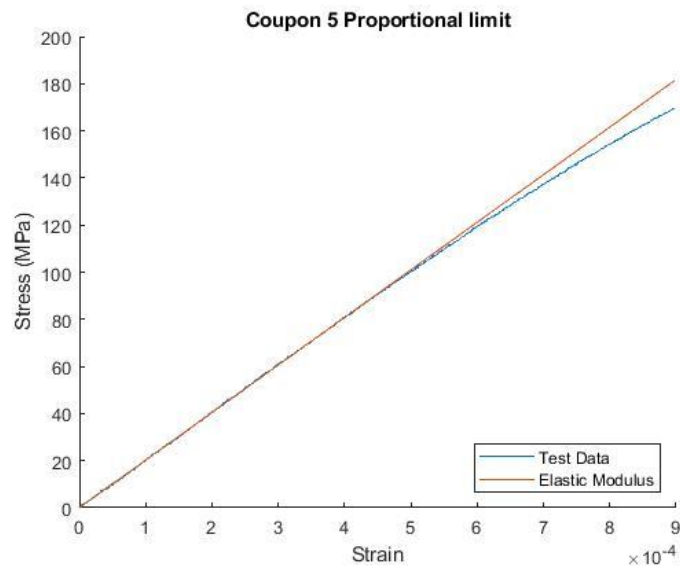




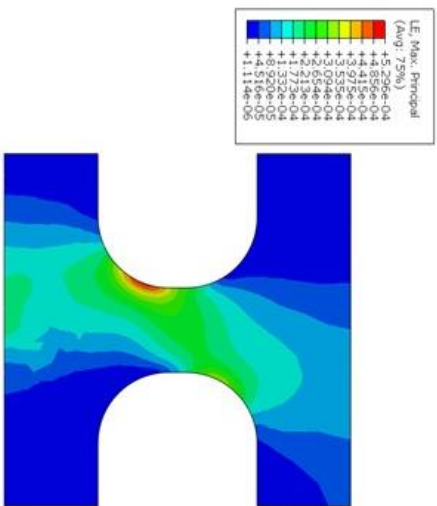
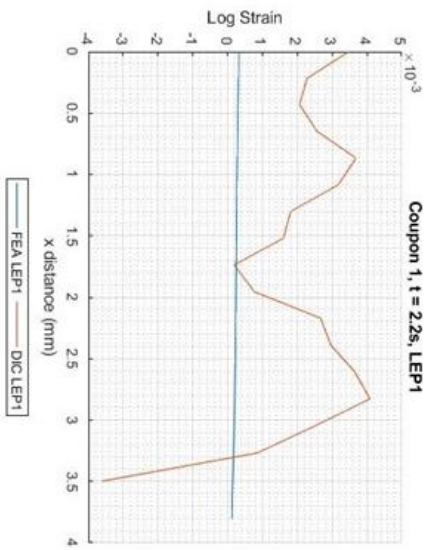








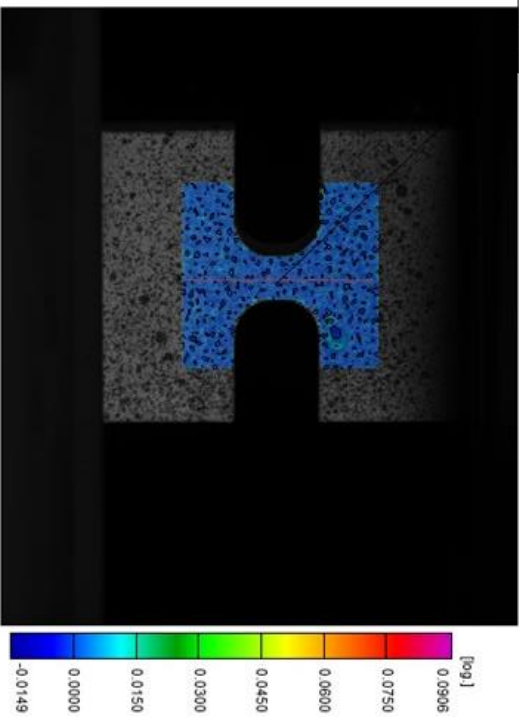
## APPENDIX B: COMPARISON OF IPL STRAIN DATA, FEA VS. DIC

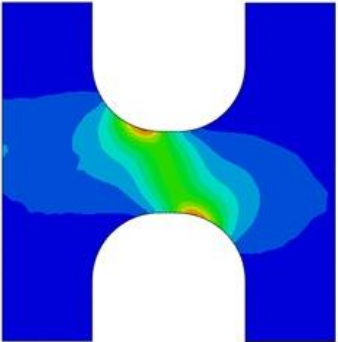
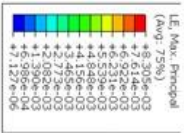
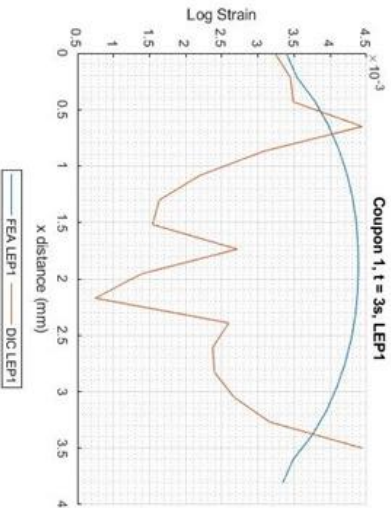


Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 11 |
| Frame Time    | 2.200 s |

| Virtual Extensometer |           |
|----------------------|-----------|
|                      | Diff.     |
| L/V                  | +0.004 mm |
| X                    | +0.006 mm |
| Y                    | +0.004 mm |
| Z                    | -0.000 mm |
| φ                    | 0.23 deg  |





Abaqus FEA

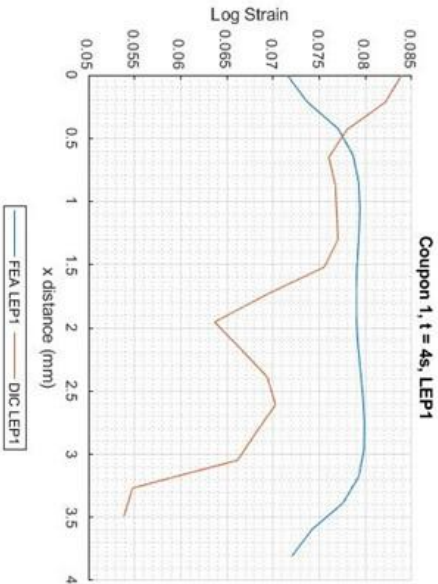
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 15 |
| Frame Time    | 3.000 s |

| Virtual Extensometer |           |
|----------------------|-----------|
|                      | Diff.     |
| L/V                  | +0.024 mm |
| X                    | +0.027 mm |
| Y                    | +0.024 mm |
| Z                    | +0.008 mm |
| φ                    | 0.014 deg |



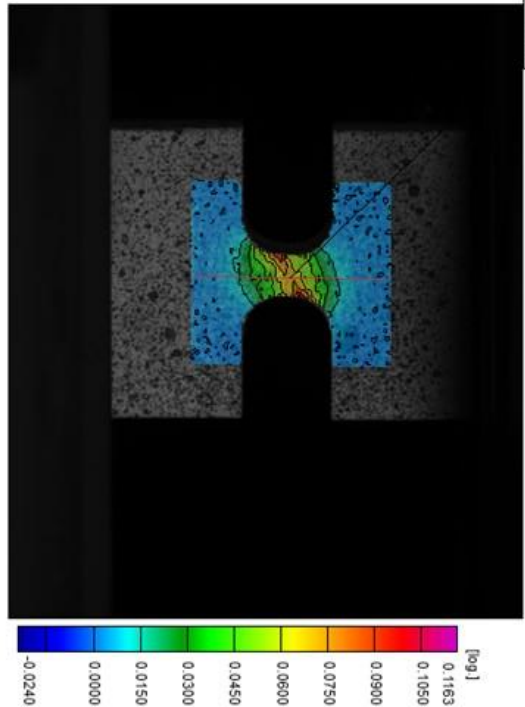
Aramis DIC



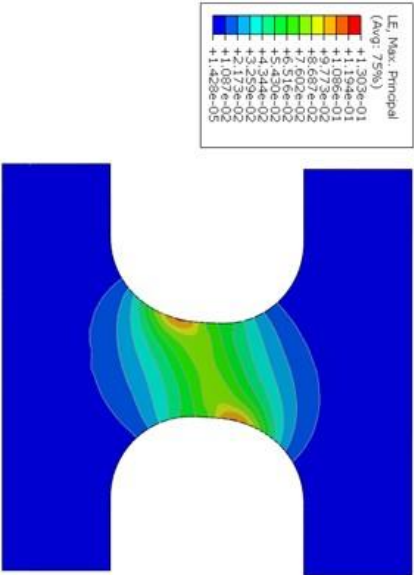
Major Strain

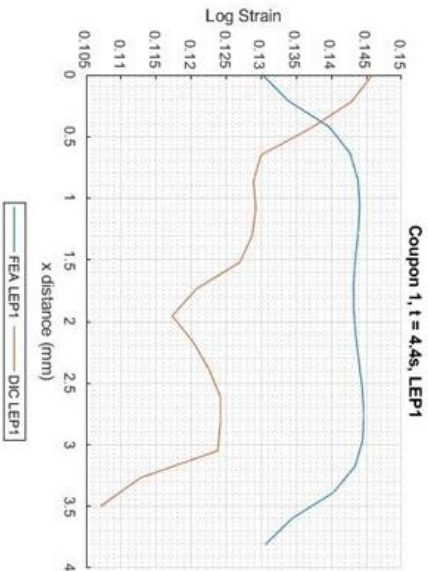
|               |         |
|---------------|---------|
| Stage from to | 0 -> 20 |
| Frame Time    | 4.000 s |

| Virtual Extensometer |           |
|----------------------|-----------|
|                      | Diff.     |
| L/V                  | +0.381 mm |
| X                    | +0.235 mm |
| Y                    | +0.378 mm |
| Z                    | +0.012 mm |
| φ                    | 0.014 deg |



