SIMULATION AND TESTING OF RESIN INFUSION MANUFACTURING PROCESSES FOR LARGE COMPOSITE STRUCTURES

by

Daniel Blair Mastbergen

A thesis submitted in partial fulfillment
of the requirements for the degree

of

Master of Science

in

Mechanical Engineering

MONTANA STATE UNIVERSITY-BOZEMAN
Bozeman, Montana

JULY 2004

©COPYRIGHT

by

Daniel Blair Mastbergen

2004

All Rights Reserved

APPROVAL

of a thesis submitted by

Daniel Blair Mastbergen

This thesis has been read by each member of the thesis committee and has been found to be satisfactory regarding content, English usage, format, citations, bibliographic style, and consistency, and is ready for submission to the College of Graduate Studies.

Dr. Douglas Cairns

Approved for the Department of Mechanical and Industrial Engineering

Dr. Vic Cundy

Approved for the College of Graduate Studies

Dr. Bruce McLeod

STATEMENT OF PERMISSION TO USE

In presenting this thesis in partial fulfillment of the requirements for a master's degree at Montana State University-Bozeman, I agree that the Library shall make it available to borrowers under rules of the Library.

If I have indicated my intention to copyright this thesis by including a copyright notice page, copying is allowable only for scholarly purposes, consistent with "fair use" as prescribed in the U.S. Copyright Law. Requests for permission for extended quotation from or reproduction of this thesis in whole or in parts may be granted only by the copyright holder.

Daniel Mastbergen

Date 7-19-04

TABLE OF CONTENTS

LIST OF TABLES vii

LIST OF FIGURES viii

ABSTRACT xi

1. INTRODUCTION 1

2. GENERAL BACKGROUND 4

Composite Materials 4
Matrix Materials 6
Reinforcement Materials 7
Fiber Volume Fraction 10
Porosity 11
Manufacturing Processes 12
Blade Design 17

3. PROCESS MODELING BACKGROUND 20

Stokes flow 22
Injection System Modeling 23
Channel Flow Modeling 29
Fabric Flow Modeling 32
Darcy Flow 32
Saturated vs. Unsaturated Flow 34
Fabric Compressibility 38
Calculating Saturation Time 42
Comprehensive Model 44
Methodology 44
Building the Matrix 46
Assumptions 53

4. EXPERIMENTAL PROCEDURES AND EQUIPMENT 55

Test Fluid 55
Injection System Tests 57
Channel Flow Tests 58
Fabric Flow Tests 60
Fabrics Tested 60
Fabric Compaction Data 62

Air Permeability Tester 62
Liquid Permeability Tester 65
Permeability Testing Procedures 66
Capillary Pressure Tests 68
Comprehensive Model Tests 69

5. EXPERIMENTAL RESULTS AND ANALYTICAL CORRELATIONS 72

Injection System Test Results 72
Channel Flow Test Results 73
Fabric Test Results 75
Fabric Compaction Data 75
Liquid Permeability Test Results 77
Air Permeability Test Results 81
Capillary Test Results 82
Comprehensive Model Test Results 84

6. PARAMETRIC STUDY 90

Channel Height 90
Injection System 97
Injection Pressure 100
Fabric Permeability 102
Fabric Thickness 104

7. DISCUSSION OF RESULTS 107

Fabric Tests 107
Air Permeability Testing 109
Comprehensive Model 111
Limitations of the Model 114
Parametric Study 118

8. CONCLUSIONS AND FUTURE WORK 121

Application to Manufacturing 121
Injection System / Channel Flow Modeling 123
Injection System / Channel Flow Future Work 123
Fabric Tests 124
Fabric Test Future Work 125
Comprehensive Model 126
Comprehensive Model Future Work 127

REFERENCES CITED 128

APPENDICES 129

Appendix A – Matlab Program for Entire Process 133
Appendix B – Hose System Calculations from Mathcad 144
Appendix C – Permeability Data 147
Appendix D – Compaction Data 149
Appendix E – Input to Model for Experimental Correlations 151

LIST OF TABLES

Table Page

1. Summary of manufacturing process details. 17
2. Results from hose system tests 73
3. Results from channel flow experiments 74
4. Comparison of air permeability results and liquid permeability results 82
5. Effect of varying parameters 120

LIST OF FIGURES

Figure		Page
1.	Micrograph of fibers and resin	6
2.	Fabric roll	9
3.	Unidirectional, double bias and woven roving fabrics	9
4.	Schematic for pressure bag molding	15
5.	Pressure bag molding during stage one	16
6.	Blade construction	18
7.	Blade cross section	18
8.	Injection system diagram	27
9.	Correction factor for channel aspect ratio	30
10.	Illustration of dual scale flow	37
11.	Pressure gradient as flow front progresses	43
12.	Division of mold into cells	45
13.	Schematic of flow model with variables labeled	47
14.	Expanded matrix for 3 cell example	49
15.	Flow chart for model	51
16.	Example output from model at three different times	52
17.	Pressure profile in hose and channel	53
18.	Effect of temperature on viscosity	56
19.	Injection manifold	58
20.	Schematic of channel flow experimental setup	59
21.	Fabric tested for permeability	61

22. Cross section of hybrid composite stack....61
23. Air test coupon....63
24. Cross section of air permeability tester....64
25. Air permeability test setup....64
26. Liquid permeability tester....65
27. Test sample being prepared....66
28. Test apparatus for testing channel flow and comprehensive model....69
29. Upper and lower flow fronts....70
30. Fiber volume % vs. compaction pressure....76
31. Ply thickness fraction vs. compaction pressure....76
32. Permeability results for all materials tested....78
33. Permeability at high pressure for woven carbon fabric....79
34. Illustration of flow channel variation....80
35. Repeatability study for unidirectional fabric....81
36. Flow front coming through fabric during capillary pressure test....83
37. Output from model compared to experimental result (test 1)....85
38. Output from model compared to experimental result (test 2)....85
39. Pressure profile from experiment compared to profile used in model....87
40. Output from model compared to experimental result....88
41. Varying channel height for thin part....91
42. Effect of channel height on small part....93
43. Flow front for thick part, 20% channel height....94
44. Flow fronts after resin is injected and total process time for large part....95
45. Effect of channel height on large part....97

46. Effect of hose system on saturation time for .6 cm thick part.....98

47. Effect of hose system on saturation time for 10 cm thick part.....99

48. Effect of injection pressure on process time for .6 cm thick part.....100

49. Effect of injection pressure on process time for 10 cm thick part.....102

50. Effect of fabric permeability on process time for .6 cm thick part.....103

51. Effect of fabric permeability on process time for 10 cm thick part.....104

52. Effect of fabric thickness on process times.....105

53. Error when using individual equations compared to fabric thickness. 106

54. Effect of injection pressure on woven carbon fabric (10 cm initial thickness).....108

ABSTRACT

The use of composite materials in large primary structures such as wind turbine blades and boat hulls has dramatically increased in recent years. As these structures get larger, new manufacturing processes are required to make them possible. Larger parts also require more expensive tooling, and a higher cost for scrapped parts. This may prohibit the trial and error approach that has been used for many years. The need for accurate process modeling in the design of tooling is becoming essential. Unfortunately, as the processes become more complex so do the models.

