



Magnetic properties of two copper (II) halide layered perovskites  
by Nava Rabiner Sivron

A thesis submitted in partial fulfillment of the requirements for the degree of Master of Science in  
Physics

Montana State University

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Abstract:

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Both compounds demonstrate an antiferromagnetic exchange between the layers, since the value measured for the exchange parameter is negative.  $J_{2h} = -57 \pm 7$  for  $(SAP)CuBr_4$  and  $-25 \pm 1$  for  $(SAP)CuCl_4$ . Both salts demonstrate ferromagnetic exchange within the layer, with positive  $J_{1h} = 15 \pm 1$  for the Cl compound and  $20.5 \pm 2.5$  for the Br.

The interaction is stronger for  $(SAP)CuBr_4$  than for  $(SAP)CuCl_4$  as the absolute values of both  $J_{1h}/k$  and  $J_{2h}/k$  are larger for the bromide compound. The antiferromagnetic exchange is dominant for both samples. For the bromide salt this result is more evident, as the ratio  $J_{2h}/J_{1h}$  is larger.

The Cu-X and the X-X bond lengths are found to affect the strength of the exchange interaction in a similar way to other salts. Longer bonds result in weaker interaction. The natural logarithm of X-X bond length and the natural logarithm of  $J_{2h}/k$  obey the linearity which was previously found for  $(nDA)CuX_4$  series of compounds.

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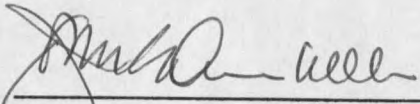
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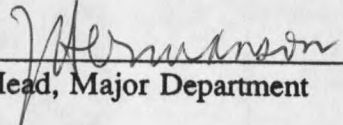
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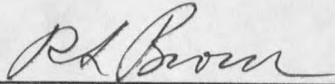
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## TABLE OF CONTENTS

	Page
1. INTRODUCTION.....	1
Theoretical Background.....	2
2. SAMPLE STRUCTURE AND PREPARATION.....	10
Sample Preparation.....	10
Crystal Structure.....	12
3. EXPERIMENTAL INFORMATION.....	19
4. EXPERIMENTAL RESULTS.....	30
5. CONCLUSION.....	43
REFERENCES CITED.....	45
APPENDIX.....	47

## LIST OF TABLES

Table	Page
1. Structural information of $(3AP)CuBr_4$ and $(3AP)CuCl_4$ .....	18
2. Helium consumption in %, and temperature variation in degrees Kelvin /min as a function of helium flow rates in cc/min. The flow numbers could change if the v.s.m. top is sealed in a different way then it was when this table was made. This table is for Cooling.....	24
3. Helium consumption in %, and temperature variation in degrees Kelvin /min as a function of helium flow rates in cc/min. The flow numbers could change if the v.s.m. top is sealed in a different way then it was when this table was made. This table is for heating.....	25
4. New results for the values of the exchange parameters and the g constant for the compounds $(3AP)CuBr_4$ and $(3AP)CuCl_4$ , obtained by the Vibrating Sample Magnetometer.....	38
5. Predicted values for the exchange parameters and the g constant.....	38

## LIST OF FIGURES

Figure	Page
1. A side look at the layers reveals the eclipsed structure and shows how the layers are linked. The c axis of the monoclinic crystal is horizontal and the b axis is vertical.....	15
2. A look at the two dimensional noncentrosymmetric structure of the layer.....	16
3. A look at the atomic structure of the layer. The b axis of the monoclinic crystal is horizontal and the a axis is vertical. Each Cu atom has 4 Cu neighbors inside the layer, bridged by one X halide, and 2 Cu neighbors from adjacent layers, bridged by 2X halides.....	17
4. The susceptibility vs. Inverse temperature for HgCo(SCN) <sub>4</sub> . The curve was repeatable at the range 4.2-150. This range was chosen for future measurements of unknown samples .....	29
5. The magnetization vs. temperature of (3AP)CuBr <sub>4</sub> .....	32
6. The magnetization vs. temperature of (3AP)CuCl <sub>4</sub> .....	33
7. The inverse susceptibility vs. temperature for (3AP)CuBr <sub>4</sub> .....	34
8. The inverse susceptibility vs. temperature for (3AP)CuCl <sub>4</sub> .....	35
9. Fit of the data of (3AP)CuBr <sub>4</sub> , created by SAS statistical program on the VAX network. The experimental data points are marked in x and the model calculated for the optimal values is marked as a solid line.....	36
10. Fit of the data of (3AP)CuCl <sub>4</sub> , created by SAS statistical program on the VAX network. The experimental data points are marked in x and the model calculated for the optimal values is marked as a solid line.....	37
11. J <sub>1b</sub> /k values vs. Cu···Br measured in Å, of A'CuBr <sub>4</sub> and A <sub>2</sub> CuBr <sub>4</sub> . Previous data points are marked as squares, and the new result for the (3AP)CuBr <sub>4</sub> is marked as a full circle.....	39

## LIST OF FIGURES-Cont'd

Figure	Page
12. $J_{1n}/k$ values vs. $\text{Cu}\cdots\text{Cl}$ measured in $\text{\AA}$ , of $\text{A}'\text{CuCl}_4$ and $\text{A2CuCl}_4$ . Previous data points are marked as squares, and the new result for the $(3\text{AP})\text{CuCl}_4$ is marked as a full circle.....	40
13. $\ln J_{2n}/k$ values vs. $\ln \text{Br}\cdots\text{Br}$ for $(\text{nDA})\text{CuBr}_4$ series. Previous data points are marked as squares and the new result obtained in this work is marked as a full circle.....	41
14. $\ln J_{2n}/k$ values vs. $\ln \text{Br}\cdots\text{Br}$ for $(\text{nDA})\text{CuCl}_4$ series. Previous data points are marked as squares and the new result obtained in this work is marked as a full circle.....	42
15. Documentation of general data analysis in fortran.....	47

## ABSTRACT

The magnetic moments of copper(II) halide perovskite salts  $(3AP)CuX_4$ , where X stands for Br or Cl, have been reported for the first time.

The experimental results are explained by the Baker model, which is a high T expansion of the Heisenberg Hamiltonian for a square lattice combined with a molecular exchange field correction.

Both compounds demonstrate an antiferromagnetic exchange between the layers, since the value measured for the exchange parameter is negative.  $J_{2h} = -57 \pm 7$  for  $(3AP)CuBr_4$  and  $-25 \pm 1$  for  $(3AP)CuCl_4$ . Both salts demonstrate ferromagnetic exchange within the layer, with positive  $J_{1h} = 15 \pm 1$  for the Cl compound and  $20.5 \pm 2.5$  for the Br.

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## CHAPTER 1

### INTRODUCTION

In 1988 the crystal structures of two new copper (II) halide layer perovskite salts were reported for the first time. The special interest in the 3-ammoniumpyridinium tetrabromocuprate(II) and 3-ammoniumpyridinium tetrachlorocuprate(II), arose from the fact that they were non centrosymmetric. Predictions about their magnetization, made by comparison with other crystals were limited, and subject to the fact that insufficient data had existed to make satisfying correlations for the tetrahedrally distorted anions.<sup>[1]</sup>

It was expected that the strength of the exchange interaction for the bromide salts would be greater than for the chloride salts. The samples were expected to demonstrate a ferromagnetic exchange inside the layer and antiferromagnetic exchange between the layers.

In this work the crystal growth was repeated according to the literature, and the powder susceptibility was measured, both by cooling and by heating. The data was interpreted using the Baker model Heisenberg high temperature series expansion for a square lattice, combined with a molecular exchange field correction.<sup>[7,10]</sup>

A detailed explanation of the structure of the crystals and how it relates to the predictions of the magnetic behavior of the samples is given in chapter 2, as well as

information pertaining to the crystal growth. Estimates of the accuracy and signal stability of the Vibrating Sample Magnetometer which was used to measure the magnetization are given in chapter 3. The new results for the powder susceptibility as well as comparison with other compounds are presented in chapter 4, and discussed in chapter 5 - the conclusion. The current chapter gives the reader the necessary theoretical background needed to understand the models used.

### Theoretical Background

The macroscopic magnetic behavior of the magnetic moment  $M$  depends on the field  $H$  and susceptibility  $\chi$  of the material:

$$M = \chi H \quad (1)$$

The most general equations used to describe the susceptibility are given by the Curie law,  $\chi = C / T$ , and Curie-Weiss law,  $\chi = C / (T - \theta)$ ,<sup>[1,2,3]</sup> where  $C$  is the Curie constant,  $T$  is the temperature and  $\theta$  is a positive constant for ferromagnets, and negative for antiferromagnets.

According to the simplest models, the absolute value of  $\theta$  is almost equal to the critical temperature  $T_c$ , at which long range order is obtained. This, however, is not always true. For example, short range order can cause the ratio  $T_c/\theta$  to be different than one. In some models only short range order exists at temperatures above zero. For

example, the calculation for a linear Heisenberg chain for spin 1/2 yields<sup>[2,6]</sup> the result that the 1D systems do not have a non zero  $T_c$ .

The Curie law and the Curie Weiss law for spin 1/2 systems are shown<sup>[2]</sup> to be the result of an exact calculation which assumes long range order only, and uses the partition function to calculate the magnetization. The microscopic magnetization  $\mu$ , which is the mean z component of the magnetization of an atom is determined<sup>[2]</sup> from the well known statistical mechanics results

$$\bar{\mu}_z = kT \frac{\partial \ln Z}{\partial H} \quad (2)$$

$$Z = \text{trace} \{ e^{\mathcal{H}/kT} \} = \sum_i e^{\epsilon_i/kT},$$

where  $k$  is the Boltzman constant,  $Z$  is the partition function,<sup>[3,8]</sup>  $\mathcal{H}$  is the Hamiltonian and  $\epsilon_i$  are the energy levels accessible to the atom.

If  $M_z$  is the average macroscopic magnetization per mole in the z direction, then

$$\bar{M}_z = N_0 \bar{\mu}_z, \quad (3)$$

where  $N_0$  is avogadro's number. From equations (1), (2) and (3) we get

$$\chi = \frac{N_0 kT}{H} \frac{\partial \ln Z}{\partial H} \quad (4)$$

The difference between the Curie law and the Curie Weiss law comes from the difference in the Hamiltonians used. For the Curie law, only the Zeeman term is taken

into account, and the following Hamiltonian is used

$$\mathcal{H} = -g \mu_B S_{jz} H_z, \quad (5)$$

where  $\mu_B$  is the Bohr magneton,  $S$  is the spin of the electron of the  $j$  atom and  $g$  is the Lande factor.

For the calculation of the Curie Weiss law an additional term is used in the Hamiltonian, based on the assumption that a perturbation in the form of an additional internal field  $H'$  is added to the external field. This perturbation can be caused by the presence of an exchange interaction.<sup>[3]</sup> The additional term in the Hamiltonian is written as

$$-g\mu S_{jz}H' = -2JS_{jz} \sum_{k=1}^n S_{kz}, \quad (6)$$

where  $n$  is the number of nearest interacting neighbors of the atom,  $J$  is the exchange parameter and  $H'$  is the molecular exchange field.

By using the new Hamiltonian, the following result is obtained<sup>[3]</sup>

$$\chi = \frac{N_0 g^2 \mu^2 j(j+1)}{3k(T-\theta)} = \frac{C}{(T-\theta)}, \quad (7)$$

where  $j$  is the sum of the quantum number of the spin and the orbital angular momentum of the atom.