Abaqus FEA

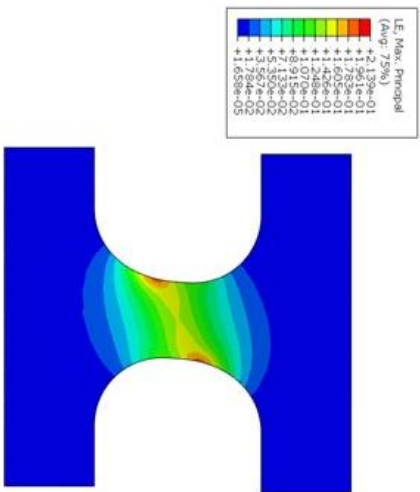




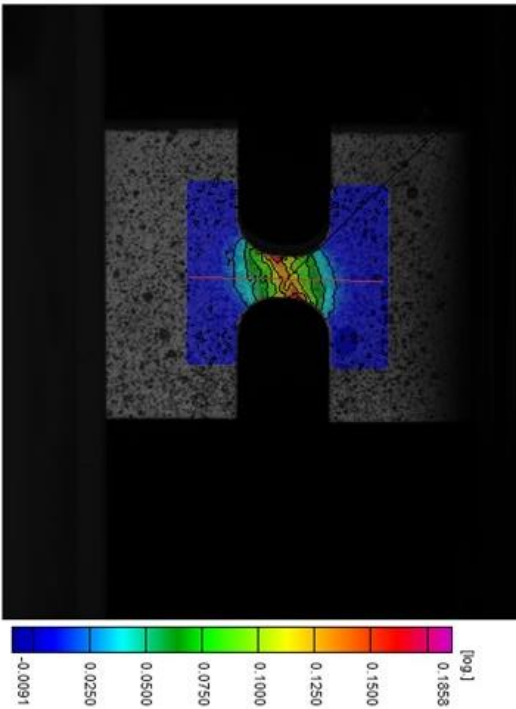
Major Strain

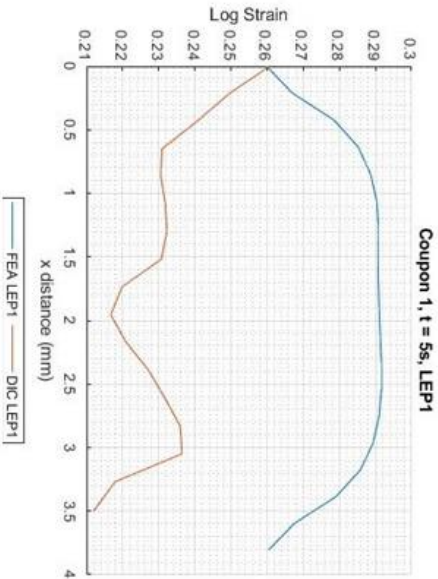
|               |         |
|---------------|---------|
| Stage from to | 0 -> 22 |
| Frame Time    | 4.400 s |

| Virtual Extensometer |           |
|----------------------|-----------|
|                      | Diff.     |
| LV                   | +0.652 mm |
| X                    | +0.344 mm |
| Y                    | +0.646 mm |
| Z                    | +0.009 mm |
| Φ                    | 0.023 deg |



Abaqus FEA

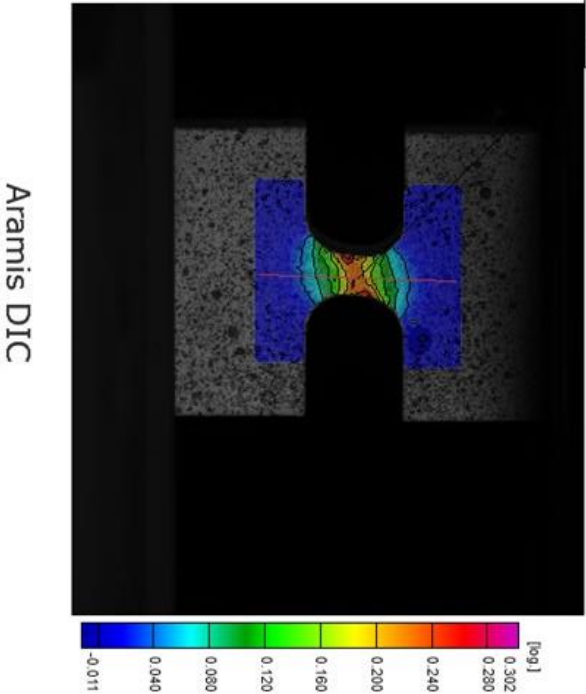
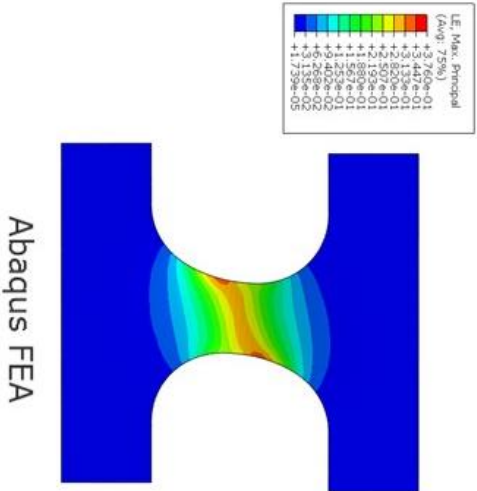


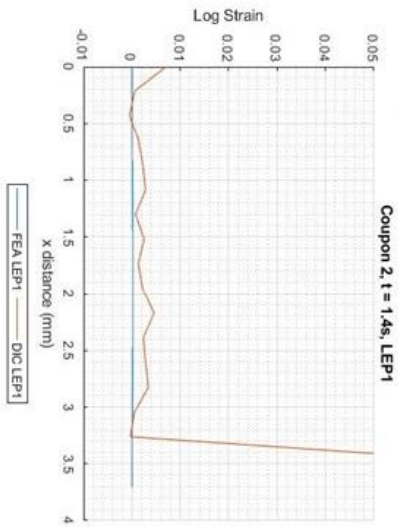


Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 25 |
| Frame Time    | 5.000 s |

| Virtual Extensometer |           |
|----------------------|-----------|
|                      | Diff.     |
| L/V                  | +1.156 mm |
| X                    | +0.524 mm |
| Y                    | +1.146 mm |
| Z                    | +0.007 mm |
| Φ                    | 0.019 deg |

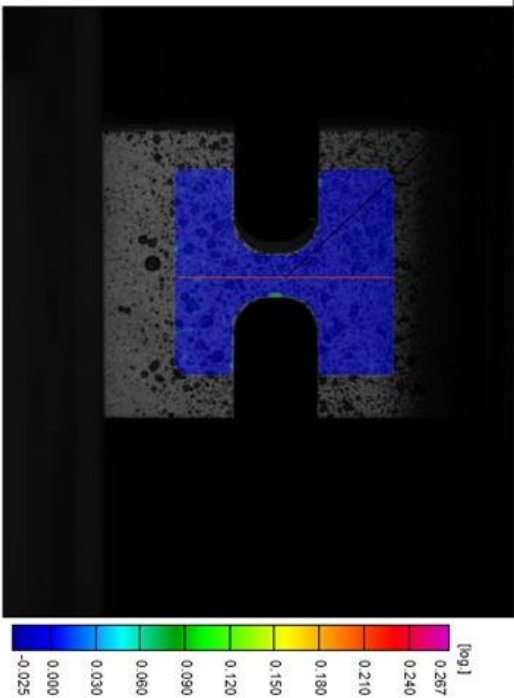
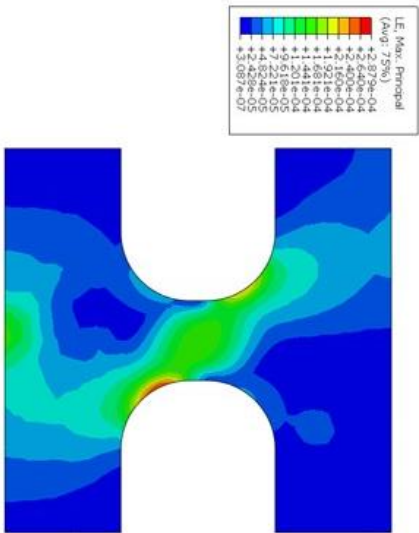


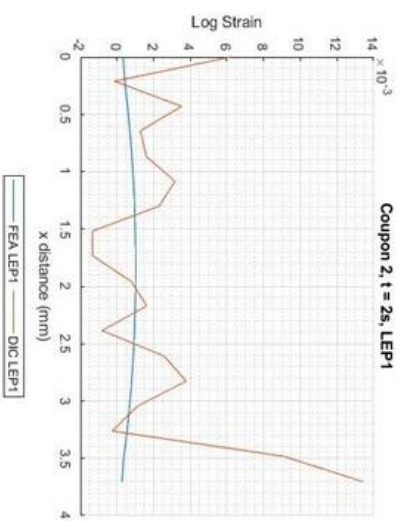


Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 7  |
| Frame Time    | 1.400 s |

| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| LV                 | -0.001 mm |
| X                  | -0.005 mm |
| Y                  | -0.000 mm |
| Z                  | +0.010 mm |
| φ                  | 0.008 deg |

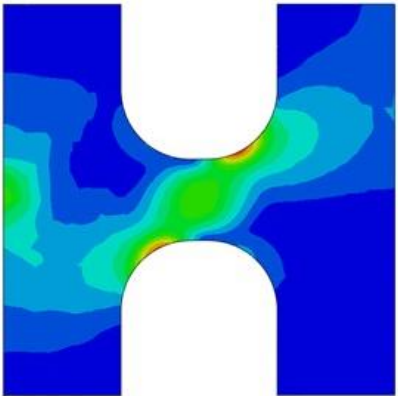
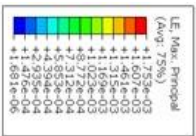




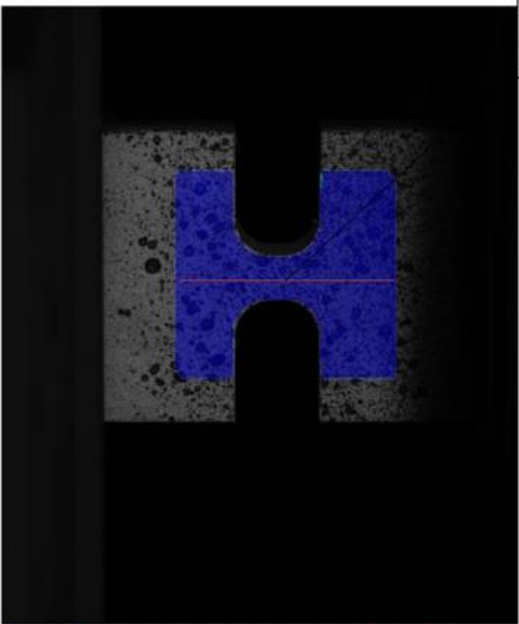
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 10 |
| Frame Time    | 2.000 s |

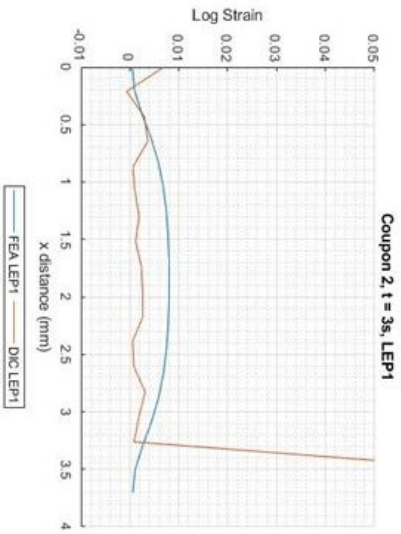
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +0.003 mm |
| X                  | -0.021 mm |
| Y                  | +0.003 mm |
| Z                  | -0.000 mm |
| φ                  | 0.005 deg |