Although there are several potential processes capable of producing very large parts (10 m - 50 m), they all have one common feature. In order to alleviate the problem of forcing the resin to flow large distances though the fabric, they use a distribution system to spread the resin over the surface of the part. The resin then flows a substantially shorter distance between the channels or through the thickness. The goal of this work was to develop a modeling technique that could accurately model these processes, yet not so complex as to loose its utility. In this study, the flows through the different regions of the mold are examined individually. These regions include the injection system, the distribution channel, and the fabric. The governing equations for each region are then combined to form a comprehensive model that accounts for the flow through each region simultaneously. A series of tests were conducted to verify the models of the individual components, as well as the comprehensive model. The rate limiting step through the fabric was also examined in detail. The model correlated well with the experiments performed, and revealed critical information about these types of processes. A major conclusion is that an accurate and straightforward model can be created for large scale processes, using the small scale bench tests performed in this study. Also, the governing equations developed here from Darcy flow and Stokes flow aid in understanding how the scaling of key parameters affects the process as a whole. Variations in the geometry of the channel, the fabric thickness and fabric properties such as permeability and compressibility can be accounted for in the model.

CHAPTER 1

INTRODUCTION

In recent years, the usage of composite materials in primary structural applications has continually increased. The growth rate of composites has far surpassed all other materials [1]. Composites are rapidly replacing steel and aluminum in many applications such as aircraft, wind turbines, and automobiles [2,3]. The appeal of composites in these types of applications is due primarily to the composites structural performance. Unfortunately, this increased performance has typically come with an increased cost. The aerospace industry has been able to afford these higher prices. In some cases, composites have enabled designs that would otherwise be impossible [4]. In aerospace the added cost of advanced composite materials has been acceptable. On the other hand, the wind turbine industry has stricter limitations on material cost [3,5]. Because a wind turbine of a given size has a finite amount of power and revenue it can generate, the cost of the structure cannot exceed this amount. A large part of this cost is in the materials and manufacturing involved in the blades. Therefore, the capability of wind turbines to produce power at a rate competitive with fossil fuels is strongly dependant on these costs.

Although the constituent materials themselves can be costly, the greatest cost is in converting them into a structure [4,6]. One of the most promising methods to reduce blade cost is to decrease the cost of manufacturing. For large structures especially, the most commonly used method of manufacturing has been hand lay-up [5]. This process is very time consuming and labor intensive. In a push to reduce the time and labor involved

in manufacturing large structures, several variants of resin transfer molding(RTM) have been developed. Processes such as the Seemanns Composite Resin Infusion Molding Process (SCRIMP™), and the Fast Remotely Actuated Channeling process (FASTRAC), are being recognized as feasible alternatives to hand lay-up for large structures [5,7]. These processes, which will be described in more detail later, have eliminated some of the limitations typically associated with RTM. They have proven themselves in making boat hulls, turbine blades, and an assortment of other large structures. However, there is still uncertainty as to whether they will be capable of producing wind turbine blades for use on the current multi-megawatt wind turbines. TPI is now currently producing 30 m blades using SCRIMP™. However, recent wind turbine designs are utilizing blades up to 50 m in length [5]. Producing a blade of this size using an RTM process requires an extremely expensive mold. Before making one of these molds it is critical to know that the RTM process will be successful.

In the past, and even today, a large amount of mold design is done by trial and error [7,8,9]. As molds for new part geometries are created, the designers typically rely on years of experience to make decisions as to how the mold should be constructed, and how long the process should take. If modifications to the mold or process need to be made, a manufacturer can do so at a small expense. However, for very large structures this approach could be extremely costly. Producing a large number of trial parts in order to create a successful part may not be an option. Or even worse, if a mold turned out to be a failure, the money wasted could be enormous. Because of the high stakes involved in

making such large tooling, there needs to be a more detailed look at the process beforehand to ensure its success.

The need for an accurate computer model to aid in producing a successful part is critical to mitigate the aforementioned risks. Unfortunately, many models that do exist are so complex that they are not used by manufacturers, or they are geared to more simplistic forms of RTM that are not being used for large structures. The motivation for this work was to develop a user friendly model to help mold designers reduce the typical uncertainty and wasted parts common to RTM. This model will enable manufacturers to study the effects of changing processing parameters without generating scrap parts. As a part of this work, several key parameters are identified. Their influence on the process is illustrated through a parametric study.

In addition to the comprehensive model developed here, analytical equations are derived for the time required to fill the channel of an infusion type process, and for flow through the thickness of a typical dry lay-up. These equations give great insight into how changing parameters will affect the process. Alone, they are not as accurate as the comprehensive model. However, for someone who is not ready to put the time into developing a complex computer model, they can be very enlightening, as will be discussed.

Ultimately, these models will help the wind turbine industry and others to evaluate the feasibility and cost effectiveness of these new manufacturing processes. The models will also help in identifying problems, and optimizing the mold geometry.

CHAPTER 2

GENERAL BACKGROUND

Composite Materials

Composite materials have been known to man for thousands of years, and occur naturally in many living things. The earliest composite materials were straw reinforced brick, which was similar to modern steel reinforced concrete [4]. Some composites that exist naturally are wood and bone. A composite is generally any material that is made up of different constituent materials. Typically, the composite material has properties exceeding those of the constituent elements alone. Composites are now being used in almost every industry as the demands on materials continue to increase and become more specific. They are used for applications in aerospace, sporting goods, boats, wind turbines, and automobiles.

Because the composite is made up of two or more materials, there is almost an infinite amount of possible combinations. Because of this, composites can be engineered to have properties that are very specific to a particular application. Composites can be engineered for requirements in stiffness, strength, damage tolerance, corrosion resistance, conductivity, and many others. One property that has been of particular importance is the stiffness to weight ratio, where carbon fiber has excelled. Carbon fiber can have a five times higher stiffness to weight ratio than aluminum [4]. This has encouraged its use in the aerospace industry where weight is critical. Composites have also been chosen for

reasons that are not related to mechanical performance. They have been used to create materials with almost zero thermal expansion for use in space applications, and have also been used in applications where corrosion resistance is critical such as storage tanks and piping [4].

Composites are often combined in pairs where one material is in the form of a fiber, and the other creates a matrix to support the fiber. Typically the material with the highest stiffness and tensile strength is used as the fiber to give the material its strength [1]. The matrix can serve several purposes. Mainly, it keeps the fibers aligned and provides compressive and shear strength. Since the fiber would easily buckle in compression, the matrix is intended to stabilize the fiber. The matrix also adds toughness to the material by creating a large damage zone. The matrix transmits the load to the fibers and distributes it throughout the part. In addition to supporting the fiber, the matrix also protects it. The matrix protects the fibers from abrasion between fibers, as well as from environmental degradation [2]. Figure 1 is a micrograph of a typical composite material from reference 10. The picture is looking along the direction of the fibers of a D155 fabric at 60X magnification.