The exchange interaction isn't always direct. There are compounds in which it occurs through a bridging ion.<sup>[2]</sup> The absolute value of the exchange parameter  $J$ , depends on the overlap of the electron orbitals. When the value of  $J$  is positive, the spins tend to

align parallel to one another and the sample has a ferromagnetic exchange. When the value of  $J$  is negative the spins favor an anti-parallel configuration.<sup>[1]</sup>

The exchange interaction is used in many models. In our case it is represented by the Heisenberg Hamiltonian

$$\mathcal{H} = -2J \sum_{ij} (S_{ix} S_{jx} + S_{iy} S_{jy} + S_{iz} S_{jz}). \quad (8)$$

This Hamiltonian is used when there is no preferred direction present, and thus the local spin operators don't commute with the Hamiltonian.<sup>[4]</sup> The Heisenberg model does not assume any restriction on the spin orientations. Copper, which is used in this work, offers a good example of a Heisenberg system.<sup>[2]</sup>

The sources for the magnetic moment demonstrated by the sample are the following<sup>[1]</sup>:

1. Spin
2. Orbital angular momentum about the nucleus
3. A change in the orbital moment induced by an applied field.

In our case, the first is the most important, since the third has been shown to be independent of temperature and field. According to Lenz's law it will result in a diamagnetic effect and yield a negative susceptibility. The second is assumed to be negligible in spite of the fact that the orbital magnetic moment of copper is not zero, for the following reasons:

The Copper (II) ion has nine d electrons outside the argon core. It has  $s=1/2$

configuration, no matter what geometry the ion is placed in.<sup>[2]</sup> The [Ar](3d)<sup>9</sup> configuration has  $j=5/2$  and  $l=2$ . Therefore spin orbit coupling should be important in Cu(II) ions. When the 3d shell is more than half full <sup>[1]</sup> the  $g$  values should be greater than two.<sup>[2]</sup>

Since the effective Bohr magneton depends on the  $g$  value, theory predicts that it would be large. But when the prediction is checked, a surprising result comes out<sup>[28]</sup>: the effective Bohr magneton for the iron transition group is found to be in poor agreement with the experimental results. For this group, the correct value is obtained by assuming that the orbital momentum is "quenched".<sup>[2]</sup>

Using this assumption, in our case for copper compounds, the atomic magnetic moment, which is written as  $\mu_{\text{eff}} = g [j(j+1)]^{1/2} \mu_B$  with

$$g_j = 1 + \frac{s(s+1) - l(l+1) + j(j+1)}{2j(j+1)}$$

yields

$$\mu_{\text{eff}} = g_j [s(s+1)]^{1/2} \mu_B. \quad (9)$$

Because of the fact that the orbital contribution is largely quenched<sup>[2]</sup> and there is no zero field effect for spin 1/2, the  $g$  value is not large for copper. An example is given by  $g^{\parallel}=2.38$  and  $g^{\perp}=2.06$  for the sample  $\text{K}_2\text{CuCl}_4 \cdot 2\text{H}_2\text{O}$ .<sup>[2]</sup>

In our experiment the powder magnetic susceptibility is measured, thus the measurements refer to the value of the average susceptibility  $\langle \chi \rangle$  only, obtained from<sup>[2]</sup>:

$$\langle \chi \rangle = (\chi^{\parallel} + 2\chi^{\perp})/3, \quad (10)$$

or

$$\langle \chi \rangle = 1/3 (\chi_x + \chi_y + \chi_z). \quad (11)$$

Since the  $g$  value is averaged too, it should be in the range<sup>[2]</sup>  $2 < g < 2.3$ .

To calculate the specific behavior of our crystals, more sophisticated models should be used. The models need to include information pertaining to the ion interaction with the crystal as well as to take into account that further complication that arises from the fact that the intralayer magnetic behavior may or may not be of the same nature of that of the layer.

In our case, the crystal structure is made of two dimensional layers stacked in an eclipsed conformation. A two-dimensional model is used for the determination of the intralayer value of the exchange interaction parameter  $J_{\text{in}}$ , whose value should reveal whether the intralayer behavior is ferromagnetic or antiferromagnetic in its nature. The Baker model<sup>[7]</sup> used to calculate the exchange interaction parameter of the layers, is a high temperature susceptibility series expansion obtained for the spin 1/2 Heisenberg model for a square lattice. In their work Baker, et al.<sup>[7]</sup> add more coefficients to the ones previously obtained by Rushbrooke, et al.<sup>[8]</sup> Their calculations use the Hamiltonians in equations (5) and (8). From these Hamiltonians they calculate the partition function (see equation (2)) and expand it in powers of  $J_{\text{in}}/kT$ . Finally the susceptibility is calculated by

$$\chi = \frac{\partial^2 (N_0 kT \ln Z)}{\partial H^2}. \quad (12)$$

This relation is equivalent to equation (4).<sup>[3]</sup>

Using the final result of their work:

$$\chi T = C \left( 1 + \sum_{n \geq 1}^{10} \frac{a_n}{2^n n!} x^n \right), \quad (13)$$

where

$$C = \frac{N_0 \mu_{eff}^2}{3k} = N_0 g^2 \mu_B^2 \frac{S(S+1)}{3k}$$

and

$$x = \frac{J_{1h}}{kT}$$

and  $a_n$  are:

$$\begin{array}{cccccc} a_1=4 & a_2=16 & a_3=64 & a_4=416 & a_5=4544 \\ a_6=23488 & a_7=(-)207616 & a_8=4205056 & a_9=198295552 & a_{10}=(-)2574439424 \end{array}$$

This formula is used to find the value of the intralayer exchange parameter. However the effect of the interlayer parameter  $J_{2h}$  is still needed to be taken into account. As previously mentioned the exchange interaction can be added in the form of a correction to the external magnetic field, as shown in previous work<sup>[10,11]</sup>

$$M_i = \chi_i (H_i + H'_i). \quad (14)$$

By using the molecular exchange field expression<sup>[2,10]</sup> the susceptibility is

calculated

$$H'_i = \frac{2ZJ}{N_0 g_i^2 \mu_B^2} \chi'_i H_i, \quad (15)$$

where  $H'_i$  is the molecular exchange field,  $H_i$  is the external field,  $\chi_i$  is the zero perturbation order susceptibility and  $\chi'_i$  is the exchange corrected susceptibility actually measured. From equations (14) and (15)

$$\chi'_i = \lim_{H_i \rightarrow 0} \frac{M_i}{H_i} = \frac{\chi_i}{1 - (2ZJ_{2h}/g_i^2 \mu_B^2) \chi_i}. \quad (16)$$

Thus by using the experimental results for  $\chi'_i$  once again and the previous zero order calculation for  $\chi_i$ , the interlayer exchange parameter  $J_{2h}$  is obtained.

## CHAPTER 2

### SAMPLE STRUCTURE AND PREPARATION

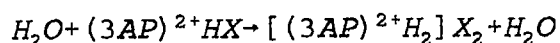
The magnetic behavior of the perovskite salts samples cannot be well understood without looking at their structures. At the beginning of this chapter the crystal growth technique is described. The second part of the chapter contains information pertaining to the structure of the samples and it's correlation to the values of the exchange parameters.

#### Sample Preparation

The crystals were prepared by evaporation of concentrated HX solution that contained  $\text{CuX}_2:(3\text{AP})$  with ratio somewhat greater than one, where X stands for either Cl or Br.<sup>[1]</sup> In order to avoid competing reactions and the formation of the compound  $(3\text{AP})_2\text{Cu}_2\text{X}_6$  the strength of the acid solutions was required to be greater than 1M.<sup>[1,2]</sup>

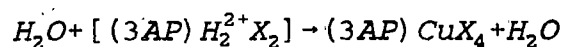
To grow the samples we performed the following steps:

1. HX in  $\text{H}_2\text{O}$  solution was slowly added to (3AP), allowing the reaction heat from



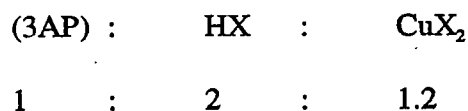
to escape.

2. H<sub>2</sub>O was added drop by drop to the CuX<sub>2</sub>, until a uniform solution was formed. (No more H<sub>2</sub>O was used than the minimum required in order to dissolve the CuX<sub>2</sub>.)



After the solutions were mixed together, the crystals formed slowly by evaporation, and when ready they were washed with EtOh, and left to dry.

The following ratios were used to calculate the appropriate amounts needed for the above process:



Because of the requirement for high acidity we used a concentration of approximately 6M HCl in H<sub>2</sub>O, and approximately 7M HBr in H<sub>2</sub>O. After two days of slow evaporation the crystals formed as green flat plates for the chloride salts, and dark opaque plates for the bromide salts.

In order to avoid large background signals the sample holder was prepared from teflon, which has a very small magnetic permeability. It was treated in the following ways:

1. Washed with soap, distilled water, 50% methanol and 50% acetone mixture.
2. Pickled ultrasonically with 10% nitric acid solution inside an ultrasonic device.

### Crystal Structure

The salts consist of two dimensional perovskite type  $(\text{CuX}_4)_n$  layers, interleaved by the organic cations  $(3\text{AP})^{2+}$ .<sup>[1]</sup> The 3-aminopyridine cations bridge between layers with the ammonium group  $\text{NH}_3$  and the pyridinium  $\text{NH}^+$  group hydrogen bonding to adjacent layers. The  $\text{NH}^+$  group forms  $\text{N-H}\cdots\text{X}$  hydrogen bonds with  $\text{CuX}_4^{2-}$ . The three hydrogen atoms of the ammonium group ( $\text{NH}_3$ ) each form a hydrogen bond, one to a bridging halide ion and two to non bridging halide ions.<sup>[1]</sup>

To understand the interlayer structure and how it relates to the magnetic behavior of the samples we need to use the following information: The ability of the  $\text{Cu}\cdots\text{X}$  distance to vary over a large range makes it possible to change the size of the cation used, and to vary the magnetic properties systematically. The (3AP) cation is used in our work. Considering the stacking of the layers it is found<sup>[1]</sup> that the relatively small size of the 3-aminopyridine plays an important role in term of the stacking of adjacent layers. It leads to short interlayer halogen-halogen distances. Thus short  $\text{X}\cdots\text{X}$  contacts are created between the layers which are referred to as interlayer distances —  $3.992\text{\AA}$  for  $\text{X}=\text{Cl}$  and  $3.889\text{\AA}$  for  $\text{X}=\text{Br}$ .

The value of  $J_{2h}$ , the interlayer exchange parameter depends on the  $\text{X}\cdots\text{X}$  bond length (2h stands for the two halides in the linkage  $\text{Cu-X}\cdots\text{X-Cu}$  between the layers).  $J_{2h}$  is expected to decrease when the bond length increases, since the differential overlap between the two magnetic ions depends on it. This trend is experimentally demonstrated for a series similar to the one we use — the  $n\text{DACuX}_4$  series, in which n varies from 2

to 5.<sup>[1]</sup>

The layers are found to be stacked in an eclipsed conformation, as seen in Figure 1 in which the linkage between layers was demonstrated.

From the crystal structure it is concluded<sup>[1]</sup> that  $J_{2h}$  depends on:

1.  $X \cdots X$ , the contact distance between layers. ( $J_{2h}$  gets bigger when  $X \cdots X$  gets smaller.)
2. The angle  $Cu-X \cdots X$ .  $J_{2h}$  gets bigger when this angle is closer to  $180^\circ$ .
3. The  $Cu-X$  distance of the interlayer linkage  $Cu-X \cdots X-Cu$ .  $J_{2h}$  gets bigger when the  $Cu-X$  distance gets smaller.

The next step is to try and understand the intralayer structure, and how it relates to the magnetic behavior of the sample. Once again, we need to use the information given in reference [1]. It is found that the layers consist of  $(CuX_4^{2-})_n$  arrays. The arrays are found to be approximately two dimensional, since although the anions are found to be tetrahedrally distorted the bridging angle  $Cu-X \cdots Cu$  is only  $161.2^\circ$  for chloride and  $157.6^\circ$  for bromide. The two dimensional structure is non centrosymmetric, as seen in Figure 2 and Figure 3. The chloride  $Cu-X$  distance is  $2.28\text{\AA}$ , and the semicoordinate bond  $Cu \cdots X$  is of the order of  $3.25\text{\AA}$ . The bromide  $Cu-X$  distance is found to be  $2.428\text{\AA}$  and the  $Cu \cdots X$  distance is of the order of  $3.35\text{\AA}$ .

Since the absolute value of  $J_{1h}$  depends on the extent of the differential overlap between the two magnetic orbitals, it is assumed<sup>[1]</sup> that there should be a strong

dependence on the  $\text{Cu}\cdots\text{X}$  bond length.  $J_{1h}$  is expected to decrease when the bond length increases, although variations in the coordinate  $\text{Cu-X}$  influence the  $J_{1h}$  absolute value as well. The differential overlap depends on the  $\text{Cu}\cdots\text{X}$  bond for another reason: it affects the tetragonality of the  $(\text{CuX}_4^{2-})$  groups.

Experimental results for  $J_{1h}$  for compounds containing bromine reveals that its value is 50% - 100% larger than for those containing chlorine.<sup>[1]</sup> Bromine, being more polarizable than chlorine, frequently allows larger superexchange interaction. However bromine is also a larger ion, and hence separates the metal ions further apart.<sup>[3]</sup>

A summary and additional data pertaining to these compounds (obtained from the literature) is listed in Table 1.