Abaqus FEA



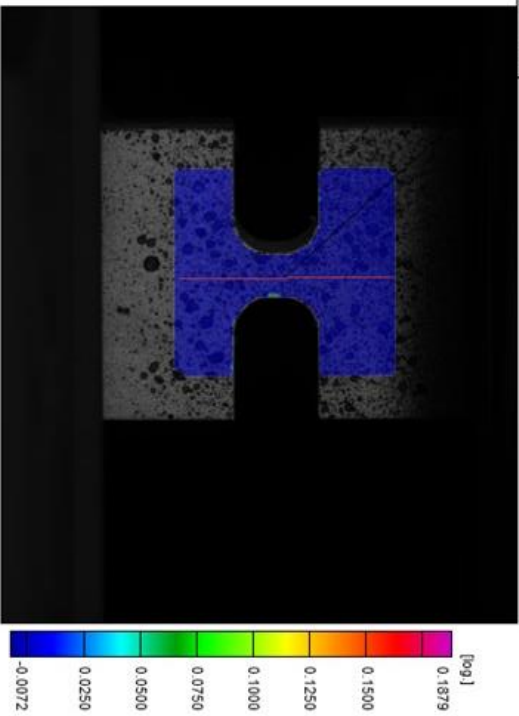
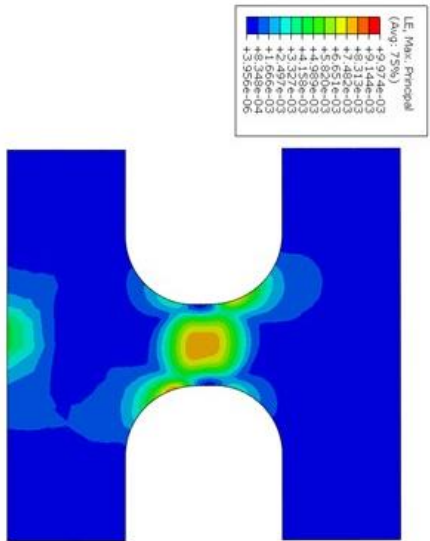
Aramis DIC

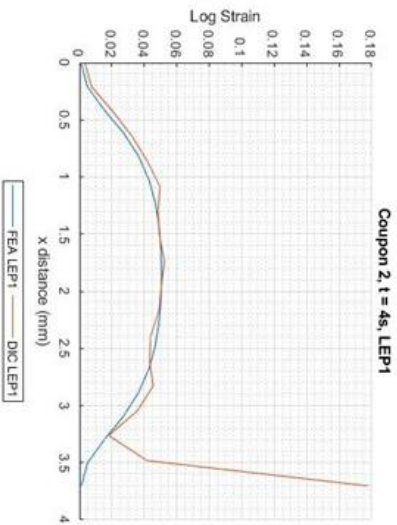


Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 15 |
| Frame Time    | 3.000 s |

| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| LV                 | +0.002 mm |
| X                  | -0.104 mm |
| Y                  | +0.003 mm |
| Z                  | +0.016 mm |
| $\Phi$             | 0.065 deg |

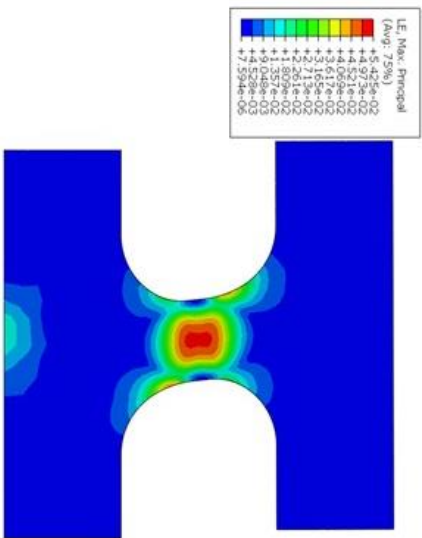




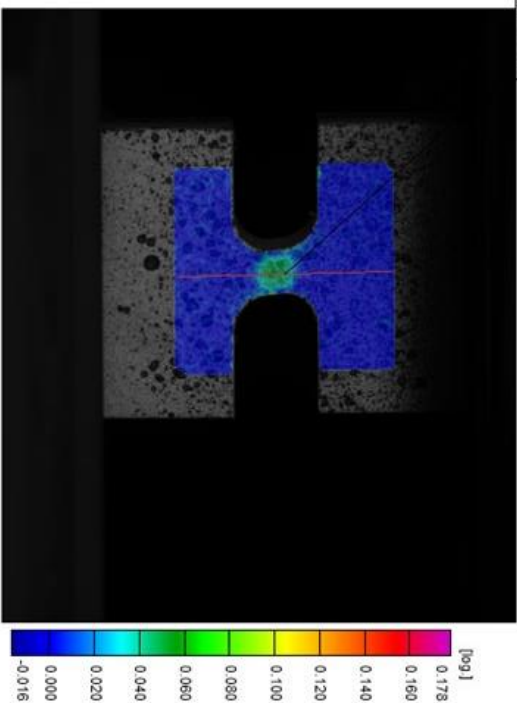
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 20 |
| Frame Time    | 4.000 s |

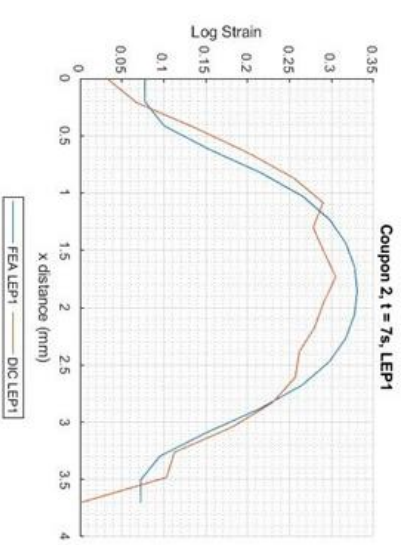
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| LV                 | -0.009 mm |
| X                  | -0.485 mm |
| Y                  | -0.013 mm |
| Z                  | +0.022 mm |
| φ                  | 0.178 deg |



Abaqus FEA



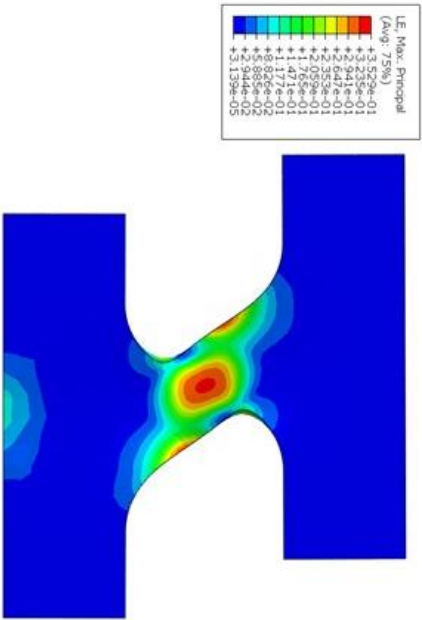
Aramis DIC



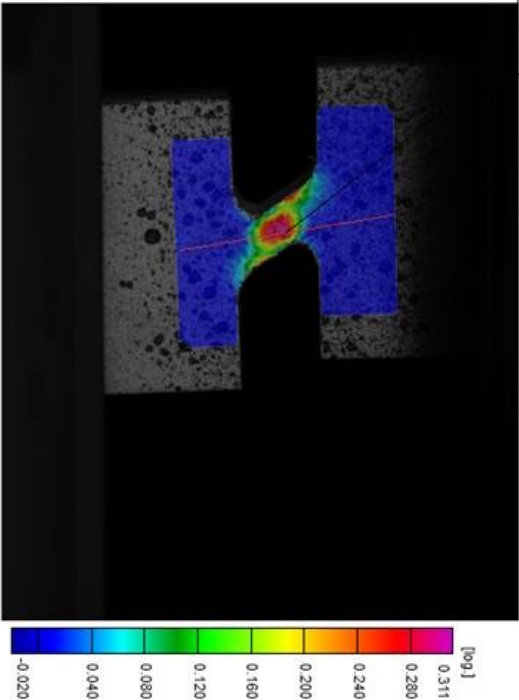
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 35 |
| Frame Time    | 7.000 s |

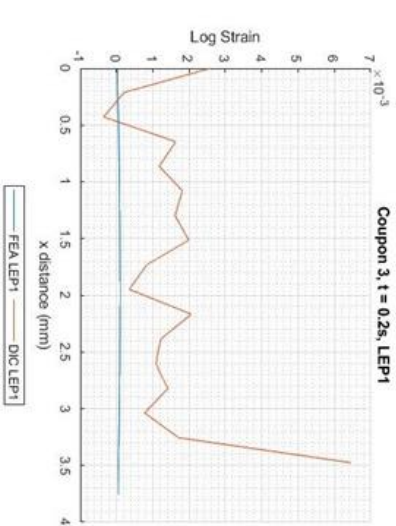
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| U/V                | +0.054 mm |
| X                  | -2.971 mm |
| Y                  | -0.180 mm |
| Z                  | +0.086 mm |
| Φ                  | 0.132 deg |



Abaqus FEA



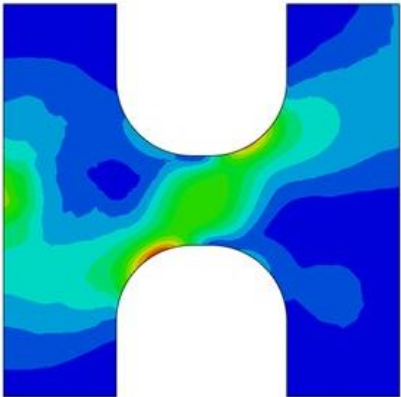
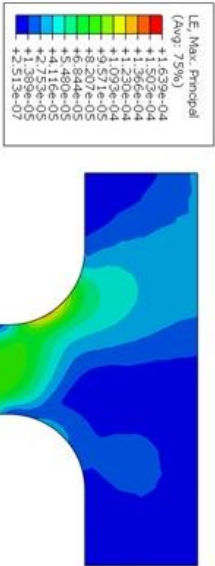
Aramis DIC



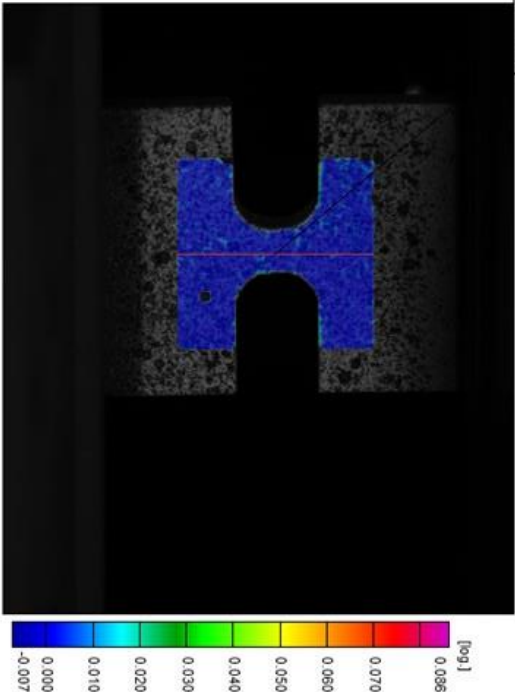
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 1  |
| Frame Time    | 4.400 s |