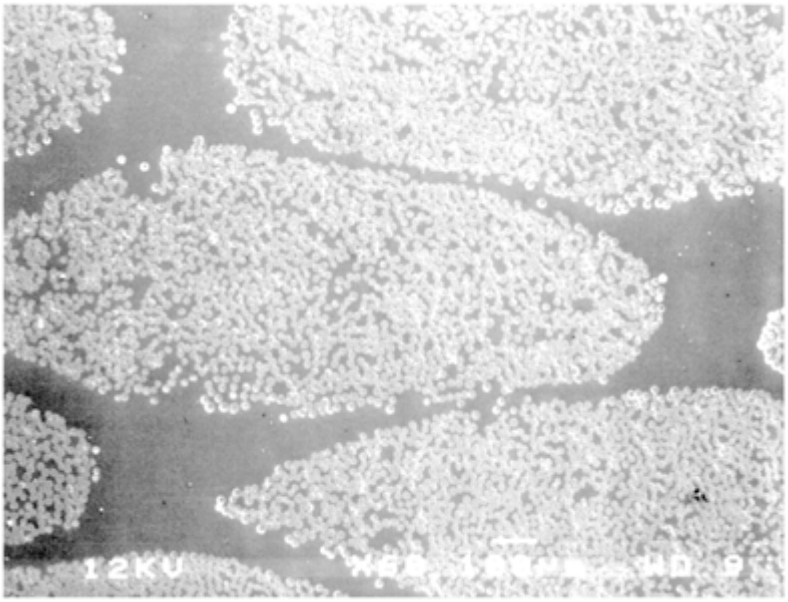


Figure 1: Micrograph of fibers and resin [10].

Matrix Materials

Composites utilize many different materials to form the matrix. There are metal matrix composites, ceramic matrix composites, and polymer matrix composites. The first two can be very difficult to process, and have been used sparsely for very specific applications. The most common structural composite materials are fiber reinforced plastics, or FRPs [11]. These materials typically use one of two types of plastic for the matrix. The first types are thermosetting plastics such as epoxy, otherwise known as thermosets. Thermosets are polymer chains infused into the reinforcement in the liquid form where they then become strongly cross-linked over a short period of time. Due to the cross-linking, these matrix materials tend to be quite stiff, and are resistant to creep. Unfortu-

nately, they can also be very brittle [11,12]. The second type of polymer used is the thermoplastic such as nylon. Thermoplastics are also combined with the reinforcement in the liquid form. However, they contain much longer polymeric chains which give them a very high viscosity. As a result, thermoplastics cannot be used in many of the manufacturing processes that thermosets can. The bonding structure is also different in thermoplastics. They form much weaker secondary bonds to hold the polymer chains together [11]. For this reason, thermoplastics can be reshaped and reused to some extent. At the same time, they are also less stiff and prone to creep. One advantage of the weaker intermolecular bonds is an increase in damage tolerance [2].

Reinforcement Materials

The most common reinforcement materials are glass fibers. E-glass is the most widely used glass fiber and is very similar to window glass. The principal ingredient is silica (SiO_2), with additions of other oxides to improve workability and corrosion resistance [2]. Glass reinforced plastics have a moderately high strength at a relatively low cost. Typically, bulk glass is considered to be a very "weak" material. However, this is primarily due to the presence of flaws in the glass and its low fracture toughness. Pure glass has a very high strength, but it is very brittle due to the bonding structure. Any flaws present quickly turn to cracks which can propagate with very little stress. The use of very small fibers in a plastic matrix alleviates this effect in a couple of ways. First, by using very small fibers the average flaw size in the glass is dramatically reduced [1]. Secondly, fiber failure is isolated by the matrix. If a single fiber breaks, the crack will not propagate though the matrix, and the remaining fibers carry the load. The combina-

tion of fibers and matrix also spreads damage over a large area, which can dissipate a large amount of energy. These effects, among others, make fiberglass very strong and damage tolerant. Among composite materials, fiberglass also has one of the lowest costs [1]. The limitations of fiberglass are primarily due to its high density and low tensile modulus [2].

Carbon fibers are the second most common reinforcement, and boast one of the highest strength and stiffness to weight ratios of any material. Its primary use has been in the aerospace industry, although it is becoming more widely used in all fields. It has seen increased usage in sporting goods especially, for items such as bicycle frames and tennis rackets [2]. Carbon fiber also has very good fatigue resistance which is important in many designs, especially wind turbines [10]. The primary drawback of carbon fiber is the cost. Bulk glass fibers are produced for around $2/kg, while the lowest cost carbon fibers are currently about $19.80/kg [5]. This has limited the use of carbon fiber in many industries, and will continue to do so in the future. Another weakness of carbon fiber is due to its high degree of anisotropy. Because the fibers are typically oriented in a single direction or plane, the part is very stiff in that direction, but not in the other planes. For this reason, any waviness or misalignment of the fibers can cause high stress concentrations. This is particularly true in compression where any defect can greatly reduce the compressive strength [13].

Glass and carbon fibers are typically used in the form of fiber mats. These mats are created by weaving bundles of fibers called tows into a fabric, much like a textile process. By altering the directions of the fiber tows, fabrics with very different properties

can be created using the same fibers. These fabrics are typically stored on rolls. The direction along the length of the roll is referred to as the warp direction. This is also commonly referred to as the 0^0 direction. The direction transverse to the roll is called the weft direction. Figure 2 is an illustration of a fabric roll.

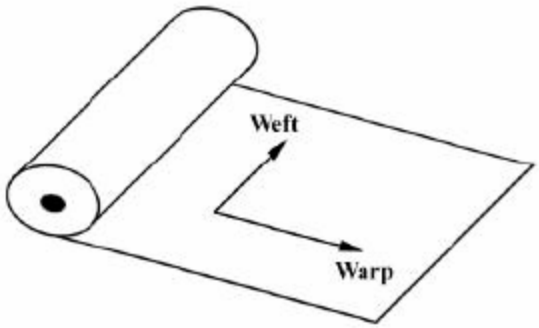


Figure 2: Fabric roll [14].

Some common fiber architectures are unidirectional (fibers in 0^0 direction), double bias(fibers in $+45^0$ and -45^0 directions), and woven roving (fibers in 0^0 and 90^0 direction typical). These architectures are shown in Figure 3.

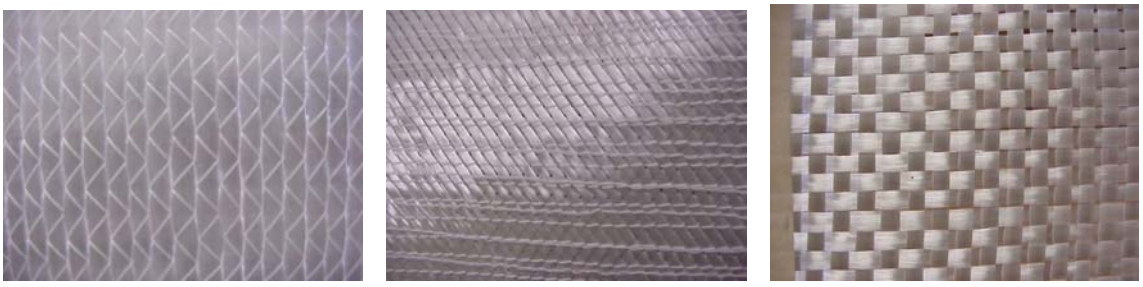


Figure 3: Unidirectional, double bias, and woven roving fabrics.