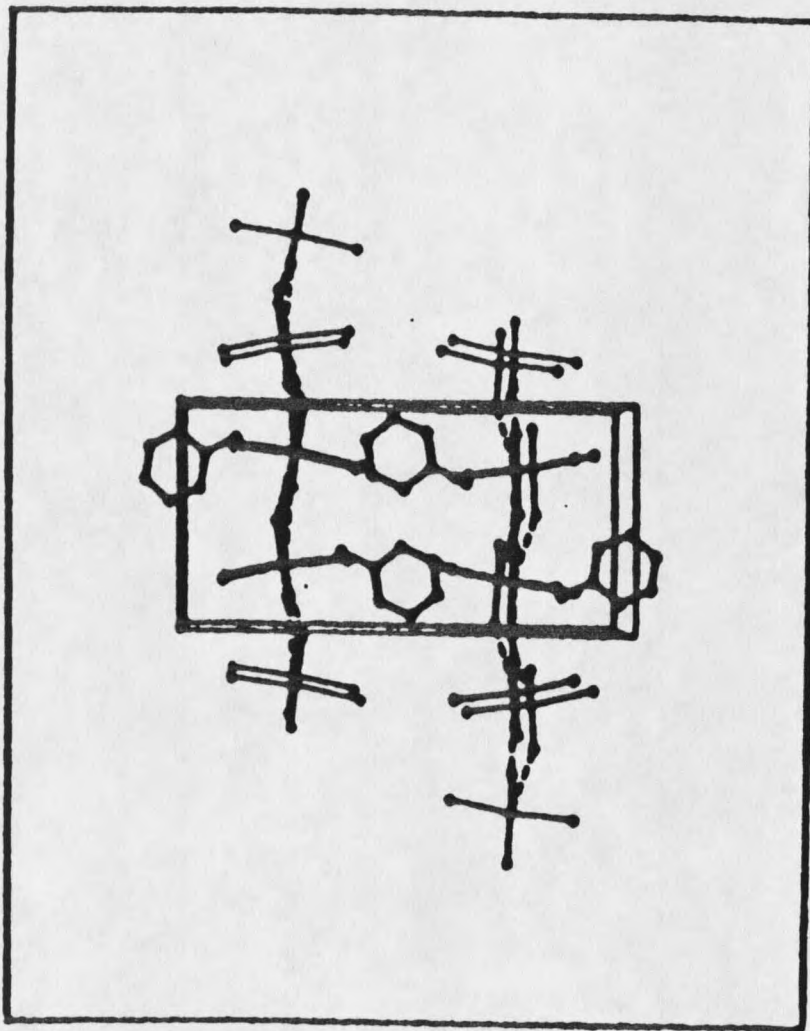


Figure 1 A side look at the layers reveals the eclipsed structure and shows how the layers are linked. The  $c$  axis of the monoclinic crystal is horizontal and the  $b$  axis is vertical.

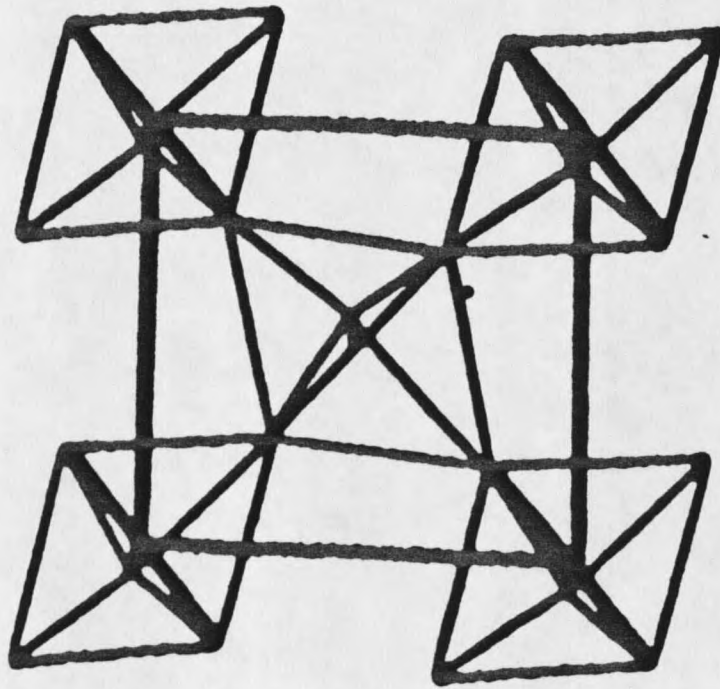


Figure 2 A look at the two dimensional noncentrosymmetric structure of the layer.<sup>11</sup>

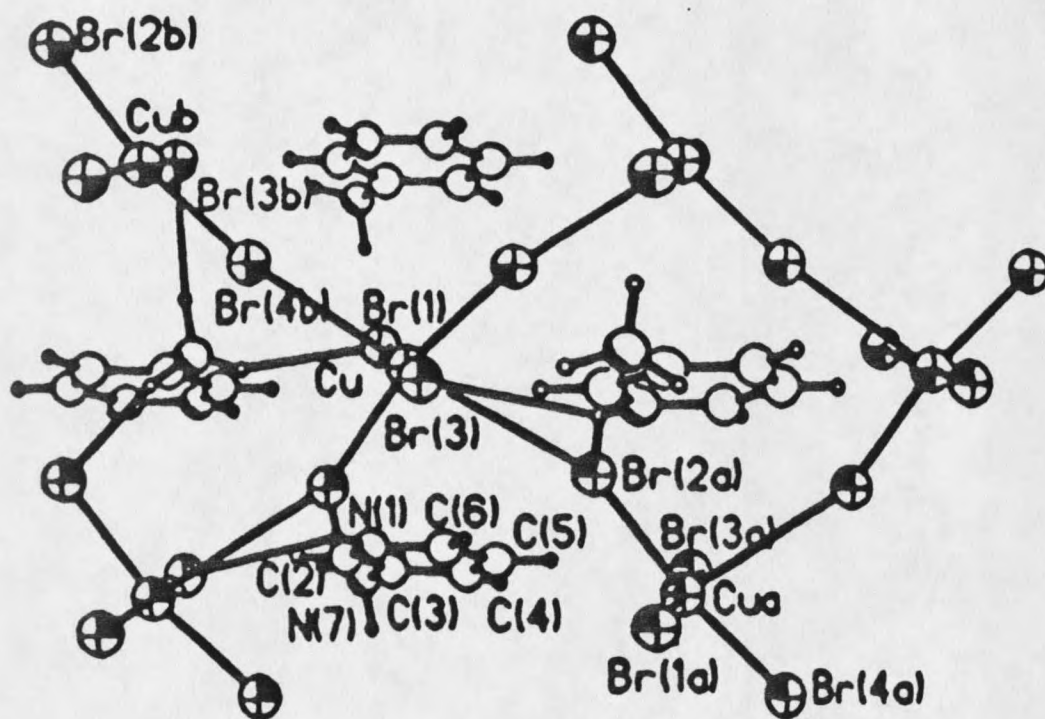


Figure 3 A look at the atomic structure of the layer.<sup>[1]</sup> The b axis of the monoclinic crystal is horizontal and the a axis is vertical. Each Cu atom has 4 Cu neighbors inside the layer, bridged by one X halide, and 2 Cu neighbors from adjacent layers, bridged by 2 X halides.

Table 1 Structural information of (3AP)CuBr<sub>4</sub> and (3AP)CuCl<sub>4</sub>.

(3AP)CuX <sub>4</sub> compounds:		
	X=chloride	X=bromide
Crystal parameters:		
Cu—X···X bridging angle (in the layer)	161.2	157.6
X—Cu—X trans angle (out of the layer)	170.56	170.6
Cu—X···X angle	163.5	165.3
X···X distance	3.992Å	3.899Å
bond distance Cu—X	2.28Å	2.428Å
semicoordinate bond distance Cu···X	3.183;3.339Å	3.266;3.478Å
monoclinic crystal parameters		
a:b (layer parameters)	6.941;8.384Å	7.179;8.766Å
c:	16.848Å	17.218Å
monoclinic crystal angle	94.63	95.29
g <sup>  </sup>	2.160	Unknown
g <sup>⊥</sup>	2.052	Unknown

## CHAPTER 3

### EXPERIMENTAL INFORMATION

In any experiment the stability, repeatability and calibration of the system are crucial because they determine the accuracy of the measurements. Possible sources for errors as well as the steps taken to minimize them are described in this chapter.

To measure the powder susceptibility of the samples a Vibrating Sample Magnetometer (V.S.M) model 155 was used. The following preliminary operational steps were taken:

1. Electronic checks, noise checks and overload checks were performed according to the instructions of the operating and service manual. The performance was good.
2. The signal stability was checked and the system accuracy was estimated by looking at the data that was obtained at constant temperature over time periods of the order of those required for a normal measurement (the results are discussed later in the chapter).

3. Efficiency checks were made by looking at the helium consumption and the time needed to complete measurements of the full temperature range. Helium consumption estimates for various flow rates were tabulated during each experiment. The table of flow rates and temperature variations which was made according to the data was used to find out how to get maximum results from the system at minimum time and helium consumption. Thus a way to operate the system efficiently was found and will be discussed later in this chapter.
4. Calibration was made by using nickel and  $\text{HgCoSCN}_4$  samples. See results at the end of this chapter.

General estimates of the system stability at the VSM interface magnetic moment scales 0.01, 0.1 and 1 for large and small signals at both ends of the temperature range gave the following results:

An empty system would give fluctuations of the order of  $\pm 0.00004$  emu\*Oe at room temperature. This is the minimal error expected from the system. Since most of the samples have a small signal at room temperature, the percent error rises when measurements are made at that temperature. The  $(3\text{AP})\text{CuX}_4$  samples, for example, have signals of the order of 0.002 at room temperature. These fluctuations would result in large errors of magnitude  $\pm 2\%$ .

The percent error due to background fluctuations is  $\pm 3\%$  for the teflon sample holder at 294K. The order of magnitude of the fluctuations in teflon background is 0.0006

emu\*Oe at room temperature, which is 30% of the fluctuating signal. These results indicate that the room temperature measurements would be extremely difficult to interpret. The signal for teflon at low temperature is larger, of the order of 0.01, and so the percent error reduces to  $\pm 0.8\%$ . That, and the fact that this signal is 1% of the 3APCuX<sub>4</sub> signal make it possible to obtain better results for the low temperature range.

For the nickel sample, which is used for the calibration and is measured on the 1 scale, the fluctuations are  $\pm 0.1\%$  emu\*Oe at room temperature. Another reason for inaccuracy in the calibration with nickel is the fact we only calibrate with an accuracy of  $\pm 0.01$  emu\*Oe. This inaccuracy should be negligible for large signals, but may not be negligible for extremely small signals. The day to day repeatability was checked as well during the calibration and showed variations of  $\pm 0.35\%$  for nickel.

Other parameters which can influence the accuracy of the measurements are:

1. The instability in the flow rate of helium can cause fluctuations in the temperature. At 4.2 K, where the flow should be the steadiest, because the needle valve which leads helium to the sample is open wide, the magnetic moment of nickel has shown fluctuations of the order of 0.04 emu\*Oe corresponding to 0.5% error. At the 10-20K range the stabilizing of the system at a single temperature over a long period of time is extremely difficult, resulting in an inaccuracy of  $\pm 1\%$  in the signal for a 0.01 scale.
2. If the sample is placed inside the teflon sample holder the magnetic field will be

reduced by 0.2% because of shielding. The magnetic field demonstrated instability of the order of 5 oe. The accuracy of the magnetic field probe was checked by measuring the field of a well known permanent magnet, and was found to be  $\pm 0.01\%$ .

3. The relative position between the sample and the pickup coils: The size of the detecting coils limits the size of the sample that these coils can detect with a constant response. For the nickel sphere the signal was at a constant peak for a motion of 0.1 cm up or down with respect to the pick up coils. If the motion continues the signal changed by 0.2%. It remains constant for additional 2.5 cm relocation in each direction. Therefore 0.5 cm is the maximal recommended size for the sample, yielding a 0.2% error. The XYZ alignment which positions the sample with respect to the pick up coils is extremely important. Its repeatability must be checked, since it has its own mechanical limitations. Upon taking the nickel sample out and inserting it back in a  $\pm 0.4\%$  change in the signal was observed.

The response of the rod which holds the sample to cooling and heating could lead to small differences in the geometry and change the signal picked by the pickup coils.

4. The temperature detector and the sample are not located at exactly the same place, and the response of the sample to the flow changes may be different from the response of the detector, depending on the heat capacity of both. This can cause

hysteresis: The cooling curves look different than the heating curves. For example, if the response of the detector is faster than the response of the sample, the temperature readings of the heating curve will be too high, thus shifting the whole curve towards higher temperatures, and that of the cooling curve too low, thus shifting the curve towards lower temperatures. However, the situation may not be so simple, as the heat capacity varies with different temperatures, especially at the phase transition range. For the (3AP)CuBr<sub>4</sub> sample, variations between cooling and heating as large as 8% are observed theoretical reasons as well. To minimize this effect cooling as well as heating measurements were done. Since heating and cooling play an important role in the measurements these results were interpreted separately and compared.