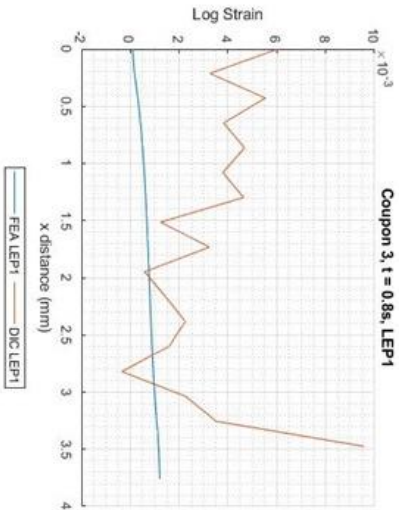
| Long-1 - Reference |           |
|--------------------|-----------|
| Diff.              |           |
| LV                 | +0.000 mm |
| X                  | -0.003 mm |
| Y                  | +0.000 mm |
| Z                  | -0.003 mm |
| Φ                  | 0.012 deg |



Abaqus FEA



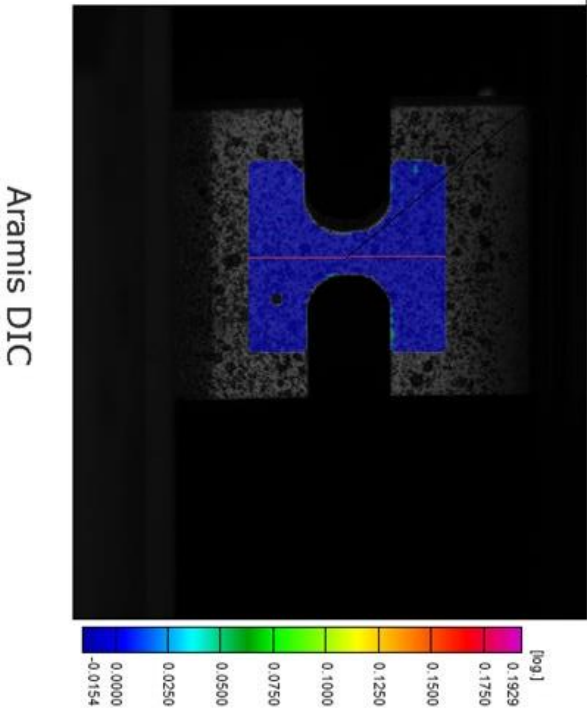
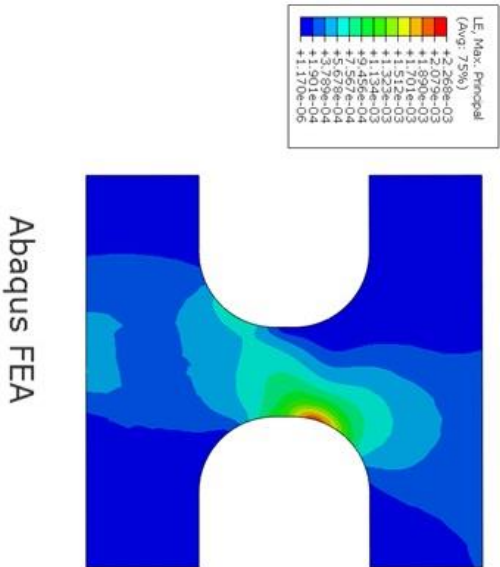
Aramis DIC

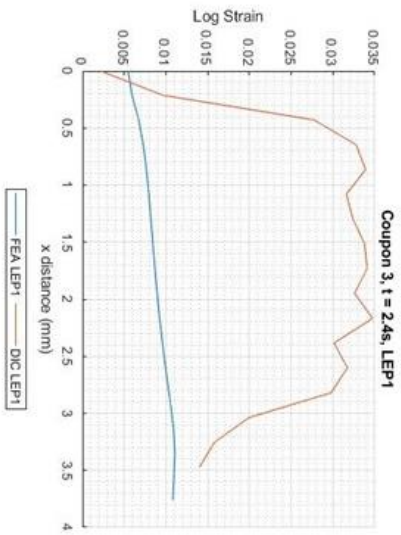


|               |         |
|---------------|---------|
| Stage from to | 0 -> 4  |
| Frame Time    | 5.000 s |

Major Strain

| Long-1 - Reference |            |
|--------------------|------------|
|                    | Diff.      |
| L/V                | +0.006 mm  |
| X                  | -0.005 mm  |
| Y                  | +0.006 mm  |
| Z                  | -0.007 mm  |
| φ                  | -0.095 deg |

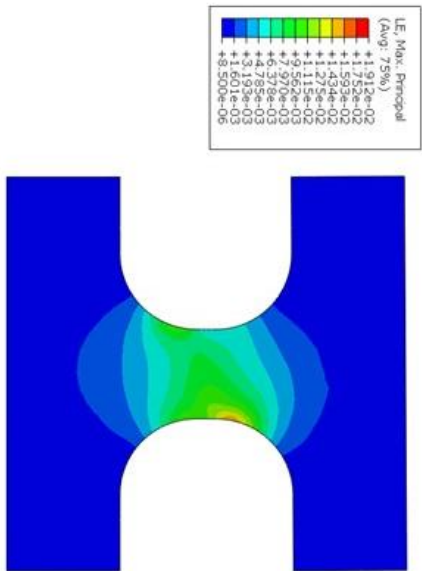




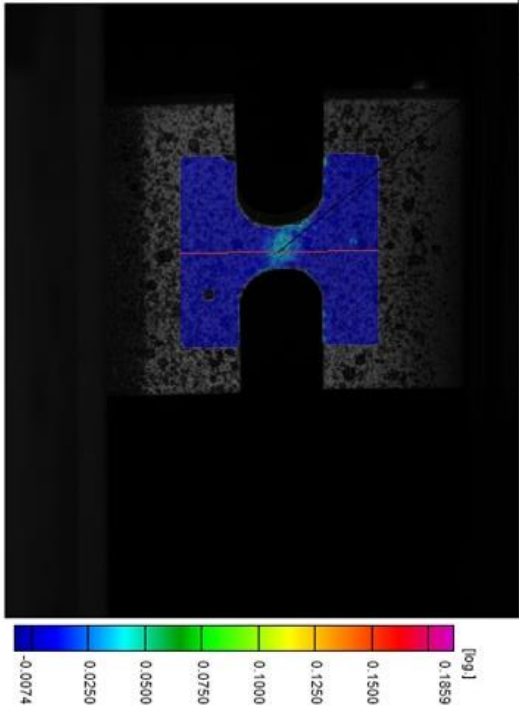
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 12 |
| Frame Time    | 6.600 s |

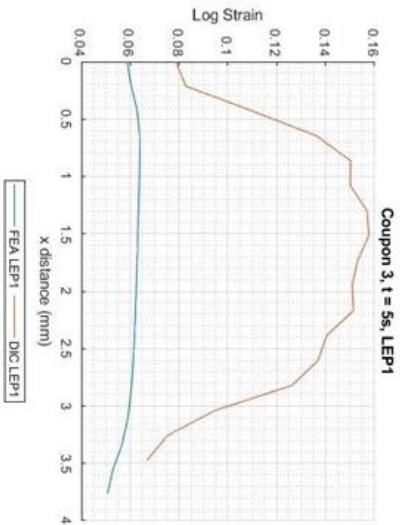
| Long-1 - Reference |            |
|--------------------|------------|
|                    | Diff.      |
| LV                 | +0.056 mm  |
| X                  | -0.029 mm  |
| Y                  | +0.056 mm  |
| Z                  | -0.007 mm  |
| Φ                  | -0.336 deg |



Abaqus FEA



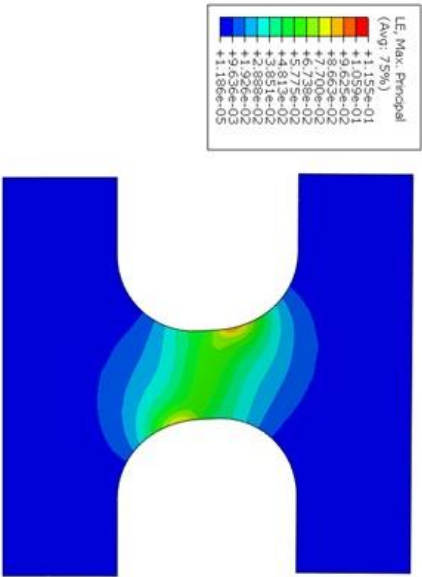
Aramis DIC



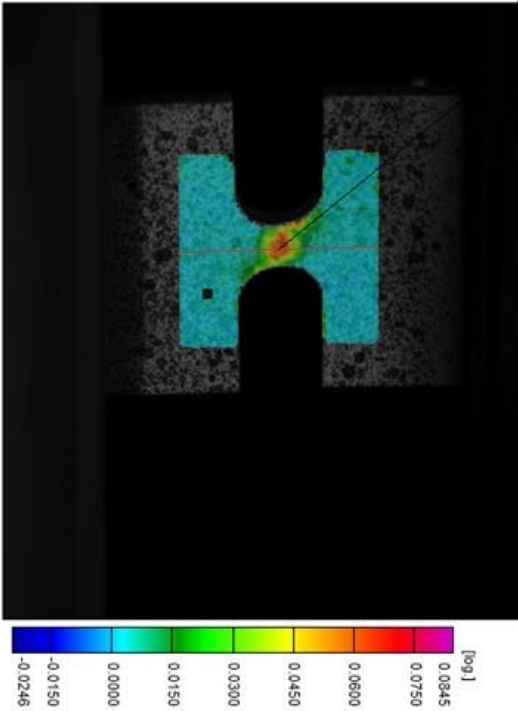
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 15 |
| Frame Time    | 7.200 s |

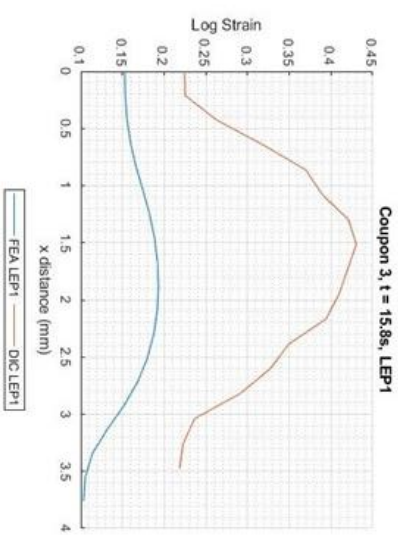
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff. 1   |
| LV                 | +0.098 mm |
| X                  | -0.047 mm |
| Y                  | +0.098 mm |
| Z                  | -0.004 mm |
| φ                  | 0.382 deg |