Fiber Volume Fraction

Another important consideration in the design and use of composites is the relative amounts of fiber and matrix. This relationship is commonly expressed as a fiber volume fraction or percent, and is sometimes referred to as fiber content. Since the fibers make the most significant contribution to the composite strength it is important to know this quantity. A composite with a high fiber volume fraction will be much stiffer and stronger than one with a lower fiber fraction. In addition, it will typically have a higher strength to weight ratio. To predict the effect of the fiber volume fraction on the composites properties the rule of mixtures is commonly used. This can be useful in predicting bulk properties such as the density, modulus, thermal conductivity, etc.

$$P_c = P_f V_f + P_m V_m \tag{2.1}$$

Where :
P_c = is a property of the composite
P_f = is the property of the fibers
V_f = is the fiber volume fraction
P_m = is the property of the matrix
V_m = is the matrix volume fraction

There are many factors that contribute to the fiber content of a composite. Since the fibers are round there will always be spaces between them even if they are all touching. This sets a theoretical limitation on the fiber volume fraction of 0.75 to 0.85 depending on the packing arrangement [10,12]. However, these fiber volume fractions are not practical since fiber on fiber contact is undesirable. This limits local fiber volume fractions to about 0.7.

In woven or stitched fabrics the maximum attainable fiber volume fraction is reduced even more. Although the fiber volume fraction within the tows may be 0.7, there are larger gaps created between tows by the weaving and stitching pattern. Resin flow channels may also be integrated into the fabric that can lower the fiber volume fraction. The fiber volume fractions of fabrics can be increased by forcing the plies together with mechanical force [10]. This can be accomplished by a hard tool surface, or by a fluid pressure. As pressure is applied, the fibers get mashed into each other, shrinking the voids caused by stitching. This is referred to as nesting, and will be described in greater detail later.

Porosity

Porosity has a couple of meanings in relation to composites. The first, in the absence of resin, is simply the opposite of the fiber volume fraction, or one minus the fiber volume fraction. This value is more relevant to flow modeling than strength concerns. For flow modeling one is more concerned about the passage ways between the fibers than the fibers themselves. The other meaning of porosity is in relation to microscopic voids or air pockets existing in a composite after the impregnation by the resin. This type of porosity can be detrimental to the mechanical performance of a part. Porosity can cause stress concentrations, as well as allow fibers to rub against each other. This is especially important for fatigue properties. Porosity can also leave the fibers exposed to harmful environments [2]. One of the best ways to reduce porosity is to use a vacuum to pull the air out of a mold. As the resin is injected, there is little air to trap.

Manufacturing Processes

There are many techniques available today for manufacturing thermoset composite parts. Some are still very low tech and labor intensive, while some involve very sophisticated tooling and computer controls. However, all of these processes share some of the same challenges and requirements. They all consist of a tool to hold the fabric in the correct position while the resin is curing, and require some means of forcing the resin into the fabric. The major differences in the processes are the resulting part quality, limitations in size and geometry, cost of tooling, and process time.

The most basic and labor intensive process is known as hand lay-up. In hand lay-up fabric is placed onto a tool where resin is applied by hand using rollers and squeegees. Each ply must be saturated as it is applied to the tool to ensure that no bubbles are left between plies. This makes hand lay-up very time consuming, but it does have its advantages. Carefully applying resin to each ply can ensure a part without dry spots. Unfortunately, the process is not performed under vacuum so micro-porosity is possible. Hand lay-up is very attractive due to the low cost of the tooling required. Since there is no pressure applied to the tool it does not have to be very robust, and can be made out of a variety of materials. In many cases, the tool will only have one side to produce a nice finish on the outside of the part. Hand lay-up can also be used to produce very large parts. As long as there are enough people to apply the resin to the fabric before it cures, there are really no limitations on the size of the part. Hand lay-up is currently the most utilized method of manufacture for large wind turbine blades [5]. Unfortunately, there are also many disadvantages to hand lay-up. The most obvious is the labor cost. In addi-

tion, the application of the resin in an open environment allows very volatile emissions to escape from the resin that can be harmful to humans and to the environment [14]. It is anticipated that the use of hand lay-up for wind turbines will eventually be restricted due to the high volume of emissions [5]. Other disadvantages are lower dimensional tolerances, poor fatigue performance, and less aerodynamic surfaces. Even with these considered, hand lay-up is still the fastest and cheapest way to produce a small number of composite parts with few defects, but the process is limited.

Beginning in the 1950's, more industrialized processes began to evolve for use on aircraft [1,15]. These processes are generally referred to as resin transfer molding processes, or RTM. In RTM the fabric is laid into a tool where the resin is forced into the fabric under pressure. These processes have several advantages over the hand lay-up process. The process has the potential to be more repeatable and consistent since the human involvement is reduced. This reduction in human involvement also reduces labor costs. In addition, the amount of volatile emissions is reduced. Much higher fiber contents can also be achieved since the tool can clamp down on the fiber preform. Dimensional tolerances can also be increased if the tool is two sided [16]. The disadvantages are the cost of the mold and the difficulty in forcing the resin through the fabric.

Modifications of the RTM process have been developed recently that reduce these disadvantages. Although there are many variants being used today, they all deal with these problems in a similar manner. Lower tool costs are achieved with the use of one-sided molds. In these processes a vacuum is drawn on the fabric, while a flexible bagging is forced against the preform by atmospheric pressure. To deal with the problem of

getting the resin to flow large distances through the fabric, a distribution network is used. This distribution network allows the resin to flow through high permeability channels or layers to disperse it throughout the mold. The resin must then flow a much shorter distance in the plane or though the thickness of the part. Several variants of these processes are described in detail by Larson [17], and will be discussed briefly here.

One process that has been successfully used on large structures is the Seemanns Composite Resin Infusion Molding Process (SCRIMP™). This process has been used since the 1980's and its use continues to increase. There are several variations of SCRIMP™. One uses a series of channels above the fabric for resin distribution, and the resin is then forced to flow in the plane of the fabric between the channels. In other variants, a high permeability layer may be placed over the fabric for resin distribution. The resin is then forced to flow though the thickness of the fabric. This layer is then peeled off after the process is complete. SCRIMP™ is capable of producing large parts very quickly, cheaply, and with high fiber volume fractions [7].

A very similar process known as the Fast Remotely Actuated Channeling process (FASTRAC) is a more recent variation of this general principle. The main difference in the FASTRAC process compared to SCRIMP™ is a more refined distribution strategy. The distribution network is created by a "FASTRAC layer" which is a flexible membrane with tightly spaced channels formed into it. The major difference is that these channels can be collapsed to force the extra resin though the fabric or out of the mold, rather than leaving them attached to the part as in SCRIMP™. The FASTRAC layer also allows a positive pressure to be applied to the fabric to achieve even higher fiber volume fractions.

A process very similar to FASTRAC was developed by Larson which will be referred to as pressure bag molding [17]. In pressure bag molding the distribution system is a channel that covers the whole surface of the fabric. Once the resin fills the channel, pressure is applied to a flexible film to force the resin into the fabric as in FASTRAC. In order to apply a positive pressure to the bagging, a second tool half is required. Although this adds an additional cost in the tooling, the second mold half would not require the surface finish and dimensional tolerance that the first half would. The mold for this process is illustrated in Figures 4 and 5. In these figures the flow channel is just empty space; however, it could also represent a highly permeable layer as in SCRIMP™ or FASTRAC.