The response of the system to cooling and heating as a function of the helium flow rates was made. The interested reader will find the necessary information needed to the V.S.M user to plan and estimate the time and helium consumption needed for the measurements. For a given flow, the rate of change of temperature with time,  $\partial T/\partial t$  varies with the temperature. This affects the helium consumption needed to complete the measurement at that range. A higher flow consumes more helium, but also covers the temperature range faster so that overall the efficiency may be better. The efficiency is represented by  $(\partial \text{He}/\partial T)$ , the helium consumed to cover temperature interval of 1K.

The user must also consider that flow rates that are too high result in large

temperature variations, which may be too fast for a particular sample. The signal stability must be obtained to achieve good data. Each sample has its own response and the appropriate method should be determined individually. However the system response can be well predicted by use of the Tables 2, 3.

Table 2 Helium consumption in %, and temperature variation in degrees Kelvin /min as a function of helium flow rates in cc/min. The flow numbers could change if the V.S.M. top is sealed in a different way than it did when this table was made. This table is for cooling.

20-40K		40-70K		70-100K		100-200K		200-300K	
$\partial T/\partial t$	$\partial He/\partial t$	$\partial T/\partial t$	$\partial He/\partial t$	$\partial T/\partial t$	$\partial He/\partial t$	$\partial T/\partial t$	$\partial He/\partial t$	$\partial T/\partial t$	$\partial He/\partial t$
Flow Rates cc/min									
200	No cooling	No cooling		No Cooling		No cooling		2.4	0.2%
300	"	"		"		2.5	0.1%		
400	"	"		3	0.07%	6.0	0.03%		
500	"	1.3	3.5%	4	0.05%	9.0		8.0	1.0%
600	"	4.5	0.15%	5.5	0%				
700	6	0%	7	0%					
800	6.5	0.6%	8	0.2%					
900	7	0.2%	10	0.5%	9	0.5%			
1000	7.5	0.1%							

$\partial T/\partial t$  is measured in Kelvin per minute  
 $\partial He/\partial T$  is measured in percent per Kelvin

Table 3 Helium consumption in %, and temperature variation in degrees Kelvin /min as a function of helium flow rates in cc/min. The flow numbers could change if the V.S.M. top is sealed in a different way than it did when this table was made. This table is for heating.

Flow Rates cc/min	20-40K		40-70K		70-110K		110-170K		170-250K		250-300K	
	$\partial T/\partial t$	$\partial He/\partial t$	$\partial T/\partial t$	$\partial He/\partial t$	$\partial T/\partial t$	$\partial He/\partial t$	$\partial T/\partial t$	$\partial He/\partial t$	$\partial T/\partial t$	$\partial He/\partial t$	$\partial T/\partial t$	$\partial He/\partial t$
	He(cc/min)											
0			4		2		1-0.5	0.4%	No heating			
100			3		1.5	0.1%	No heating		"			
200			2		No heating		"		"			
300			1		"		"		"			
400	10	0.2%	1		"		"		"			
500	8		0.5		"		"		"			
600		0.6%	No heating		"		"		"			
700	No heating		"		"		"		"			
800	No heating		"		"		"		"			
900	"		"		"		"		"			
1000	"		"		"		"		"			

The following procedure allows the V.S.M user to obtain four files with one helium transfer only. These files can be used to determine the sample response to heating and cooling. By comparing the difference between the files the user can estimate how slowly the measurements should be done.

1. A cooling file which covers the full temperature range is obtained by cooling slowly at:

200 cc/min for the range 300-200K

then 350 cc/min for the range 200-80K,

then 450cc/min for the range 80-40K,

and finally the flow is gradually changed by hand to cover the 20-4.2K range. This took 1 3/4 hour and consumed 50% of the helium.

2. A heating file for the range 4.2-130K is obtained by:

A gradual change of the flow rate to cover the 4-40K range

then 300 cc/min to cover the 40-60K range

then 100cc/min to cover the 60-130K range.

3. A cooling file which is done quickly, and gives some information about how fast the sample can respond to changes in temperature (by comparing to the slow cooling curve obtained at the first step).

600 cc/min for the range 130-20K.

The flow is changed as necessary to cover the 20-4 K range. The previous two steps consume 42% of the helium, and only 8% helium is left. They take 1/2 an hour.

4. A heating file which is done at the rate necessary to cover the range 4-40, by gradual change of the flow.

Then 150 cc/min is used to cover the 40-70 range, which consumed all of the helium that is left. Once the helium is finished, the system slowly heats up to cover the full temperature range left. This step takes 2 1/2 hours. Careful attention should be taken not to use up all the helium before the 70K temperature is obtained. If, for example, the helium level drops to zero before that the system temperature can instantaneously skip from 20K to 70K.

To calibrate the system, a pure nickel sphere sample was used. The one point calibration value required for the calibration knob was determined at room temperature according to the formula:<sup>[2]</sup>

$$M=w*54.95[1-12/H][1-0.0003(298-T)],$$

where w is the mass of the sample in gm, H is the magnetic field in Oe and T is the temperature, which is the room temperature and is close to 298K. M is the magnetization in emu\*Oe.

Since the theoretical value accuracy is 0.4%<sup>[2]</sup>, a signal of 3.51 emu\*Oe would have an error of  $\pm 0.014$  emu\*Oe.

The system was then checked at 4.2K, for which the magnetic moment for nickel was calculated according to the value<sup>[2]</sup>

$$M=58.19*w=3.7357 \text{ emu*Oe.}$$

Since the system gave a value that was different by 0.1 emu \*Oe from the

expected value; the calibration was repeated this time at low temperature, and the value at room temperature was checked again. At room temperature, the magnetization value showed an error of the order of  $0.1 \text{ emu} \cdot \text{Oe}$ . Repeating the calibration a few times at low and high temperatures confirmed that a 2.8% discrepancy was present over the full temperature range. Therefore the full range was checked by another sample.

The full temperature range was measured for the sample  $(\text{HgCo}(\text{NCS})_4)$ -whose magnetic behavior is well known.<sup>[1]</sup> The inverse susceptibility vs. temperature plot for this sample should give a linear relation as shown in figure 4. This linear relation was indeed obtained by the Vibrating Sample Magnetometer at the temperature range 4-140K. Therefore this range was chosen for measurements of the new unknown samples.

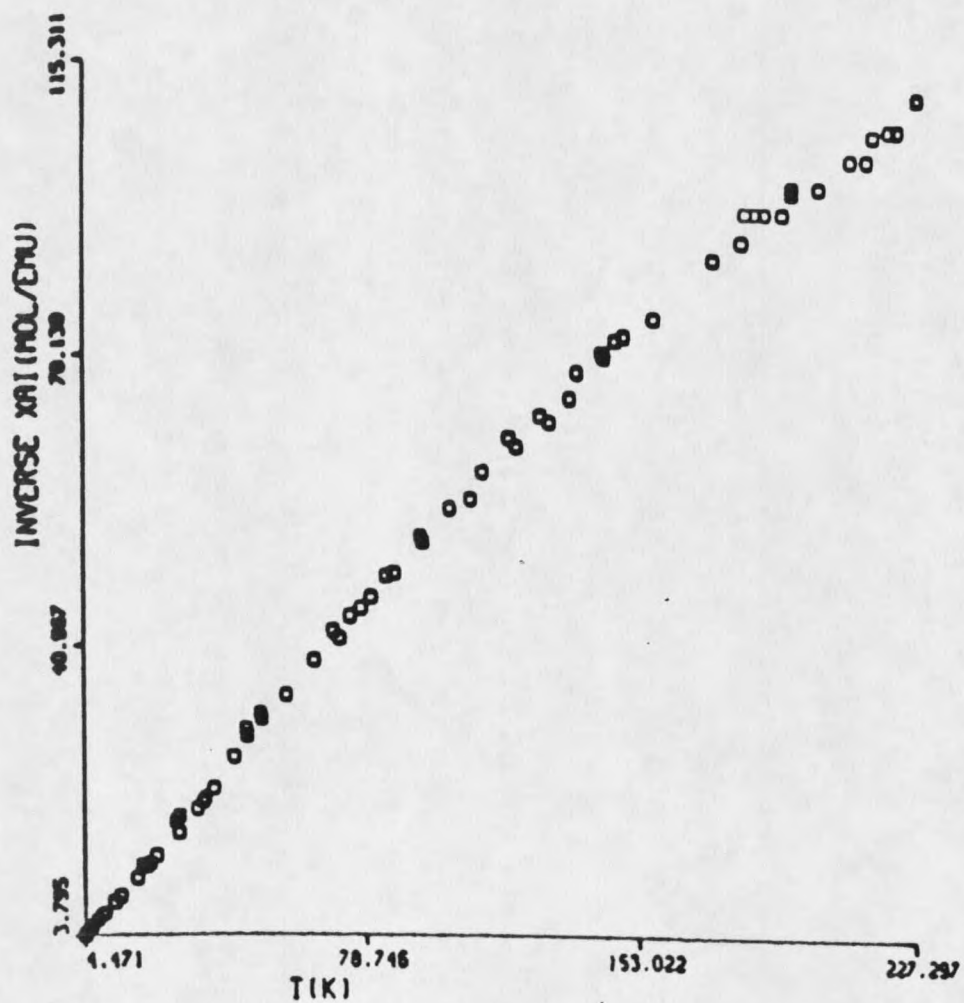


Figure 4 The inverse susceptibility vs. temperature for  $\text{HgCo}(\text{SCN})_4$ . The curve was repeatable at the range 4.2-150K. This range was chosen for future measurements of unknown samples.

## CHAPTER 4

## EXPERIMENTAL RESULTS

The new results for the magnetization of  $(3AP)CuBr_4$  and  $(3AP)CuCl_4$  which were measured at the temperature range of 4.2-150K and magnetic field of 6000 Oe, are presented in Fig 5 and Fig 6. Notice the deviation from the Curie law and the Curie Weiss law at temperatures lower than 13K. This deviation is even more obvious when looking at the curves of the inverse susceptibility versus the temperature which are presented in Fig 7 and Fig 8.

The Baker model was used to fit the data by means of a SAS statistical program on the VAX network. The fits are shown in Fig 9 and 10. In order to check the repeatability of the results, the fit was done separately for each file. Only files for which the convergence criterion was met were taken into account, and boundary statements were not used to limit the values of  $g$ ,  $J_{1h}$  or  $J_{2h}$ . Since both cooling and heating files were checked for each sample, upper and lower values were obtained. Those gave error values that were greater than the statistical errors given by the computer program for each individual file. Different temperature intervals were checked and compared as well.

The new values obtained for  $J_{1h}/k$  and  $J_{2h}/k$  are presented in Table 4.  $J_{1h/k}$  is found

to be bigger for the bromide salts than for the chloride salts, as expected.

Both salts demonstrate an antiferromagnetic exchange between the layers and a ferromagnetic exchange within the layer. The antiferromagnetic exchange is dominant, since the absolute value of the interlayer exchange parameter  $J_{2n}/k$  is greater than  $J_{1n}/k$ .

The new results which are presented in Table 4 can be compared with the ones reported in previous work for similar crystals.<sup>[1,4]</sup> The graph of  $J_{1n}/k$  values vs. the  $\text{Cu}\cdots\text{X}$  is repeated in Fig 11, Fig 12 for  $\text{X}=\text{Cl}$  and  $\text{X}=\text{Br}$ , adding the new values of  $J_{1n}/k$  obtained for  $(3\text{AP})\text{CuX}_4$  compounds. From the graph, the assumptions that the  $J_{1n}/k$  values of  $(3\text{AP})\text{CuBr}_4$  and  $(3\text{AP})\text{CuCl}_4$  would be strongly dependent upon the  $\text{Cu}\cdots\text{X}$  contact distance is confirmed.

The graphs of  $\log J_{2n}/k$  values vs.  $\log \text{X}\cdots\text{X}$  for  $(n\text{DA})\text{CuX}_4$  series<sup>[2]</sup> are repeated in Fig 13 and Fig 14. This graph gives linear relation for the  $(n\text{DA})\text{CuX}_4$  series.<sup>[1]</sup> It shows that the  $J_{2n}/k$  value depends on the  $\text{Cu}\cdots\text{X}$  distance for the  $(3\text{AP})\text{CuX}_4$  salts.

The new values reported in this work for the non-centrosymmetric salts are somewhat different from those predicted. Predictions made by Willett et al.<sup>[1]</sup> are given in Table 5. The graphs, however, show that our results agree with previous work.