Abaqus FEA



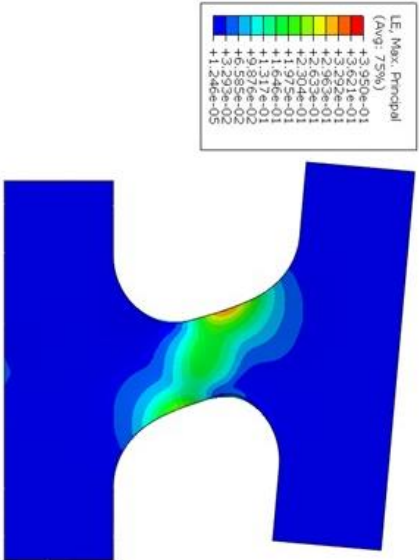
Aramis DIC



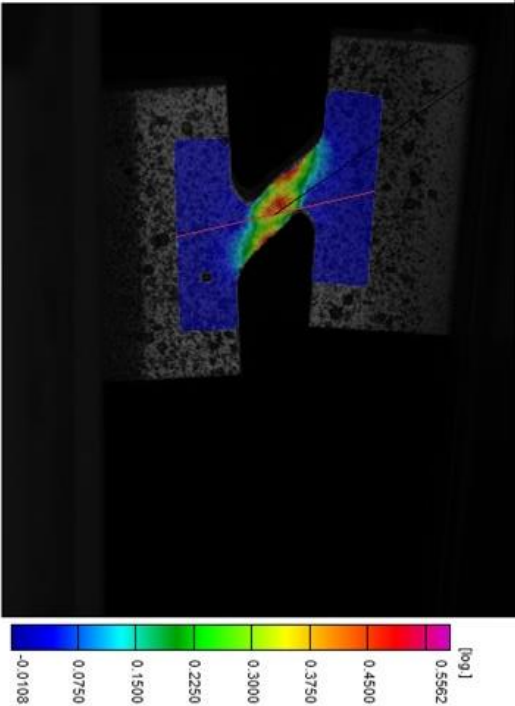
Major Strain

|               |          |
|---------------|----------|
| Stage from to | 0 -> 79  |
| Frame Time    | 20.000 s |

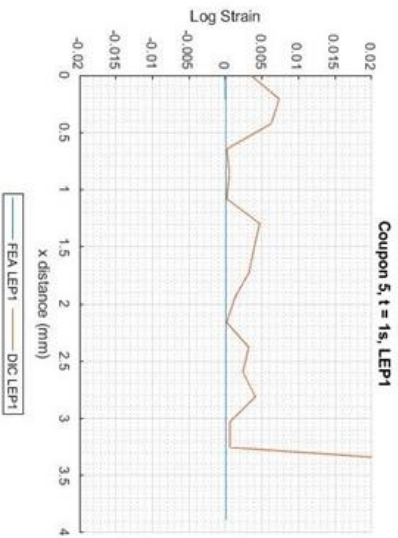
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| LV                 | +0.500 mm |
| X                  | -0.530 mm |
| Y                  | +0.494 mm |
| Z                  | -0.012 mm |
| ψ                  | s deg     |



Abaqus FEA



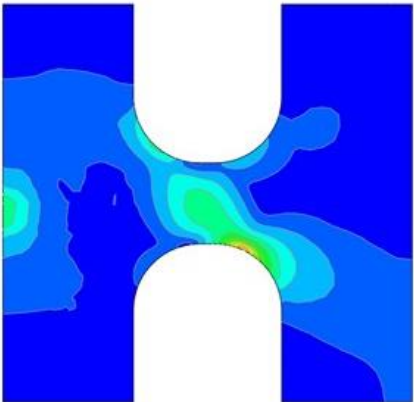
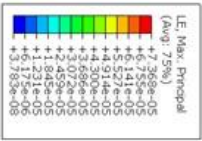
Aramis DIC



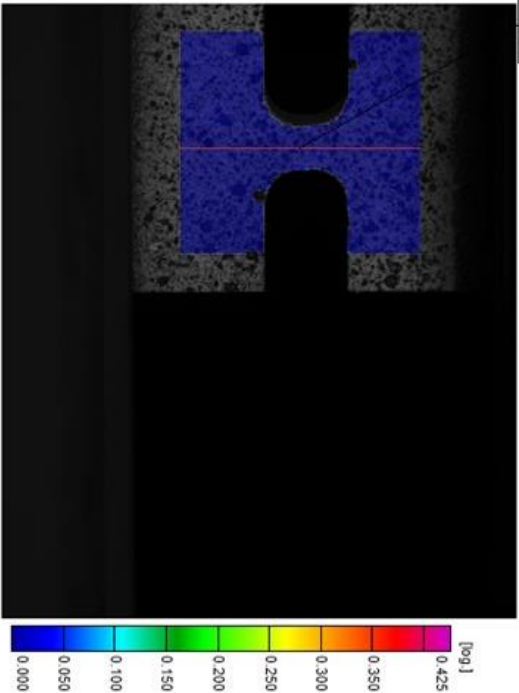
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 5  |
| Frame Time    | 1.000 s |

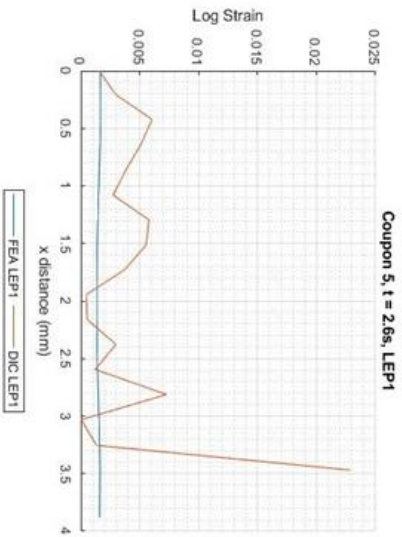
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +0.003 mm |
| X                  | +0.002 mm |
| Y                  | +0.003 mm |
| Z                  | -0.000 mm |
| dφ                 | 0.754 deg |



Abaqus FEA



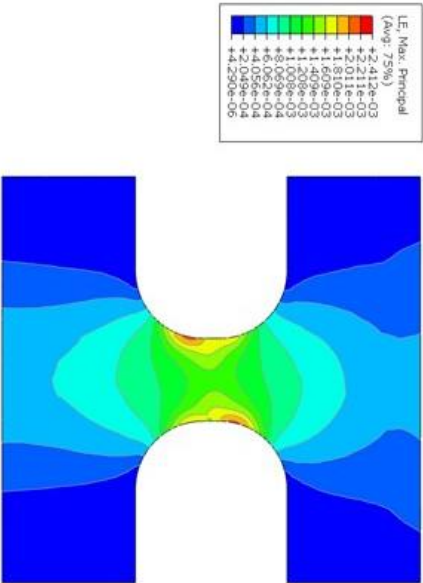
Aramis DIC



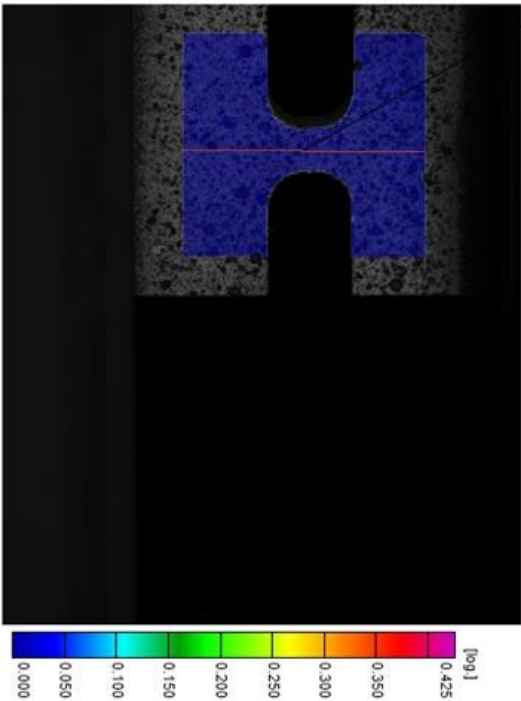
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 13 |
| Frame Time    | 2.600 s |

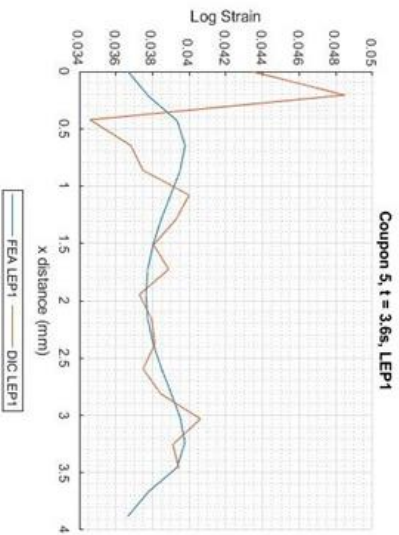
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +0.016 mm |
| X                  | +0.005 mm |
| Y                  | +0.016 mm |
| Z                  | +0.025 mm |
| dir                | 0.737 deg |



Abaqus FEA



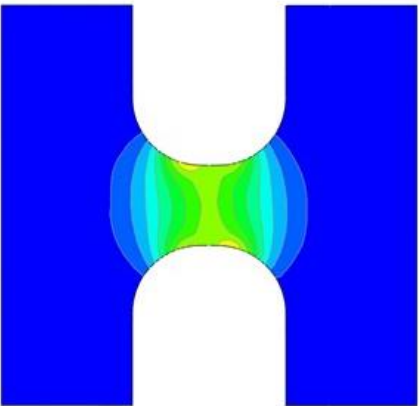
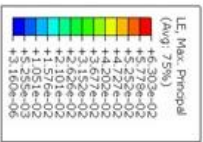
Aramis DIC



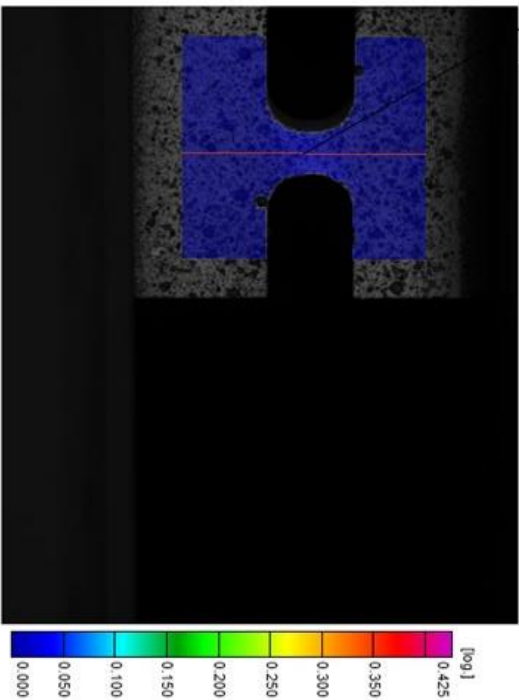
### Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 18 |
| Frame Time    | 3.600 s |

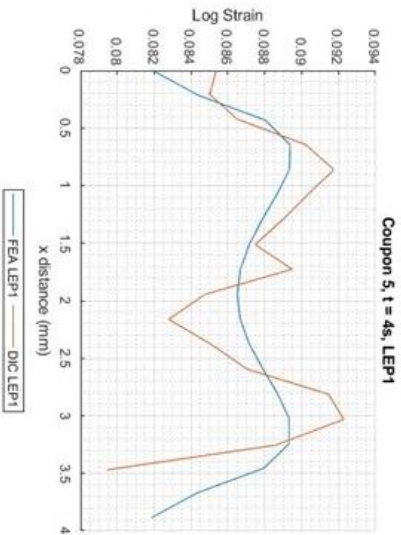
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +0.224 mm |
| X                  | +0.118 mm |
| Y                  | +0.223 mm |
| Z                  | +0.000 mm |
| dp                 | ??? deg   |