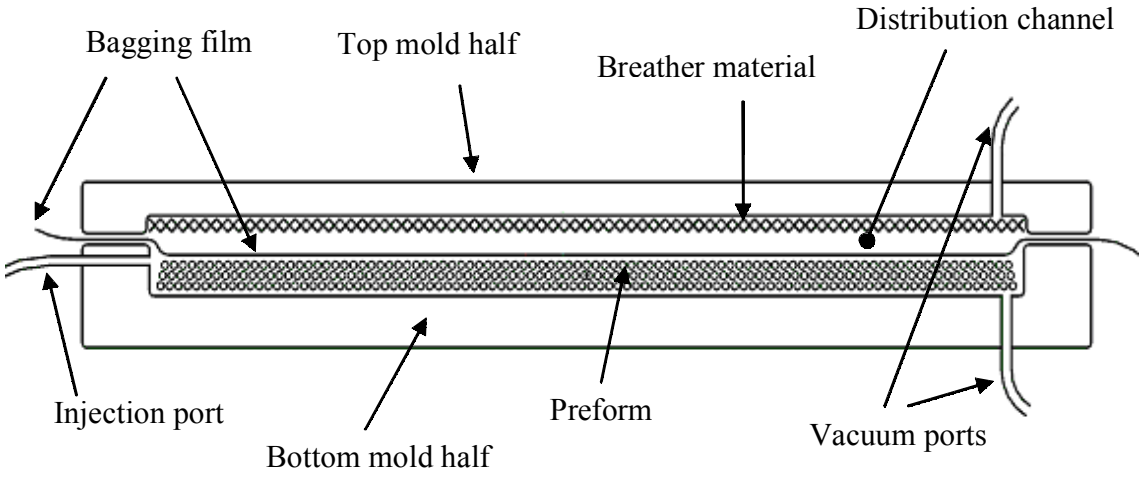


Figure 4: Schematic for pressure bag molding [17].

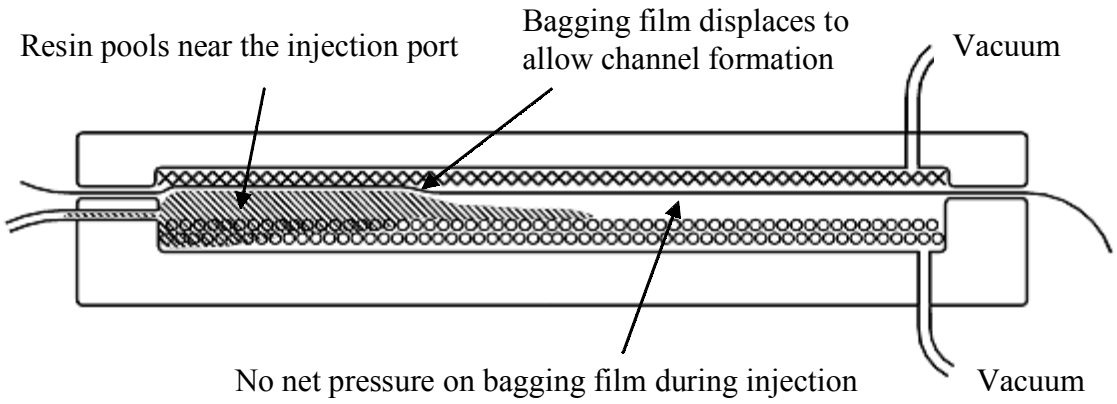


Figure 5: Pressure bag molding during stage one [17].

Of the processes examined, the FASTRAC and pressure bag molding process have been identified as having the largest injected volume per port[17]. This is due to the fact that the distribution system covers the whole part. For this reason, these processes are the most viable for large wind turbine blades, and will be the focus of this study. For future modeling this process will be described in two stages. Stage one consists of injecting the resin into the mold, and stage two is when pressure is applied to the bagging to force the resin through the thickness.

A summary of several of the processes described is presented in Table 1 which is taken from Larson [17]. Due to their similarity, the FASTRAC and pressure bag molding processes are presented together.

Table 1: Summary of manufacturing process details [17].

Process	Basic Principles	Advantages	Disadvantages
Hand Lay-up	Open mold Manual infusion One sided mold	Low cost Fastest implementation	Volatile emissions Health risks Inconsistent results Less efficient material usage
RTM	Closed mold In-plane resin flow Two-sided mold	Higher dimensional consistency Less volatile emissions Both sides finished	Higher mold cost Resin flow pattern critical Costly equipment required Lowest volume per port
VARTM	Closed mold In-plane resin flow Two-sided mold Evacuated mold	Higher dimensional consistency Less volatile emissions Both sides finished Higher quality products than RTM	Higher mold cost Resin flow behavior critical Costly equipment required Complexity of vacuum porting
SCRIMP™	Closed mold In-plane resin flow One-sided mold Evacuated mold	Higher dimensional consistency Less volatile emissions Higher quality products than RTM	Proprietary process One side finished
FASTRAC + Pressure Bag	Closed mold Channel flow One side critical Evacuated mold	High quality High dimensional consistency Less volatile emissions Largest injection volume per port	Added cost of FASTRAC layer or top mold half Highest complexity Possible artifacts from bag Costly equipment required

Blade Design

This work has focused primarily on investigating and modeling processes that could be used to produce megawatt scale wind turbine blades. In order to understand how these processes might be applied, it is important to look at how a turbine blade is constructed.

Although there have been many different blade designs over the years, the industry has converged on a fairly universal structure. A typical blade construction is shown in Figure 6.

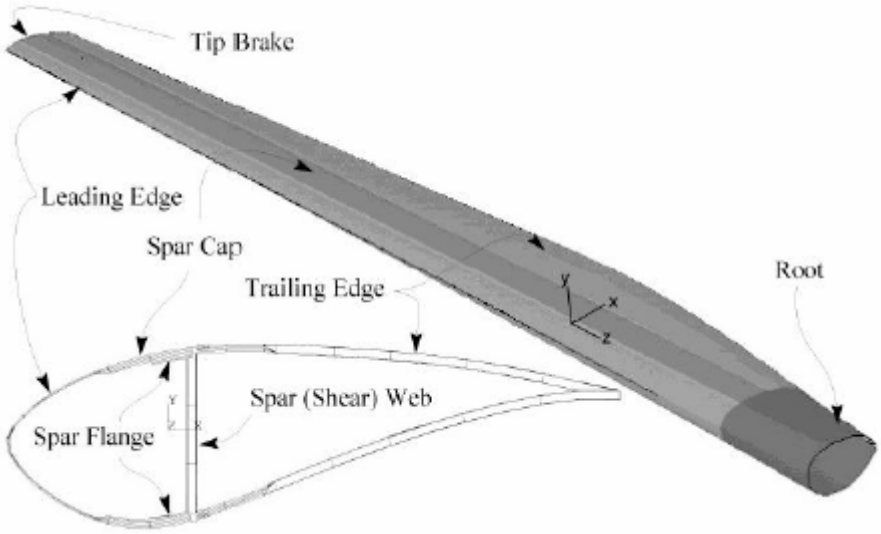


Figure 6: Blade construction [14].

The blade is made up of an upper and lower skin, a spar, and a spar cap. The skins provide the aerodynamic surface, as well as structural support. The spar and spar cap combine to form an I-beam that provides additional support in bending and in shear. The individual components are shown in Figure 7.