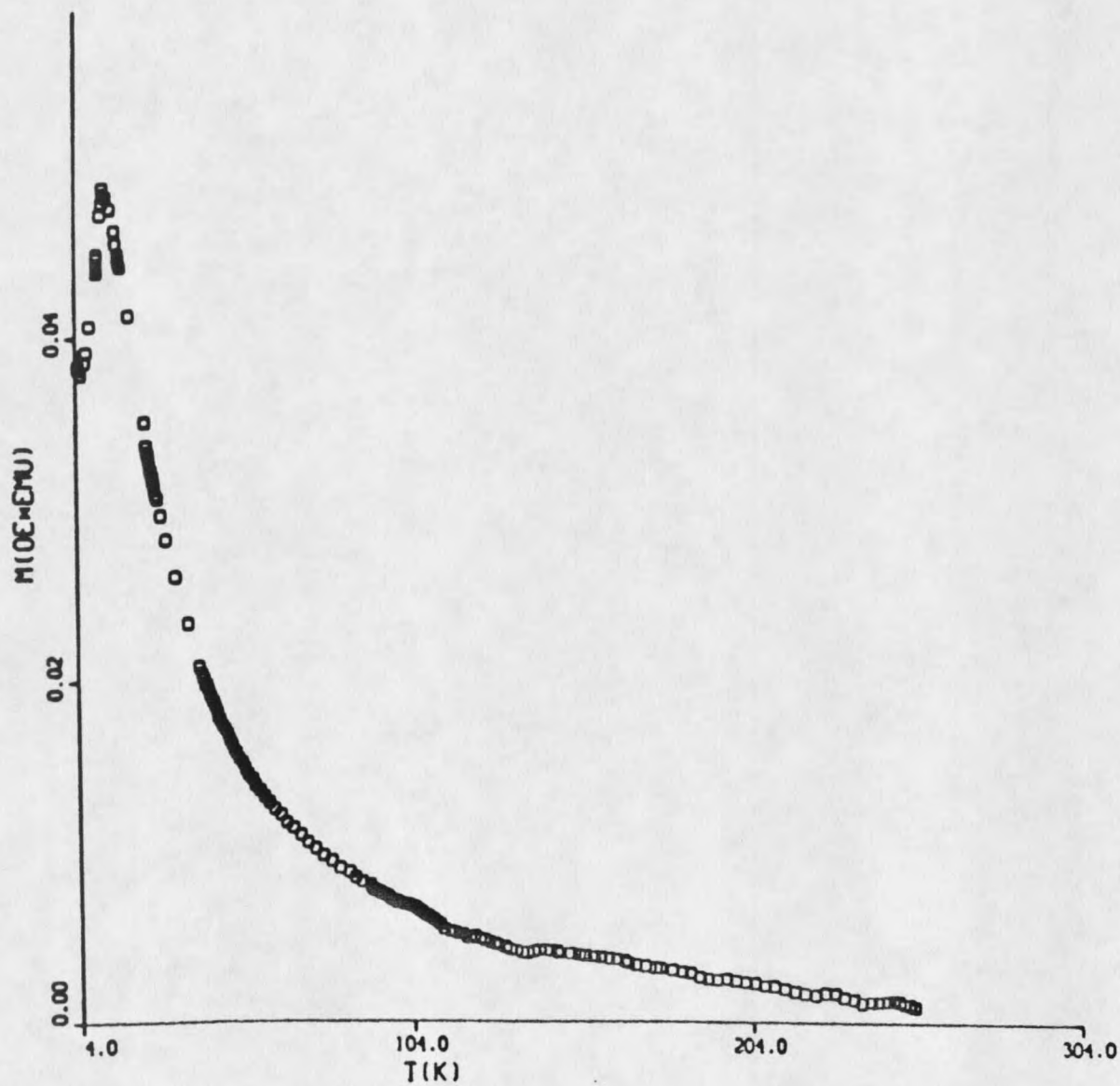


Figure 5 The magnetization vs. temperature of  $(3AP)CuBr_4$ .

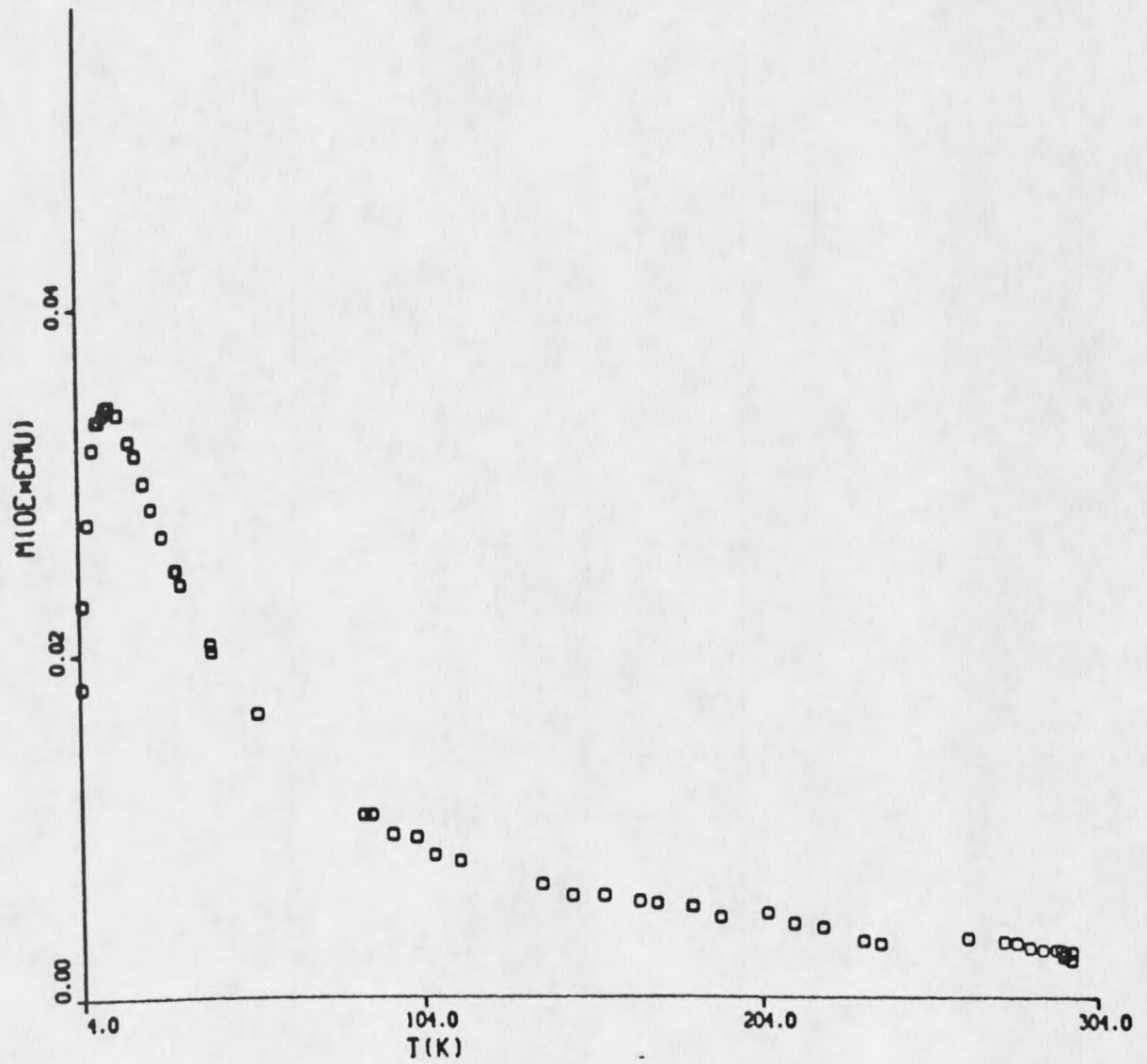


Figure 6 The magnetization vs. temperature of  $(3\text{AP})\text{CuCl}_4$ .

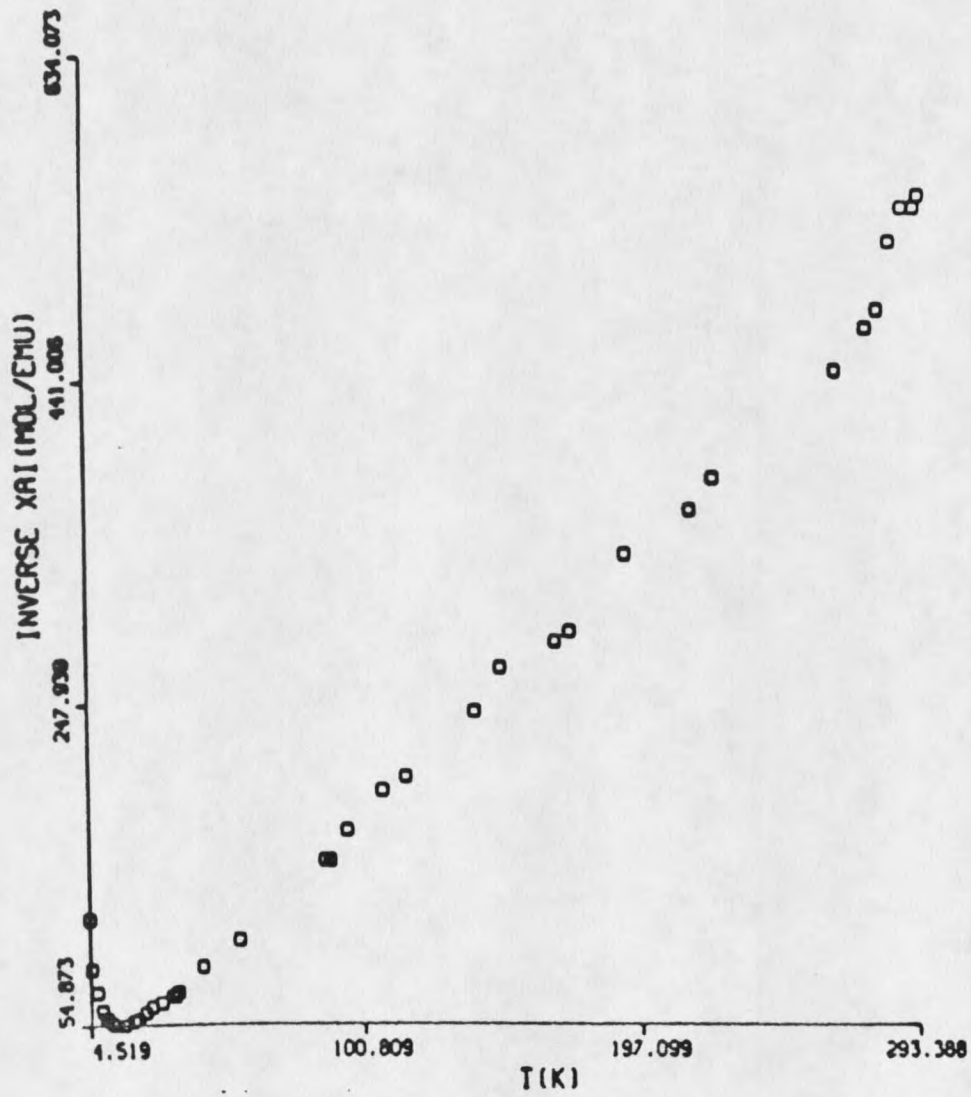


Figure 7 The inverse susceptibility vs. temperature for (3AP)CuBr<sub>4</sub>.