Abaqus FEA



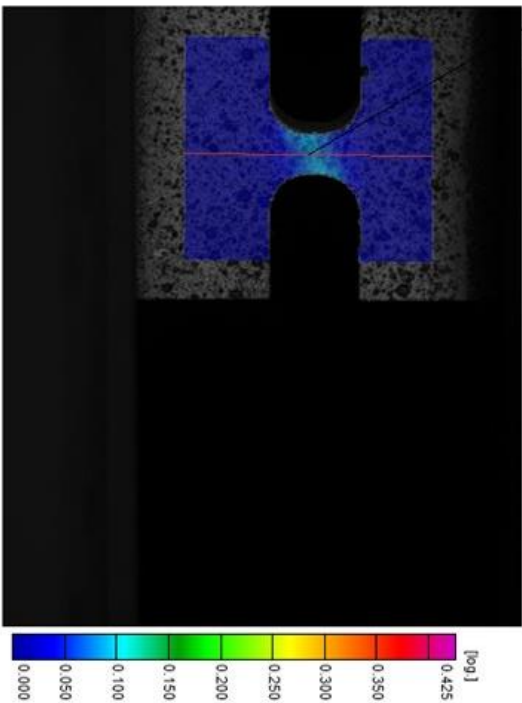
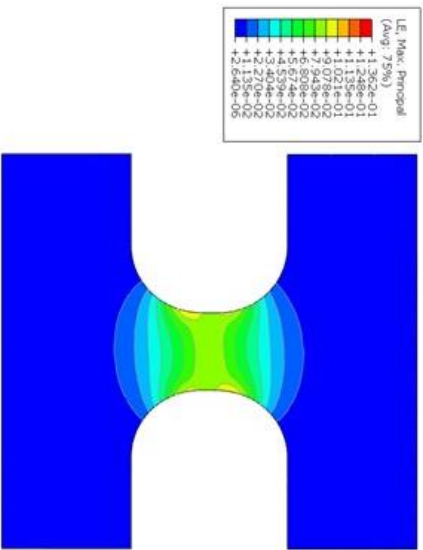
Aramis DIC

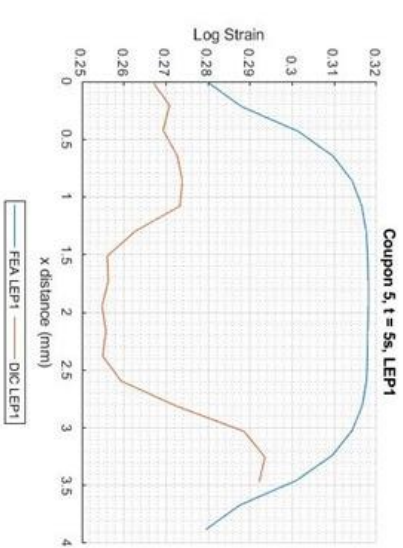


Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 20 |
| Frame Time    | 4.000 s |

| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +0.461 mm |
| X                  | +0.217 mm |
| Y                  | +0.458 mm |
| Z                  | -0.014 mm |
| dir                | ???       |

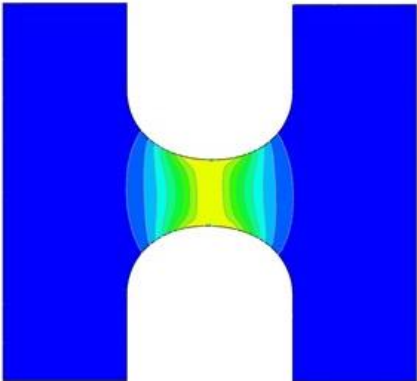
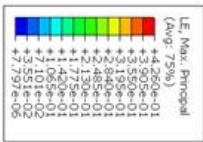




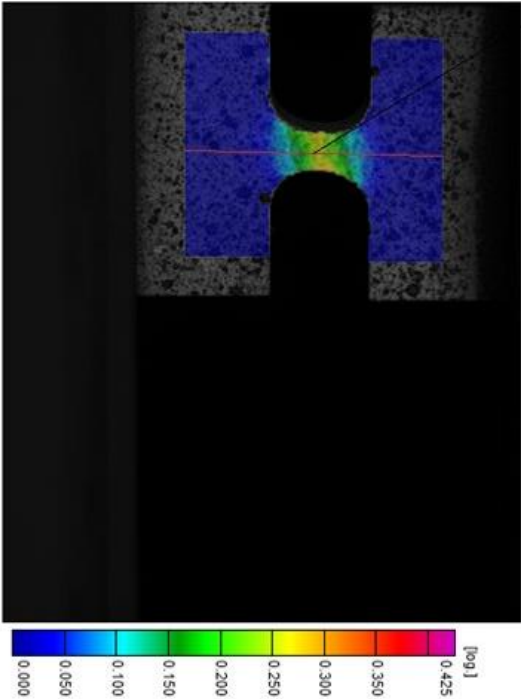
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 25 |
| Frame Time    | 5.000 S |

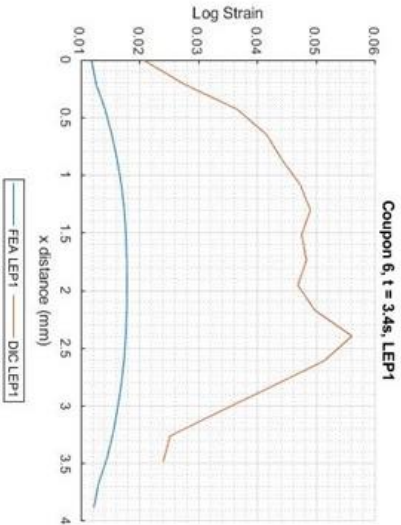
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +1.295 mm |
| X                  | +0.509 mm |
| Y                  | +1.285 mm |
| Z                  | -0.012 mm |
| dir                | 0.715 deg |



Abaqus FEA



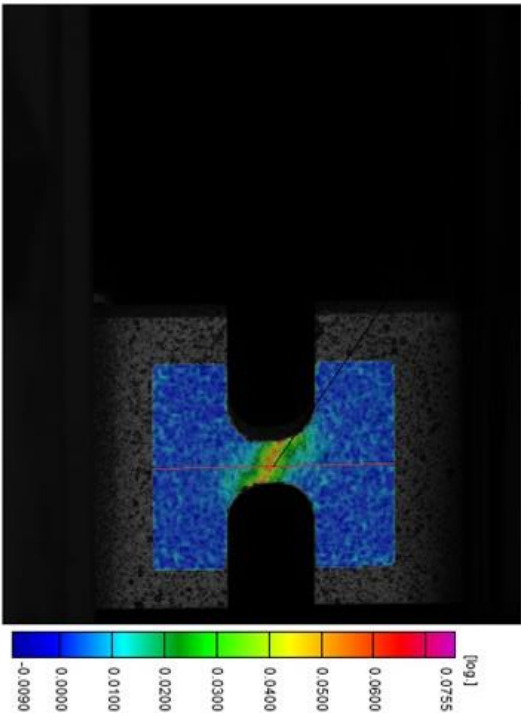
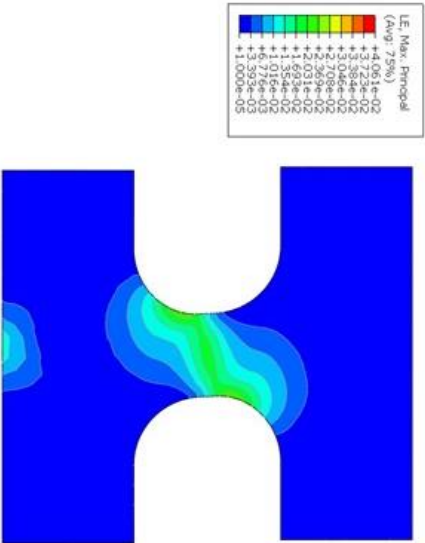
Aramis DIC

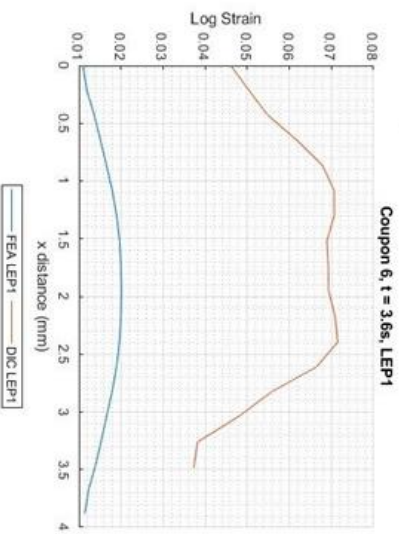


Major Strain

|               |         |
|---------------|---------|
| Image from to | 0 -> 17 |
| Frame Time    | 3.400 s |

| Long-1 - Reference |           |
|--------------------|-----------|
| Diff.              |           |
| L/V                | +0.160 mm |
| X                  | -0.204 mm |
| Y                  | -0.165 mm |
| Z                  | +3.597 mm |
| dg                 | 0.595 deg |

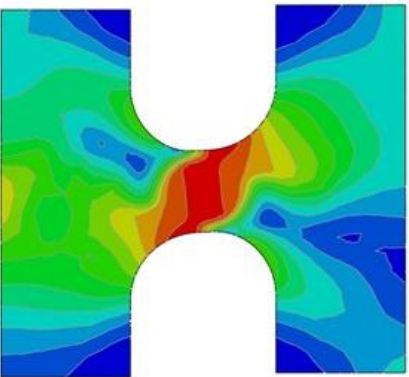
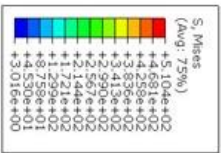




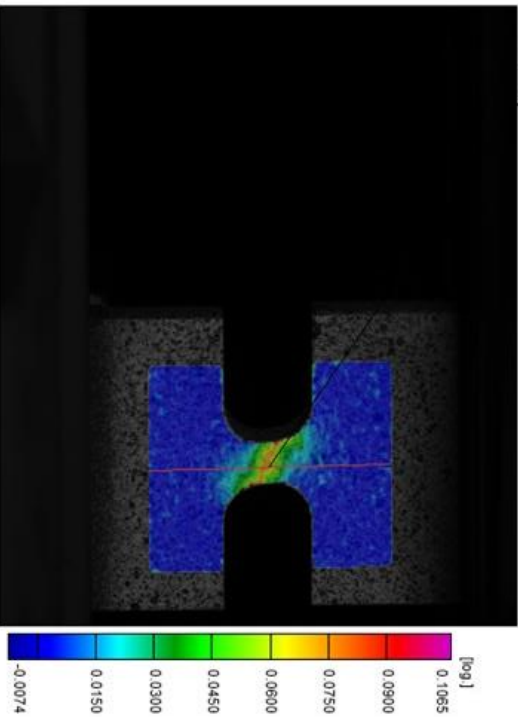
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 18 |
| Frame Time    | 3.600 s |