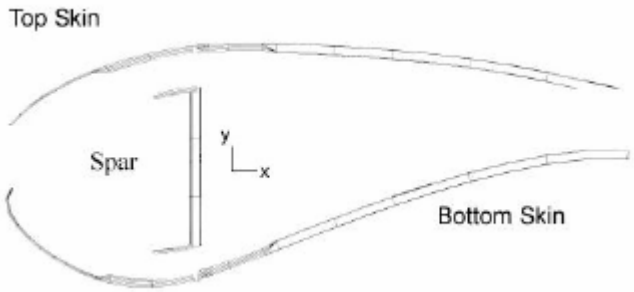


Figure 7: Blade cross section [14].

The most common materials used for turbine blades have been E-glass fibers with thermoset resins such as epoxy and vinyl-ester [5]. These materials have been used due to their cost and resistance to fatigue. As blades continue to increase in length, carbon fibers are becoming more important. In some cases, the blades are becoming so long that if the blade were made strictly of glass fibers it would fail under its own weight. The high strength and stiffness to weight ratio make carbon fiber a potential solution to this problem [5]. Although carbon fiber is more expensive, there are potential benefits that could come with its use that might offset this material cost.

CHAPTER 3

PROCESS MODELING BACKGROUND

Producing a successful part using RTM can be very challenging. Due to complex geometry, and the anisotropic permeability of the fabrics used, predicting the flow front though a mold is a difficult problem. As mentioned before, this is commonly done by experts who rely heavily on experience. A trial and error process is also used to detect and eliminate problems involving mold construction. In one such method a partial charge of resin is injected and allowed to set up. This is repeated using progressively more resin to create a series of parts with a progressing flow front. This process is very useful in identifying where vents need to be located or where more injection ports are required. For smaller parts, the cost of doing this may be insignificant as long as a new mold is not required. For parts where the absolute minimum process time is critical, as in automotive manufacturing processes, flow modeling is becoming more essential. This is also true for large parts where waste can have a significant cost and molds are very expensive. The best time to make changes to the design of a mold is before it is built.

Process modeling has been used with varying success for many years now. The liquid injection molding software (LIMS) developed by the University of Delaware is a modeling software that has been used to successfully model complex 2D parts [18,19]. This program is also developing means to model channels and account for fabric compression, as in more modern processes [20]. One advantage of this program is that it can use a finite element mesh generated by PATRAN so complex geometries can be modeled [18,20].

Unfortunately, even using commercially available software can be difficult for complex one-sided molding processes. Some existing finite element programs such as ABAQUS also have porous media fluid elements capable of orthotropic or anisotropic permeability tensors. For closed mold processes, this program could be used to model complex three dimensional geometries with little additional programming. However, for one-sided molding processes there would still need to be a large amount of manual programming. Other programs have been developed independently to model processes such as SCRIMP™ and VARTM [7,21,22,23]. These programs also use a finite element control volume technique to model the process. Changes in fabric properties during the process, as well as the resin distribution channels, are included in the models. However, they still result in a two dimensional model where the resin flows in the plane of the fabric between channels.

As was pointed out earlier, the processes with the greatest capability for very large parts are where the distribution channel covers the whole surface and the flow is though the thickness. No models were found that handle this type of process specifically. The goal of this work was to select and model a process that would be optimal for creating a large wind turbine blade. Due to the geometry of the upper and lower skins of the blade, it was decided that a flat rectangular plate would be a good approximation of the geometry for this study. Although not exact, it reduces the complexity of the problem by an order of magnitude by permitting a 2D model. In addition to being much easier to program, it is also very fast to run. This aids in examining how changing process parameters can influence the process. This geometry also lends itself to finite difference, or

control volume techniques which are much simpler to program than finite elements. The specific method used in this work is similar to the Hardy Cross method for analyzing piping systems [24]. The development of the control volume technique used in this study will be discussed in detail in the following sections.

Stokes flow

In the following development, the flow through various parts of the mold will be described by equations that have been derived from Navier-Stokes equation. The Navier-Stokes equation is:

$$\rho \frac{\partial u_j}{\partial t} + \rho\, u_k \frac{\partial u_j}{\partial x_k} = -\frac{\partial P}{\partial x_j} + \mu \frac{\partial^2 u_j}{\partial x_i^{\,2}} + \rho\, f_j \qquad (3.1)$$

Where :
ρ is density
u is velocity
x is the coordinate direction
μ is viscosity
t is time
P is pressure
f is the body force

For many situations the flow is steady, and the acceleration terms in equation 3.1 can be neglected. It can be shown by a dimensional analysis, that this is only valid for small Reynolds numbers. This results in a more simplified form known as Stokes flow equation [25]. In other cases such as flow through pipes and ducts with constant cross section, the resulting equation is the same as Stokes flow, but there is no restriction on the Reynolds number. This is referred to as Hagen-Poiseuille flow [25].

$$0 = -\frac{\partial P}{\partial x_j} + \mu \frac{\partial^2 u_j}{\partial x_i^2} + \rho f_j \tag{3.2}$$

This is the equation that is most used to determine velocities and pressure drops for internal flow problems.

Injection System Modeling

In modeling the resin flow for more traditional closed mold style processes, the injection system is typically unimportant. Since the resin can only flow though the fabric, which is relatively impermeable, the pressure drop in the hose is negligible. However, for processes with flow channels above the fabric the flow through the injection system is an important component of the process. Since the distribution channel in the pressure bag process has a high permeability, a large part of the pressure drop in the first stage of the process occurs in the hose system. Once the resin reaches the end of the mold and is forced to flow though the thickness, the pressure drop in the hoses can still be significant. Although the fabric has a low relative permeability, there is a very large cross sectional area. All the flow that goes into the fabric must first come through the injection system, which is why there is still a noticeable drop in pressure through the hoses.

In order to model the flow though the hoses, traditional pipe flow theory was used. In typical pipe flow analysis the head loss through a length of pipe is related to the velocity of the fluid in the pipe, and the friction factor. The head loss is the pressure drop through the section of length L, divided by the density of the fluid times gravity.

$$h_f = \frac{f\ L\ v^2}{D_{hose}\ 2\ g} \tag{3.3}$$

$$h_f = \frac{\Delta P}{\rho\ g} \tag{3.4}$$

Where :

h_f is the head loss

f is the friction factor

v is the average velocity

D_{hose} is the diameter of the hose

L is the length of the section

ρ is the fluid density

g is gravity

The friction factor depends on things such as the roughness of the pipe, the diameter, and the Reynolds number of the flow [26]. For turbulent flow the friction factor must be looked up on a Moody diagram. For laminar flow, the friction factor is a function of the Reynolds number only. Because of the high viscosity of the resin used in this study (300 cp), the flow was in the laminar regime in all the cases examined. The equations for the laminar friction factor and Reynolds number are:

$$f_{lam} = \frac{64}{\mathrm{Re}_D} \tag{3.5}$$

$$\mathrm{Re}_D = \frac{\rho\ v\ D_{hose}}{\mu} \tag{3.6}$$

Where :

Re_D is the Reynolds number based on diameter

μ is the fluid viscosity

The previous equations were then manipulated into a form that would be more useful in future modeling. This equation directly relates the average velocity through the pipe to the pressure drop through a given length of hose.

$$v = \frac{D_{hose}^{\ 2}}{32\ \mu}\frac{\Delta P}{L} \tag{3.7}$$

Equation 3.7 can also be derived from the Stokes flow equation. By integrating the Stokes flow equation and applying the appropriate boundary conditions, the following equation is formed [26].

$$v(r) = \frac{1}{4\ \mu}\frac{\Delta P}{L}\left(R^2 - r^2\right) \tag{3.8}$$

Where :

$v(r)$ is the velocity as a function of r

r is the radial position in the pipe

R is the outer radius of pipe

This equation can also be written in terms of the maximum velocity (at r = 0) as:

$$v(r) = v_{\max}\left(1 - \frac{r^2}{R^2}\right) \tag{3.9}$$

By integrating equation 3.9 over the cross sectional area, the average velocity through the pipe can be found to be one half of the maximum velocity. Thus, by equating equations 3.8 and 3.9, and substituting in the diameter and average velocity, equation 3.7 can be formed. Notice that in equation 3.7 the velocity is proportional to the change in pressure over a given length. This is similar to the relationship for flow through porous media where the proportionality is defined by a constant known as the permeability. This will be discussed more in the following sections.