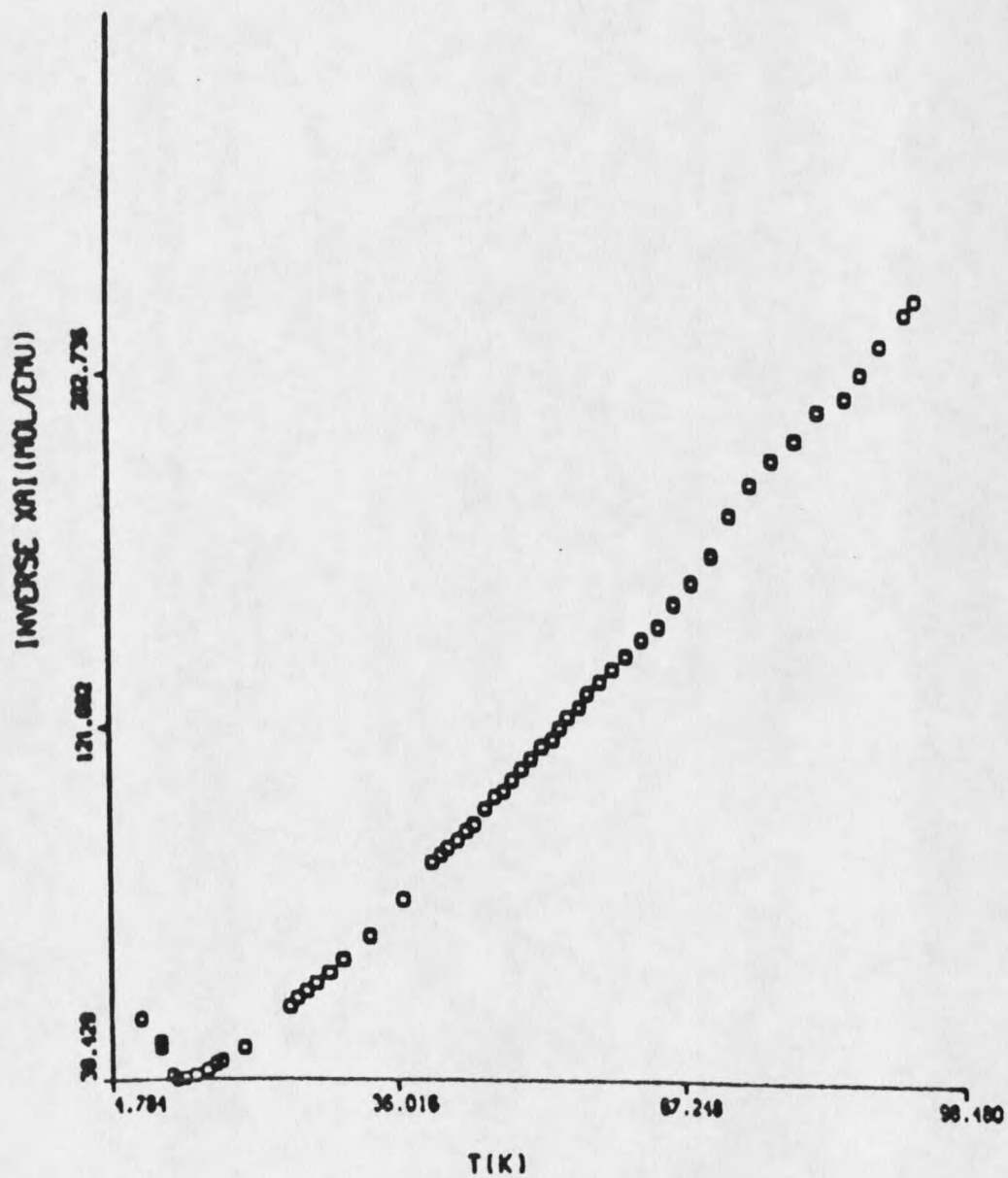


Figure 8 The inverse susceptibility vs. temperature for  $(3AP)CuCl_4$ .

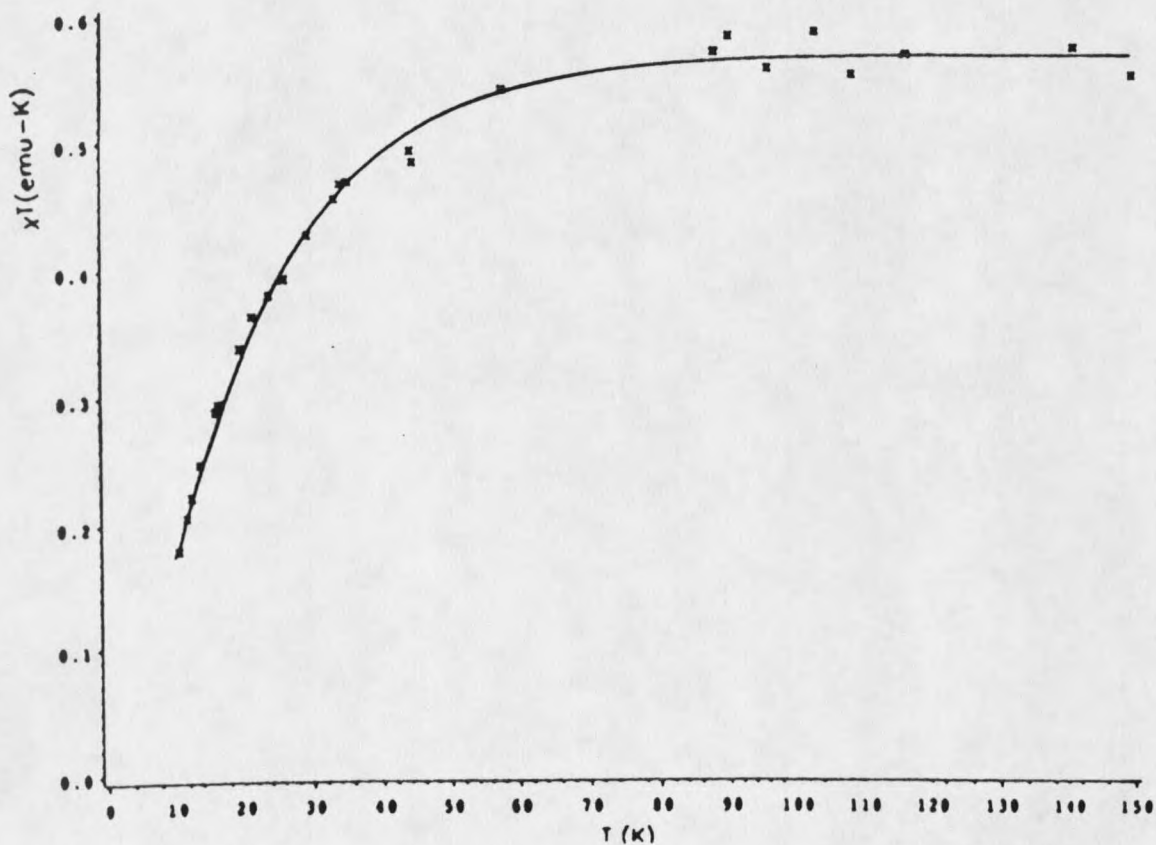


Figure 9 Fit of the data of  $(3AP)CuBr_4$ , created by SAS statistical program on the VAX network. The experimental data points are marked in x and the model calculated for the optimal values is marked as a solid line.

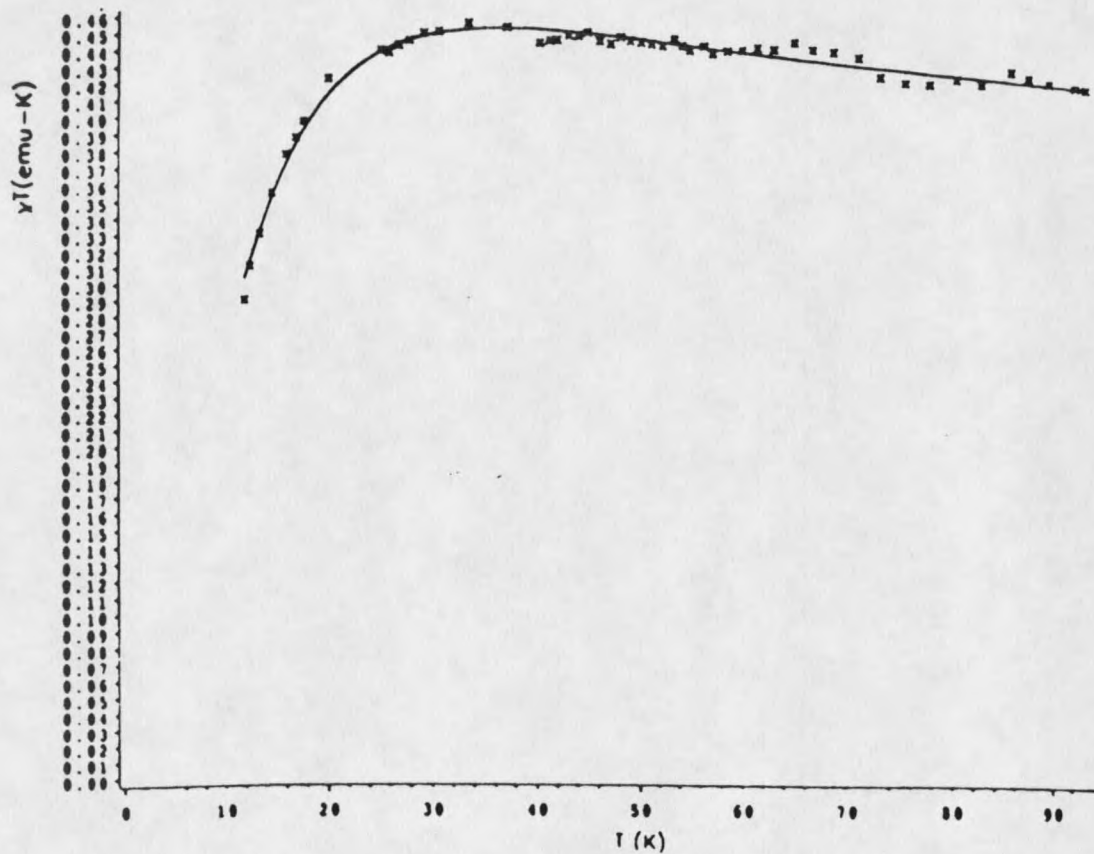


Figure 10 Fit of the data of  $(3AP)CuCl_4$ , created by SAS statistical program on the VAX network. The experimental data points are marked in x and the model calculated for the optimal values is marked as a solid line.

Table 4 New results for the values of the exchange parameters and the g constant for the compounds (3AP)CuBr<sub>4</sub> and (3AP)CuCl<sub>4</sub>, obtained by the Vibrating Sample Magnetometer.

	Cl compound	Br compound
J <sub>1h</sub> /k	15 ± 1	20.5 ± 2.5 K
J <sub>2h</sub> /k	-25 ± 1	-57 ± 7 K
g	1.95 ± 0.06	2.28 ± 0.07 K

Table 5 predicted values for the exchange parameters and the g constant from reference<sup>[1]</sup>.

	Cl compound	Br compound
J <sub>1h</sub> /k	8-10	16-18
J <sub>2h</sub> /k	3-4	35-45
g <sup>⊥</sup>	2.052	unknown
g <sup>  </sup>	2.160	"

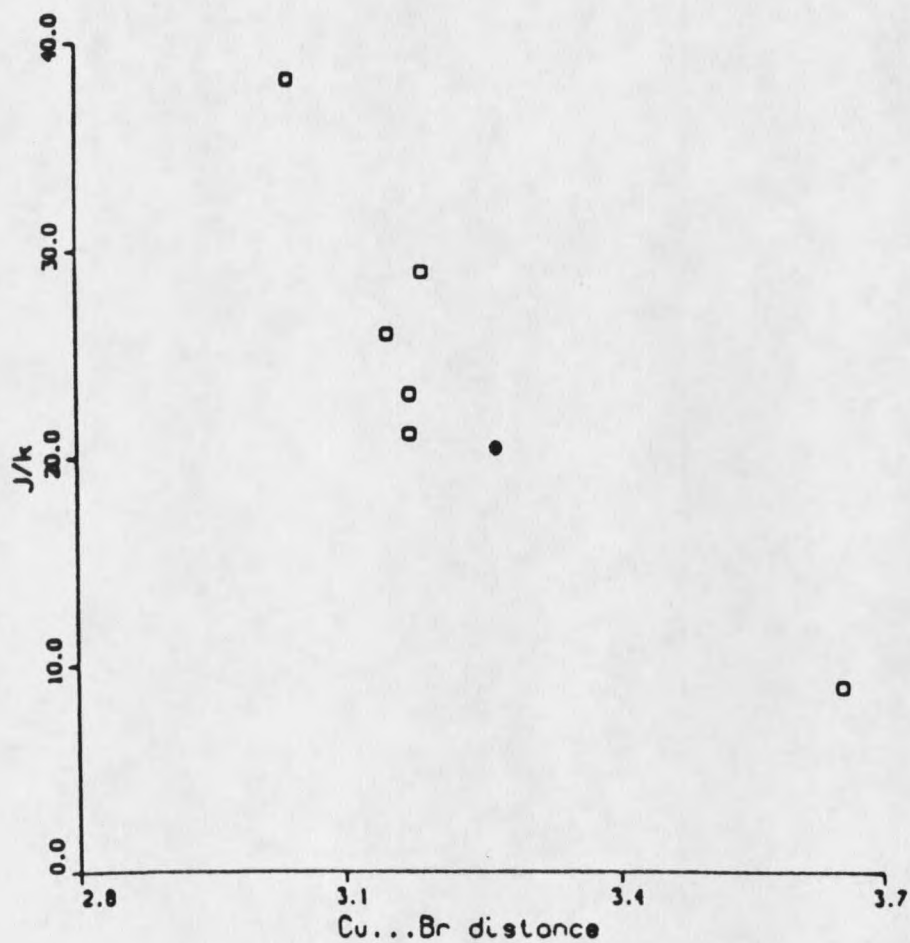


Figure 11  $J_{10}/k$  values vs. Cu...Br measured in Å, of  $A'CuBr_4$  and  $A_2CuBr_4$ . Previous data points are marked as squares, and the new result for the  $(3AP)CuBr_4$  is marked as a full circle.