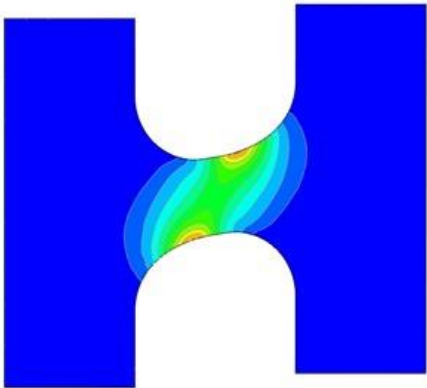
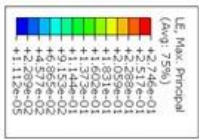
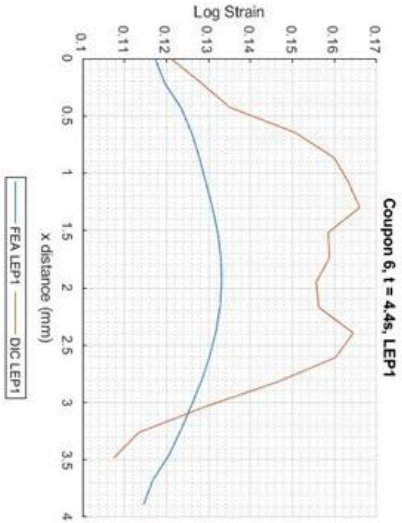
| Long-I - Reference |           |
|--------------------|-----------|
| Diff.              |           |
| L/V                | +0.244 mm |
| X                  | -0.299 mm |
| Y                  | -0.113 mm |
| Z                  | +3.764 mm |
| dφ                 | 0.595 deg |



Abaqus FEA



Aramis DIC

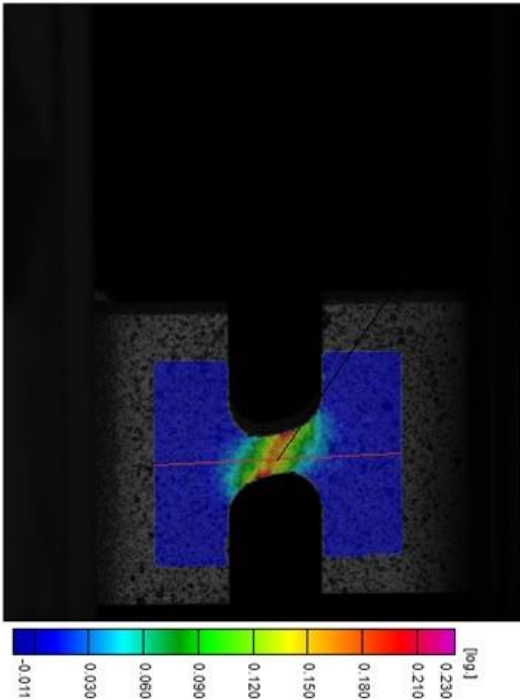


Abaqus FEA

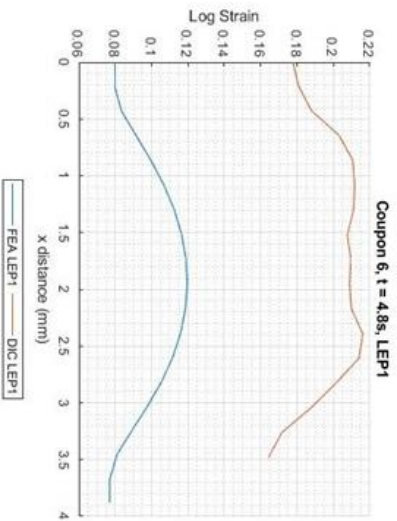
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 22 |
| Frame Time    | 4.400 s |

| Long.1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +0.699 mm |
| X                  | -0.751 mm |
| Y                  | +0.584 mm |
| Z                  | +2.003 mm |
| dφ                 | 0.550 deg |



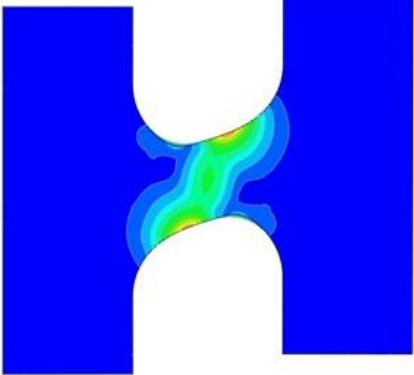
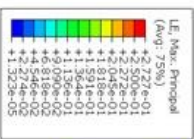
Aramis DIC



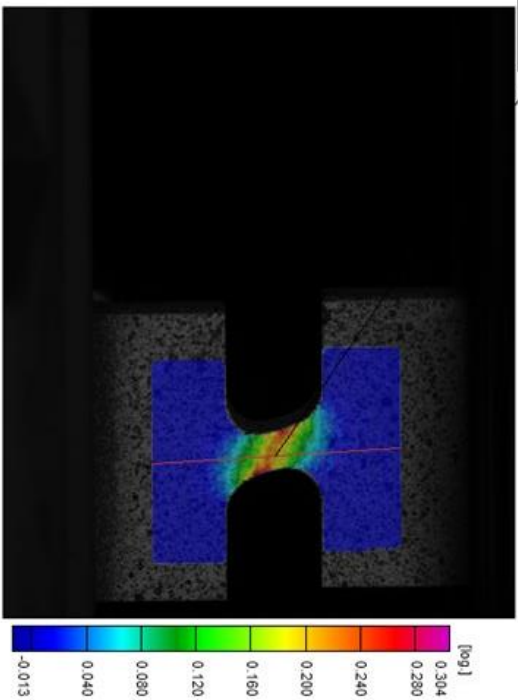
### Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 24 |
| Frame Time    | 4.800 s |

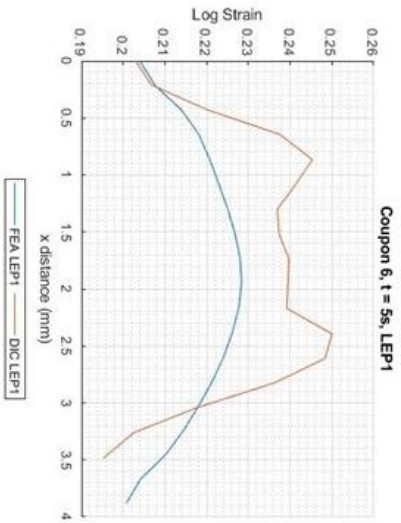
| Long-1 - Reference |           |
|--------------------|-----------|
| Diff.              |           |
| L/V                | +1.020 mm |
| X                  | -0.995 mm |
| Y                  | +0.010 mm |
| Z                  | +6.346 mm |
| dφ                 | 0.515 deg |



Abaqus FEA



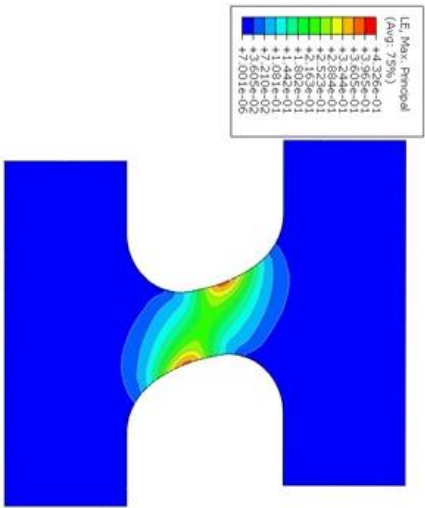
Aramis DIC



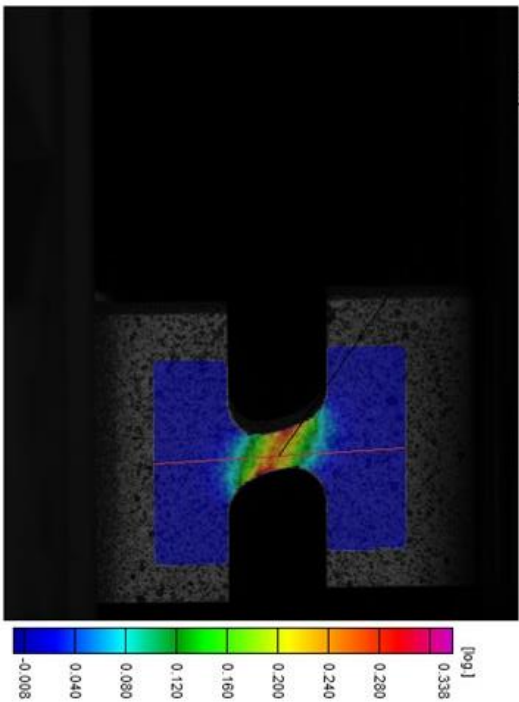
Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 25 |
| Frame Time    | 5.000 s |

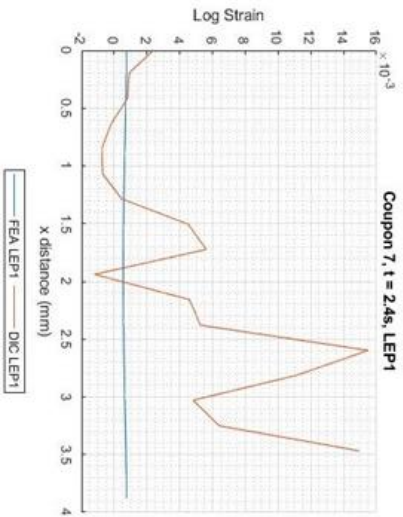
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +1.203 mm |
| X                  | -1.112 mm |
| Y                  | +0.946 mm |
| Z                  | +3.061 mm |
| dφ                 | 0.508 deg |



Abaqus FEA



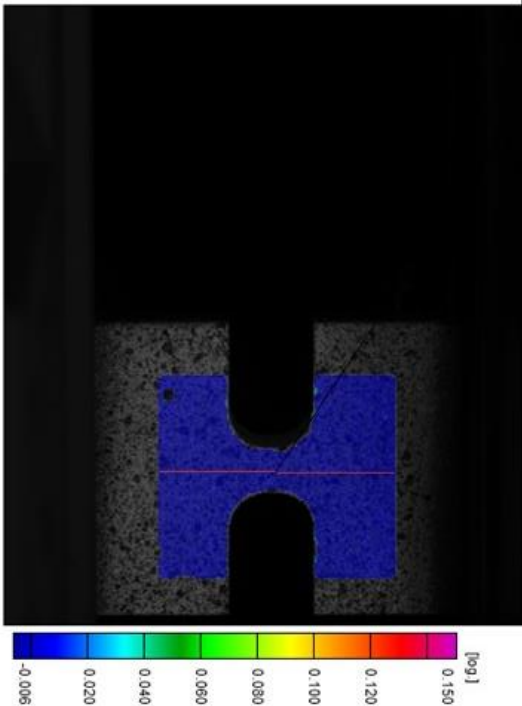
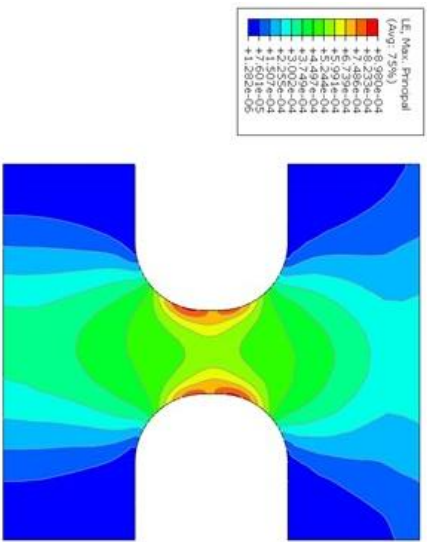
Aramis DIC