In most applications, the injection system will be more complex involving multiple hoses and hose fittings. In order to find the flow rate though the entire system given a differential pressure, compatibility and conservation of mass are used. Through conservation of mass the velocity through each component in the system can be related by a ratio of areas. In order to satisfy compatibility the pressure drop though each section must add up to the total pressure drop through the entire system. Together, these two principles can generate an equation to describe the system as a whole.

The system used for this study involved a brass cross fitting with three barbed fittings and attached hoses. Both 6.35 mm ID and 9.5 mm ID hoses were used. Figure 8 is a schematic of the hose system as well as the parameters used to determine the flow equation. A photo of the injection manifold modeled here is presented in the experimental equipment section. In real piping systems such as this, involving elbows, expansions and contractions, minor loss terms are typically included to account for any additional pressure drop as a result of these changes. In the cases modeled in this study, the minor loss terms were found to contribute less than one percent of the total pressure drop and have been omitted from this analysis for simplicity, but could be included if significant [26].

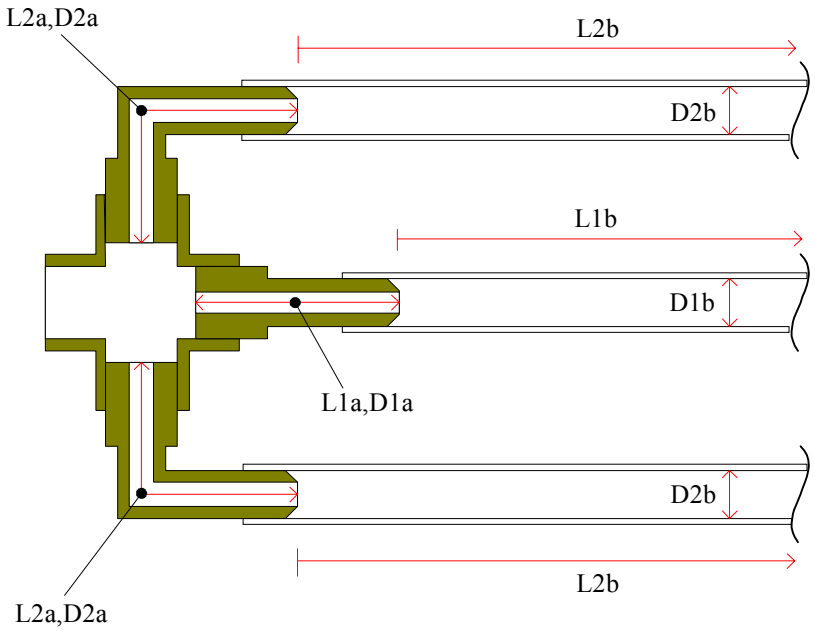


Figure 8: Injection system diagram.

By applying the governing equation as discussed to each component, the flow through each section (one fitting and one hose), can be described by:

$$Q_i = \frac{\Delta P_{hose}}{\mu}\left[\frac{A_{ia}}{32\left(\frac{L_{ia}}{D_{ia}^{\ 2}} + \frac{D_{ia}^{\ 2} * L_{ib}}{D_{ib}^{\ 4}}\right)}\right] \tag{3.10}$$

Where :

Q_i is the volumetric flow rate though section i

A is the cross sectional area

Ultimately, it was convenient to describe the flow as a function of the pressure drop, the viscosity, and a constant (K) which contains all the geometric information. This constant will be referred to as the equivalent permeability of the hose system since the resulting

equation is similar to Darcy's law [27]. Permeability is typically associated with flow through porous media. However, for modeling the flow through the hoses, channel, and fabric simultaneously, the equations must be in an analogous form. Although the physics involved in the flow through the hoses and fabric are different, the flow through both can be described by similar equations. The equivalent permeability term is used to lump all the geometric information together. This term is also different than most permeability terms because it contains the area and length terms as well. This can be done since the hoses will be full throughout the process. From equation 3.10, the term in brackets is replaced by the equivalent permeability term. This term simply defines the proportionality between the flux and the driving force as in many transport processes.

$$Q_i = \frac{\Delta P_{hose}}{\mu} K_i \tag{3.11}$$

Since the three sections of hose are in parallel, the total equivalent permeability is the sum of the individual permeabilities. It should be noted that permeability is not a resistance, it is a conductivity to flow, so the terms are added directly.

$$K_{hose} = \sum_{i=1}^{n} K_i \qquad i = 1,2,3...n_{hose} \tag{3.12}$$

and

$$Q_{hose} = \sum_{i=1}^{n} Q_i \tag{3.13}$$

thus

$$Q_{hose} = \frac{\Delta P_{hose}}{\mu} K_{hose} \tag{3.14}$$

Equation 3.14 is the desired result that will be used in subsequent modeling to combine effects of pipe flow, channel flow and fabric flow in a single model.

Channel Flow Modeling

The next flow regime in the process is through the distribution channel. This part of the process is again governed by Stokes flow, and has been extensively studied for many years. An equation similar to that obtained for flow though a circular hose can be obtained by solving the governing momentum equation. For a circular hose, or for an extremely thin flat channel, the solution is fairly straightforward. However, for more complex geometries such as semicircular, triangular, or rectangular the solution can become more difficult. Fortunately, the equations for shapes such as these are presented in most fluids textbooks. Most involve a term defined as the hydraulic diameter, which is a ratio involving the cross sectional area and the wetted perimeter. This term is important in calculating the Reynolds number of the flow. For the rectangular channel used in this study [26]:

$$D_h = \frac{4\,A}{P} = \frac{2\,h\,w}{h+w} \tag{3.15}$$

Where :
$A =$ cross sectional area
$P =$ wetted perimeter
D_h is the hydraulic diameter
h is the channel height
w is the channel width

There is also commonly a correction term for an aspect ratio as in the case of a rectangular channel. In this case the correction term is a function of the thickness to width ratio. The correction factor(C) for a rectangular channel as a function of its height to width ratio(h/w) is shown in Figure 9 [26].