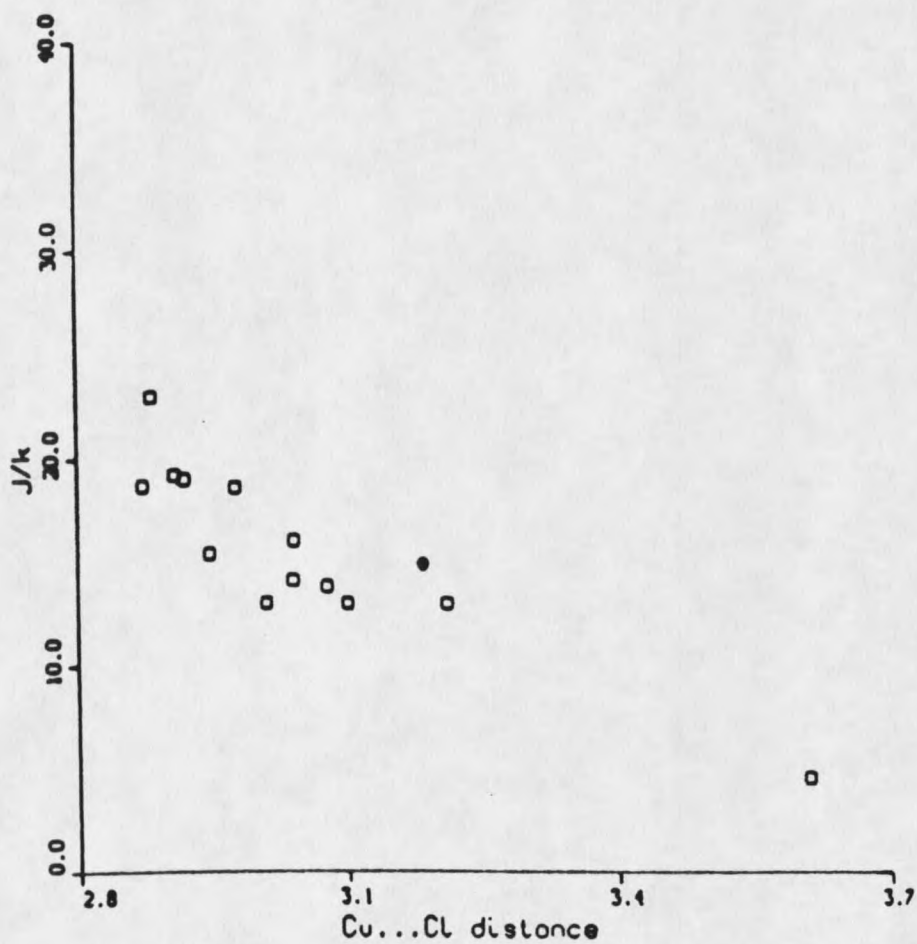


Figure 12  $J_{11}/k$  values vs. Cu...Cl measured in Å, of  $A'CuCl_4$  and  $A_2CuCl_4$ . Previous data points are marked as squares, and the new result for the  $(3AP)CuCl_4$  is marked as a full circle.

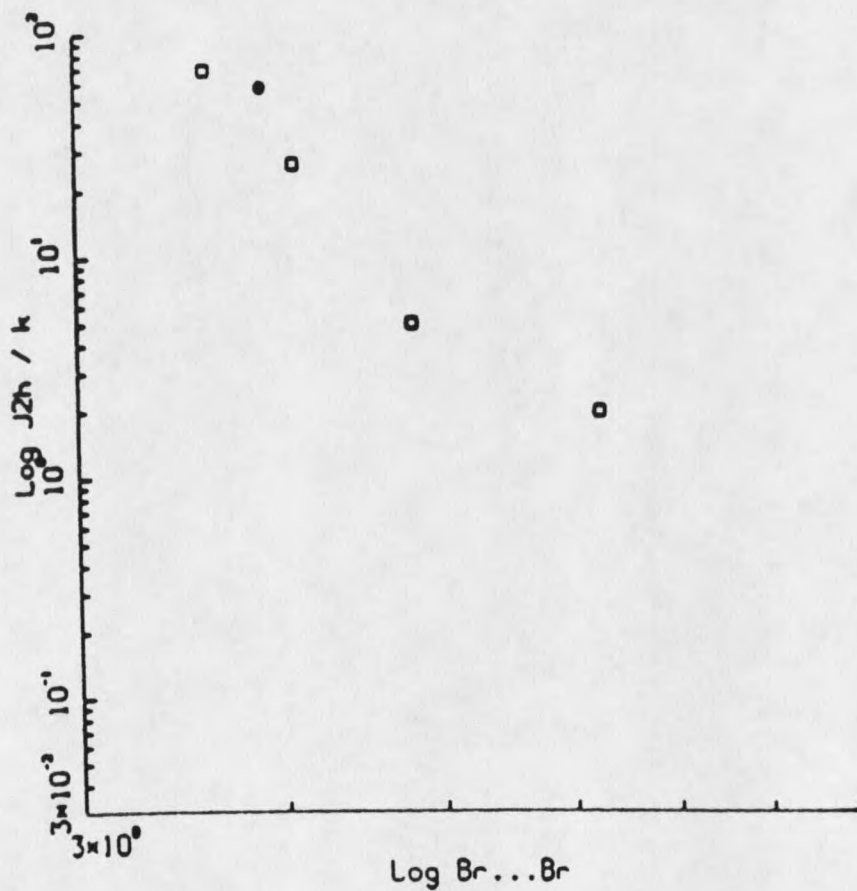


Figure 13  $\ln J_{2h}/k$  values vs.  $\ln \text{Br} \dots \text{Br}$  for  $(n\text{DA})\text{CuBr}_4$  series. Previous data points are marked as squares and the new result obtained in this work is marked as a full circle.

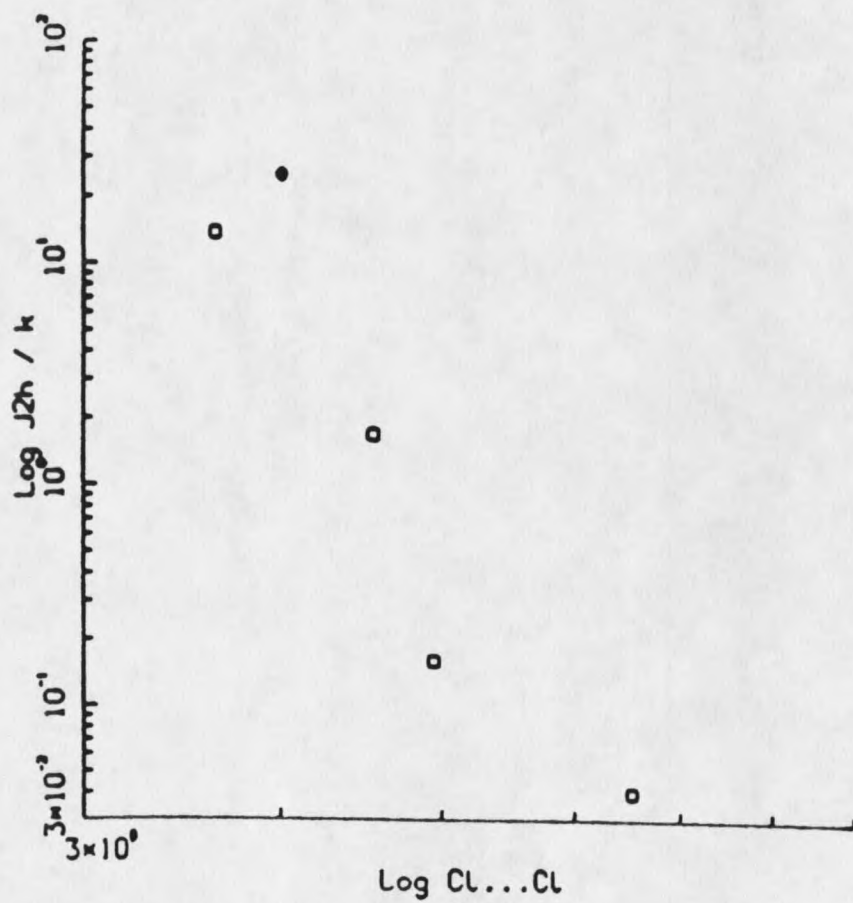


Figure 14  $\ln J_{2h}/k$  values vs.  $\ln \text{Br} \dots \text{Br}$  for  $(n\text{DA})\text{CuCl}_4$  series. Previous data points are marked as squares and the new result obtained in this work is marked as a full circle.

## CHAPTER 5

## CONCLUSION

The magnetic moments of copper(II) halide perovskite salts  $(3AP)CuX_4$ , where X stands for Br or Cl, have been reported for the first time.

The crystals were grown according to the literature and the powder susceptibility was measured by means of the Vibrating Sample Magnetometer.

The experimental results are explained by the Baker model, which is a high T expansion of the Heisenberg Hamiltonian for a square lattice combined with a molecular exchange field correction.

Both compounds demonstrate an antiferromagnetic exchange between the layers, since the value measured for the exchange parameter is negative.  $J_{2h} = -57 \pm 7$  for  $(3AP)CuBr_4$  and  $-25 \pm 1$  for  $(3AP)CuCl_4$ . Both salts demonstrate ferromagnetic exchange within the layer, with positive  $J_{1h} = 15 \pm 1$  for the Cl compound and  $20.5 \pm 2.5$  for the Br.

The interaction is stronger for  $(3AP)CuBr_4$  than for  $(3AP)CuCl_4$  as the absolute values of both  $J_{1h}/k$  and  $J_{2h}/k$  are larger for the bromide compound. The antiferromagnetic exchange is dominant for both samples. For the bromide salt this result is more evident,

as the ratio  $J_{2i}/J_{1i}$  is larger.

The  $\text{Cu}\cdots\text{X}$  and the  $\text{X}\cdots\text{X}$  bond lengths are found to affect the strength of the exchange interaction in a similar way to other salts. Longer bonds result in weaker interaction. The natural logarithm of  $\text{X}\cdots\text{X}$  bond length and the natural logarithm of  $J_{2i}/k$  obey the linearity which was previously found for  $(\text{nDA})\text{CuX}_4$  series of compounds.

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## APPENDIX

Figure 15 Documentation of general data analysis in Fortran. Comments give useful information to future program users.

C This program is called axb.for. It fits data points  
C to the polinomial ax+b. The data file is on line 13

```

IMPLICIT NONE
INTEGER IA,MWT,NDATA
REAL XLUMLG,DTLOG,SIGLX,A,B,SIGA,SIGB,CHI2,Q
DIMENSION XLUMLG(50),DTLOG(50),SIGLX(50)
MWT=1.
NDATA=1600.

OPEN (UNIT=10,FILE='chlore2.DAT',STATUS='OLD')
DO 1 IA=1,NDATA
  SIGLX(IA)=1.0
  READ (10,*,END=2) DTLOG(IA),XLUMLG(IA)
1  CONTINUE
2  CONTINUE
CLOSE (UNIT=10)
NDATA=IA-1

CALL FIT(DTLOG,XLUMLG,NDATA,SIGLX,MWT,A,B,SIGA,SIGB,
+ CHI2,Q)
+ WRITE (*,*) 'SLOPE:',B,'YCROSS:',A,'ERRORS:',SIGB,SIGA
+ ,CHI2,Q
STOP
END

SUBROUTINE FIT(X,Y,NDATA,SIG,MWT,A,B,SIGA,SIGB,CHI2,Q)
DIMENSION X(NDATA),Y(NDATA),SIG(NDATA)
SX=0.
SY=0.
ST2=0.
B=0.
IF (MWT.NE.0) THEN
  SS=0.
  DO 11 I=1,NDATA
    WT=1./(SIG(I)**2)
    SS=SS+WT
    SX=SX+X(I)*WT
    SY=SY+Y(I)*WT
11  CONTINUE
  ELSE
    DO 12 I=1,NDATA
      SX=SX+X(I)
      SY=SY+Y(I)
12  CONTINUE
    SS=FLOAT(NDATA)
  ENDIF
  SXOSS=SX/SS
  IF (MWT.NE.0) THEN
    DO 13 I=1,NDATA
      T=(X(I)-SXOSS)/SIG(I)
      ST2=ST2+T*T
      B=B+T*Y(I)/SIG(I)
13  CONTINUE
  ELSE
    DO 14 I=1,NDATA
      T=X(I)-SXOSS
      ST2=ST2+T*T
      B=B+T*Y(I)
14  CONTINUE
  ENDIF