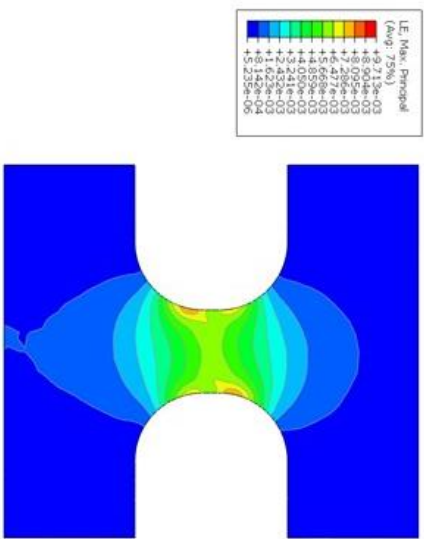


|               |         |
|---------------|---------|
| Stage from to | 0 -> 12 |
| Frame Time    | 2.400 s |

Major Strain

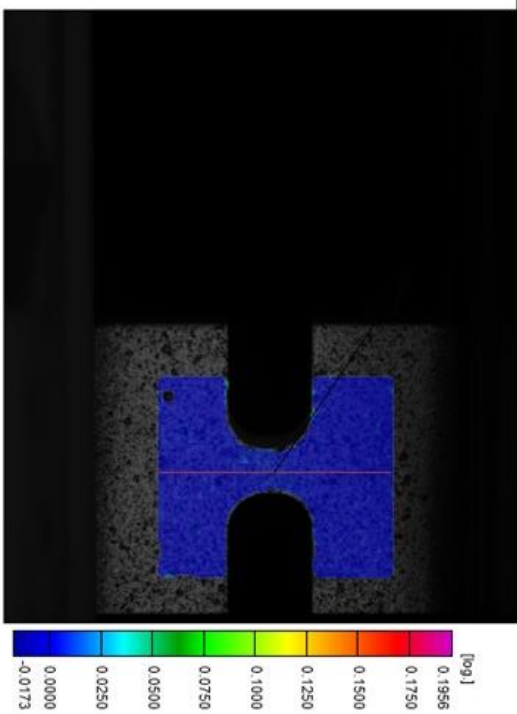
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +0.008 mm |
| X                  | +0.001 mm |
| Y                  | +0.008 mm |
| Z                  | -0.005 mm |
| φ                  | 0.606 deg |

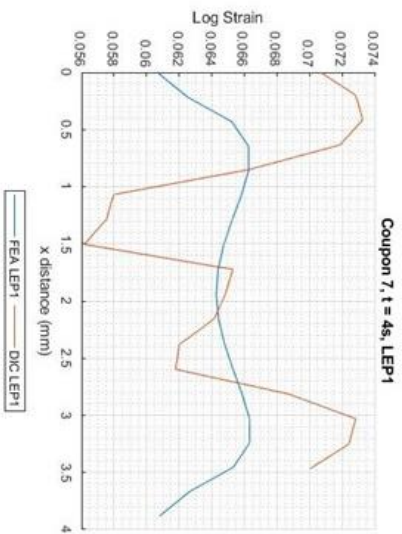




|               |         |
|---------------|---------|
| Stage from to | 0 -> 16 |
| Frame Time    | 3.200 s |

| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| LV                 | +0.041 mm |
| X                  | +0.005 mm |
| Y                  | +0.041 mm |
| Z                  | -0.007 mm |
| φ                  | .612 deg  |

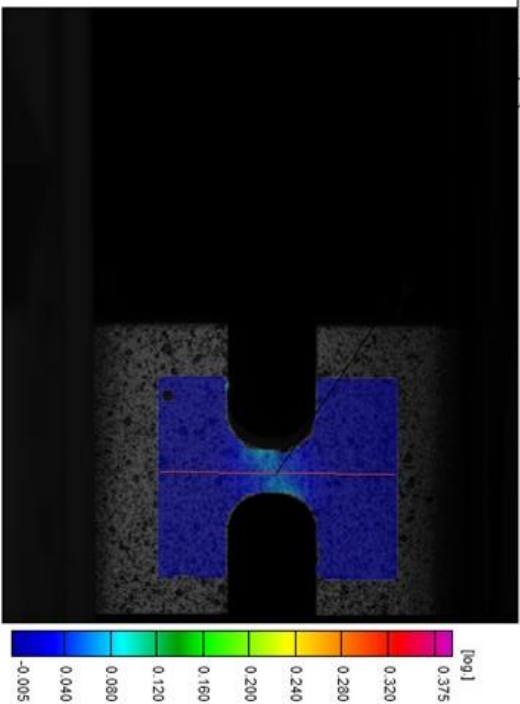
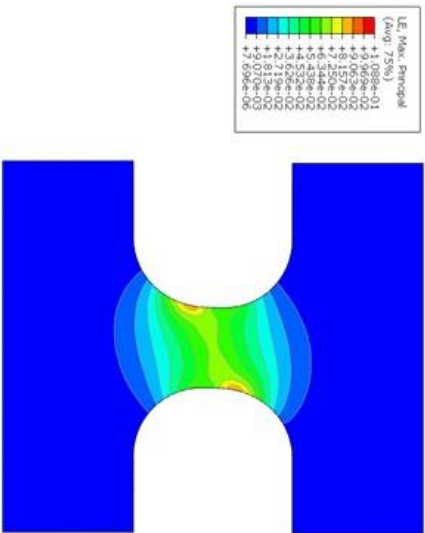


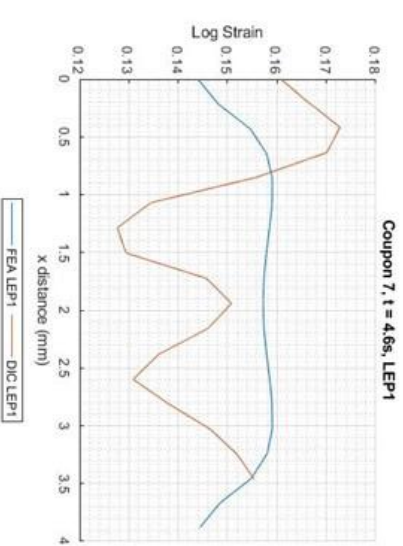


### Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 20 |
| Frame Time    | 4.000 s |

| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +0.345 mm |
| X                  | +0.120 mm |
| Y                  | +0.344 mm |
| Z                  | -0.067 mm |
| Φ                  | 0.620 deg |

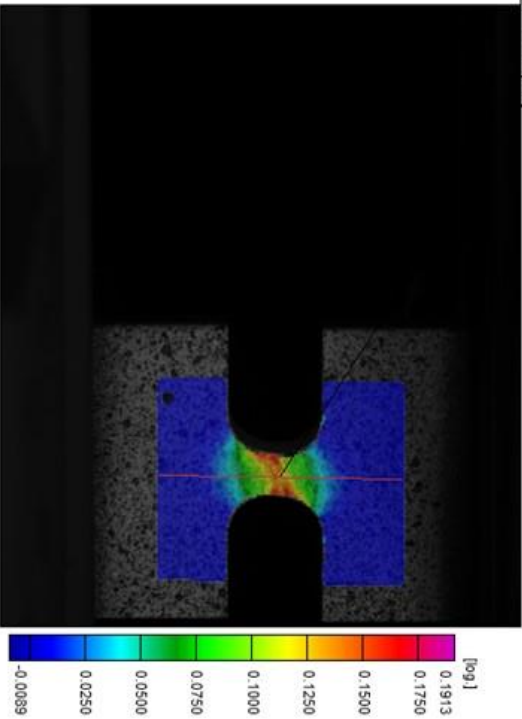




Major Strain

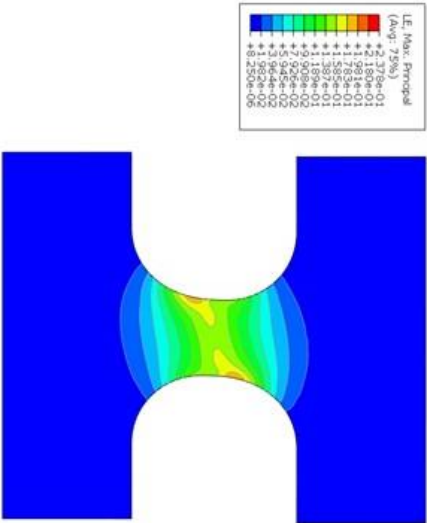
|               |         |
|---------------|---------|
| Image from to | 0 -> 23 |
| Frame Time    | 4.600 s |

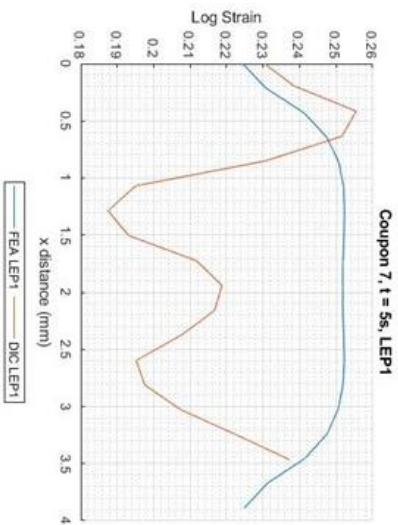
| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +0.749 mm |
| X                  | +0.226 mm |
| Y                  | +0.746 mm |
| Z                  | -0.165 mm |
| φ                  | 0.618 deg |



Aramis DIC

Abaqus FEA

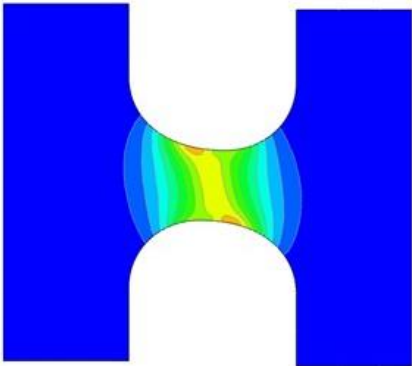
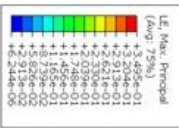
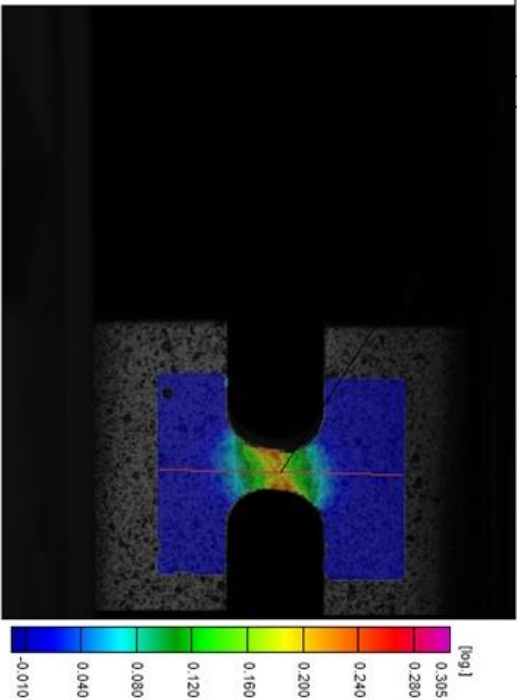




Major Strain

|               |         |
|---------------|---------|
| Stage from to | 0 -> 25 |
| Frame Time    | 5.000 s |

| Long-1 - Reference |           |
|--------------------|-----------|
|                    | Diff.     |
| L/V                | +1.086 mm |
| X                  | +0.304 mm |
| Y                  | +1.081 mm |
| Z                  | -0.233 mm |
| φ                  | 0.803 deg |



Abaqus FEA

Aramis DIC