```

```

B=B/ST2
A=(SY-SX*B)/SS
SIGA=SQRT((1.+SX*SX/(SS*ST2))/SS)
SIGB=SQRT(1./ST2)
CHI2=0.
IF(MWT.EQ.0) THEN
  DO 15 I=1,NDATA
    CHI2=CHI2+(Y(I)-A-B*X(I))**2
15  CONTINUE
    Q=1.
    SIGDAT=SQRT(CHI2/(NDATA-2))
    SIGA=SIGA*SIGDAT
    SIGB=SIGB*SIGDAT
  ELSE
    DO 16 I=1,NDATA
      CHI2=CHI2+((Y(I)-A-B*X(I))/SIG(I))**2
16  CONTINUE
    Q=GAMMQ(0.5*(NDATA-2),0.5*CHI2)
ENDIF
RETURN
END

```

```

FUNCTION GAMMQ(A,X)
IF(X.LT.0..OR.A.LE.0.) PAUSE
IF(X.LT.A+1.) THEN
  CALL GSER(GAMSER,A,X,GLN)
  GAMMQ=1.-GAMSER
ELSE
  CALL GCF(GAMMCF,A,X,GLN)
  GAMMQ=GAMMCF
ENDIF
RETURN
END

```

```

SUBROUTINE GSER(GAMSER,A,X,GLN)
PARAMETER (ITMAX=100, EPS=3.E-7)
GLN=GAMMLN(A)
IF(X.LE.0.) THEN
  IF(X.LT.0.) PAUSE
  GAMSER=0.
  RETURN
ENDIF
AP=A
SUM=1./A

```

```

DEL=SUM
DO 11 N=1,ITMAX
  AP=AP+1.
  DEL=DEL*X/AP
  SUM=SUM+DEL
  IF (ABS (DEL) .LT. ABS (SUM) *EPS) GO TO 1
11 CONTINUE
  PAUSE 'A too large, ITMAX too small'
1  GAMSER=SUM*EXP (-X+A*LOG (X) -GLN)
  RETURN
  END

```

```

SUBROUTINE GCF (GAMMCF, A, X, GLN)
PARAMETER (ITMAX=100, EPS=3.E-7)
GLN=GAMMLN (A)
GOLD=0.
A0=1.
A1=X
B0=0.
B1=1.
FAC=1.
DO 11 N=1, ITMAX
  AN=FLOAT (N)
  ANA=AN-A
  A0=(A1+A0*ANA) *FAC
  B0=(B1+B0*ANA) *FAC
  ANF=AN*FAC
  A1=X*A0+ANF*A1
  B1=X*B0+ANF*B1
  IF (A1.NE.0.) THEN
    FAC=1./A1
    G=B1*FAC
    IF (ABS ((G-GOLD) /G) .LT. EPS) GO TO 1
    GOLD=G
  ENDIF
11 CONTINUE
  PAUSE 'A too large, ITMAX too small'
1  GAMMCF=EXP (-X+A*ALOG (X) -GLN) *G
  RETURN
  END

```

```

FUNCTION GAMMLN (XX)
REAL*8 COF (6), STP, HALF, ONE, FPF, X, TMP, SER
DATA COF, STP/76.18009173D0, -86.50532033D0, 24.01409822D0,
* -1.231739516D0, .120858003D-2, -.536382D-5, 2.50662827465D0/
DATA HALF, ONE, FPF/0.5D0, 1.0D0, 5.5D0/
X=XX-ONE
TMP=X+FPF

```

```
TMP=(X+HALF)*LOG(TMP)-TMP
SER=ONE
DO 11 J=1,6
  X=X+ONE
  SER=SER+COF(J)/X
11 CONTINUE
GAMMLN=TMP+LOG(STP*SER)
RETURN
END
```

```

C      THE NAME OF THIS PROGRAM IS OA.FOR
C      THIS PROGRAM WILL ORDER THE TEMPS.  COMMENTS ALLOW
C      POSSIBLE CALCULATIONS FOR M AND T.
C      THE OLD FILE IS ON LINE 11 THE NEW ON 23
C      H,M, ARE DEFINED ON LINES 19,20
      IMPLICIT NONE
      INTEGER IB, IA, IC, ID, IF, N
      REAL H, MOL, T, MOM, OVT, XAI, TB, MOMB, MOMC, DY
      DIMENSION OVT(5000), XAI(5000), MOM(5000), T(5000), TB(5000),
      MOMB(5000)
      OPEN(UNIT=10, FILE='check1.DAT', STATUS='OLD')
      DO 2 IA=1,1000
      READ(10, *, END=3) T(IA), MOM(IA)
2     CONTINUE
3     CONTINUE
      CLOSE(UNIT=10)
      *****
      CALL ORDER (T, MOM, IA-1)
      *****
      *C
      *****

      H=6000
      MOL=0.00031163
      OPEN(UNIT=20, FILE='check2.DAT', STATUS='NEW')
      DO 4 IB=1, IA-1
      XAI(IB)=MOM(IB)/(H*MOL)
C     XAI(IB)=MOM(IB)/T(IB)
      XAI(IB)=1./XAI(IB)
      MOM(IB)=XAI(IB)
      WRITE(20, *) T(IB), MOM(IB)
4     CONTINUE
      CLOSE(UNIT=20)
      STOP
      END
C     THE NEXT SUBROUTINE ORDERS TEMPS.

      *****

      SUBROUTINE ORDER(T, MOM, N)
      *****
      IMPLICIT NONE
      INTEGER J, I, N
      REAL T, MOM, TTEMP, MOMTEMP
      DIMENSION T(N), MOM(N)
      DO 100 I=1, N
      DO 200 J=I, N
      IF (T(J) .LT. T(I)) THEN
      TTEMP=T(I)
      MOMTEMP=MOM(I)
      T(I)=T(J)
      MOM(I)=MOM(J)
      T(J)=TTEMP
      MOM(J)=MOMTEMP
      ENDIF
200    CONTINUE
      WRITE (*, *) T(I), MOM(I)
100   CONTINUE
      RETURN
      END

```

```

C     THE NAME OF THIS PROGRAM IS BP.FOR
C     LINE-15 HAS THE NAME OF THE SAMPLE FILE.
C     LINE-27 HAS THE NAME OF THE BACKGROUND FILE.
C     THIS PROGRAM SUBTRACTS BACKGROUND. (TAKES BACKGROUND FILE
C     AND EXTRAPOLATES EVERY TWO POINTS TO A STREIGHT LINE)
C     LINE 56 HAS CREATED FILE NAME.COMMENTS ALLOW TO CALCULATE XT INSTEAD
C     OF M .LINE 56 HAS THE NAME OF THE NEW FILE.

```

```

      IMPLICIT NONE
      INTEGER IB, IA, IC, ID, IF, N
      REAL H, MOL, T, MOM, OVT, XAI, TB, MOMB, MOMC, DY
      DIMENSION OVT(1000), XAI(1000), MOM(1000), T(1000), TB(1000),
      MOMB(1000)

      OPEN(UNIT=10, FILE='check.DAT', STATUS='OLD')
      H=5995.
      MOL=3.1163E-4

      DO 2 IA=1,1000
        READ(10, *, END=3) T(IA), MOM(IA)
2       CONTINUE
3       CONTINUE

      CLOSE(UNIT=10)
      CALL ORDER (T, MOM, IA-1)
      OPEN(UNIT=111, FILE='tef5.DAT', STATUS='OLD')

      DO 222 IC=1,1000
        READ(111, *, END=223) TB(IC), MOMB(IC)
222      CONTINUE
223      CONTINUE
      CLOSE(UNIT=111)

      N=IC-1
      *****
      CALL ORDER(TB, MOMB, N)
      *****
C     TB AND MOMB ARE THE BACKGROUND FILE INFO.
C     FROM THE SUBROUTINE WE GET TB, MOMB, AND AN UNCHANGED IC-1=N
      *****

      DO 333 ID=1, IA-1
        MOMC=0.
      *****
      CALL YAXB(TB, MOMB, N, T(ID), MOMC)
C     WE SEND BG AND SAMPLE INFO AND GET THE SUBTRACTED MOMC
      *****
      MOM(ID)=MOM(ID)-MOMC
      WRITE(*, *) T(ID), MOM(ID), MOMC
333      CONTINUE

      OPEN(UNIT=69, FILE='check1.DAT', STATUS='NEW')
      DO 777 IF=1, IA-1
        WRITE(69, *) T(IF), MOM(IF)
777      CONTINUE
      CLOSE (UNIT=69)
      END

```

```

C      OPEN(UNIT=20,FILE='POLI.DAT',STATUS='NEW')
C      DO 4 IB=1,IA-1
C          XAI(IB)=MOM(IB)/(H*MOL)
C          XAI(IB)=T(IB)*XAI(IB)
C          WRITE(20,*)T(IB),XAI(IB)
C      CONTINUE
C      CLOSE(UNIT=20)
C      STOP
C      END
C      THE NEXT SUBROUTINE ORDERS TEMPS.

```

\*\*\*\*\*

```

SUBROUTINE ORDER(T,MOM,N)
IMPLICIT NONE
INTEGER J,I,N
REAL T,MOM,TTEMP,MOMTEMP
DIMENSION T(N),MOM(N)
DO 100 I=1,N
  DO 200 J=I,N
    IF(T(J).LT.T(I))THEN
      TTEMP=T(I)
      MOMTEMP=MOM(I)
      T(I)=T(J)
      MOM(I)=MOM(J)
      T(J)=TTEMP
      MOM(J)=MOMTEMP
    ENDIF
  200 CONTINUE
  WRITE(*,*)T(I),MOM(I)
  100 CONTINUE
RETURN
END

```

```

C      THE NEXT SUBROUTINE EXTRAPOLATES THE BG FILE.
SUBROUTINE YAXB(TB,MOMB,N,T,MOMC)
IMPLICIT NONE
INTEGER IG,N
REAL T,TB,MOMB,MOMC,MOM
DIMENSION TB(N),MOMB(N)

MOMC=0.
DO 100 IG=1,N
  IF(T.LT.TB(1))THEN
    MOMC=MOMB(1)
    GOTO 200
  ENDIF
  IF(T.GT.TB(N))THEN
    MOMC=MOMB(N)
    GOTO 200
  ENDIF
  IF(T.EQ.TB(IG))THEN
    MOMC=MOMB(IG)
    GOTO 200
  ENDIF
  IF(T.GT.TB(IG))THEN
    IF(TB(IG).EQ.TB(IG+1))GOTO 100
    MOMC=(T*(MOMB(IG+1)-MOMB(IG))/
    (TB(IG+1)-TB(IG))+MOMB(IG)-
    TB(IG)*((MOMB(IG+1)-MOMB(IG))/(TB(IG+1)-TB(IG)))
    ④
    ④
  ENDIF
  200

```

100 CONTINUE  
200 RETURN  
END

```

C      THIS PROGRAM IS CALLED AV1.FOR . IT CALCULATES THE
C      AVERAGE BACKGROUND AT EACH TEMPERATURE INTERVAL DT DEFINED ON LINE 38
C      THE OLD FILE IS ON LINE 10, THE NEW ON 40
      IMPLICIT NONE
      INTEGER IB, IA, IC, ID, IF, N, HI, II, IH
      REAL H, MOL, T, MOM, OVT, XAI, TB, MOMB, MOMC, DY, TPM
      DIMENSION OVT(5000), XAI(5000), MOM(5000), T(5000), TB(5000),
      MOMB(5000)
e
      OPEN(UNIT=10, FILE='check33.DAT', STATUS='OLD')
      DO 20 IH=1, 5000
      READ(10, *, END=30) T(IH), MOM(IH)
20     CONTINUE
30     CONTINUE
      CLOSE(UNIT=10)

      CALL ORDER(T, MOM, IH-1)
*****
      CALL AVERAGE (T, MOM, IH-1)
*****
      END

*****
      SUBROUTINE AVERAGE(T, MOM, N)
*****
      IMPLICIT NONE
      INTEGER J, I, N, M, K, NMAX
      REAL T, DT, TI, MOM, TP, MP, MF, TF, TPM
      DIMENSION T(N), MOM(N)
      TPM=0.
      TI=4.
      TF=0.
      K=1.
      DT=1.
      NMAX=NINT((T(N)-T(1))/DT)
      OPEN (UNIT=22, FILE='check34.DAT', STATUS='NEW')

      DO 500 J=1, NMAX
      IF (TI+DT.GE.T(N)) THEN
      GOTO 600
      ENDIF
      DO 300 I=1, N
      IF (TI.LT.T(I).AND.T(I).LT.TI+DT) THEN
      TF=TF+T(I)
      MF=MF+MOM(I)
      TP=TF/K
      MP=MF/K
      K=K+1.
      ENDIF
300    CONTINUE
      IF (TP.NE.TP) THEN
      WRITE(22, *) TP, MP
      ENDIF
      MF=0.
      TF=0.
      TPM=TP
      TI=TI+DT
      K=1.

500    CONTINUE
600    CLOSE(UNIT=22)
      RETURN

```

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