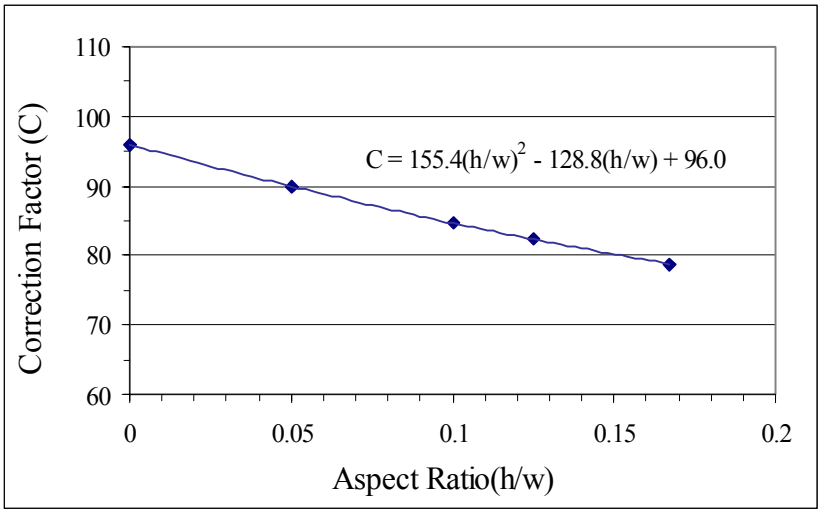


Figure 9: Correction factor for channel aspect ratio.

These terms were then used to find the friction factor which is the variable relating the pressure drop and velocity. The governing equation as presented in [26] is shown below.

$$\Delta P_{chan} = \frac{f\ v^2\ \Delta x}{2\ D_h} \tag{3.16}$$

Where :

f is the friction factor

ΔP is the pressure drop

Δx is the length of the channel

The friction factor for low Reynolds number is defined by:

$$f = \frac{C}{\mathrm{Re}_h} \tag{3.17}$$

Where :

C is the constant for a given aspect ratio

Re_h is the Reynolds number

For the rectangular channel, the Reynolds number is defined as:

$$\mathrm{Re}_h = \frac{\rho\, v\, D_h}{\mu} \tag{3.18}$$

This equation was then rearranged into a more useful form as in the case of the hose system. Again, the desired equation was one relating the flow rate to the gradient in pressure, and a constant containing the geometric information. The resulting equations are:

$$Q_{chan} = \frac{A_{chan}\, K_{chan}\, \Delta P_{chan}}{\mu\, \Delta x_{chan}} \tag{3.19}$$

and

$$K_{chan} = \frac{D_h^{\,2}\, 2}{C} \tag{3.20}$$

Where :

Q_{chan} is the volume flow rate

A_{chan} is the cross sectional area

K_{chan} is the equivalent permability of the channel

This technique of generating an equivalent permeability of a channel has been examined by Hammami, et al., for modeling the edge effect in conventional RTM [28]. Their study also examined the effect of the simultaneous flow into the fabric as the resin is flowing into the channel. The flow of the fluid into the fabric changes the velocity pro-

file in the channel, and thus the equivalent permeability. For cases where the channel is very small and the permeability of the fabric is large, they found that the effect of the transverse flow into the fabric dramatically changed the flow though the channel. In order to quantify when this effect needs to be accounted for, they introduced a transverse flow factor which was defined as:

$$\eta = \frac{12\, k_z\, m}{d^2} \tag{3.21}$$

$$\text{with} \quad m = \sqrt{\frac{k_z}{k_x}} \tag{3.22}$$

Where :

η is the transverse flow factor

d is the channel height

k_z is the fabric permeability in the transvese direction

k_x is the fabric permeabilitiy in the flow direction

m is a ratio of permeabilities

It was experimentally determined that for values of η < 5E-4 that the transverse flow into the fabric could be neglected. For the cases examined in this study the permeabilities are sufficiently small that the transverse flow can be neglected, thus equation 3.20 is valid.

Fabric Flow Modeling

Darcy Flow

The flow of resin through the fabric is governed by Darcy's law [27], which is very similar to the resulting equation for channel flow. Darcy's law expresses the flow of the fluid through the fabric by relating the velocity to the pressure drop, and the fabric

permeability which is a conductance to flow. The permeability is actually a second order tensor, meaning its value depends on the direction of the flow. For one dimensional flow through the thickness, Darcy's law is:

$$v = -\frac{K_z}{\mu}\frac{dP}{dz} \tag{3.23}$$

Where :

K_z is the fabric permability in the z direction

$\frac{dP}{dz}$ is the pressure gradient

For flow through the fabric, it is extremely difficult to calculate the permeability constant (K) by knowing only the geometric information. Micro-models exist for estimating the permeability of a fabric given fiber diameters, fiber spacing, and other relevant information [6,29,30]. However, these models are very complex and have varying accuracy. In addition, there must still be tests performed in order to determine some of the parameters needed as input to the models. The most accurate and direct way to determine the permeability is through testing. By knowing the velocity, pressure drop, and viscosity of a fluid moving through a fabric the permeability can be calculated. Because most RTM modeling has been done for closed mold processes, the permeability in the plane of the fabric was typically of the greatest concern [8,18,31,32,33]. For this reason, the majority of available permeability data is for flow in the plane. For the two-stage processes such as pressure bag molding and FASTRAC, the most important value is the permeability through the thickness. This is because the distribution channel covers the surface of the fabric so all the in-plane flow occurs in the channel and the flow in the fabric is primarily though the thickness. For a process such as SCRIMP™ where there may be a large spac-

ing between the flow channels the in-plane permeability would be more important. The in-plane permeability can be either higher or lower than the through thickness value depending on the fabric type and compaction pressure. Parnas et al. have found in general the in-plane permeability in the direction of the fibers is 6-8 times larger than it is for through the thickness [34]. However, if the flow in the plane is transverse to the fibers the permeability could be expected to be close to the through thickness value or possibly even less.

Saturated vs. Unsaturated Flow

Darcy's law was originally intended for modeling saturated flow of water through soil [27]. Because of this, it has some deficiencies when modeling unsaturated flow though a fabric. In order to use it to model this type of flow it must be modified slightly. In calculating the permeability, the velocity is determined by dividing the flow rate by the cross sectional area. The area used is the total flow area of the fabric. This means that the velocity in Darcy's law is the superficial velocity, or the velocity averaged over the whole area. Due to the presence of the fabric, the actual flow area is less than the total area. This means that the actual velocity of the fluid through the preform is higher than the superficial velocity because the flow area is reduced. This reduction in flow area can be determined by knowing the fiber volume fraction of the fabric. Actually, the term commonly used is called the porosity (e) of the fabric which is one minus the fiber volume fraction. The modified equation becomes:

$$v_{actual} = -\frac{K_z}{\mu\, e}\frac{dP}{dz} \tag{3.24}$$

Another additional term required to model unsaturated flow is the capillary pressure. This is a consequence of the wicking behavior of the fabric caused by surface tension. This tends to pull the resin along, which results in a higher apparent pressure than the applied pressure. The -dP term will be replaced by ΔP, recognizing the pressure drop is linear, and that the flow occurs from high to low pressure. Darcy's law is modified accordingly.

$$v = \frac{K_z}{\mu\, e}\frac{(\Delta P_{app} + P_{cap})}{dz} \tag{3.25}$$

Where :

ΔP_{app} is the drop in fluid pressure

P_{cap} is the capillary pressure

The capillary pressure is dependant on properties of the fabric and the resin. One equation for determining the surface tension as presented by [35] is

$$P_{cap} = \frac{F}{D_f}\frac{1-e}{e}\sigma\ \cos\theta \tag{3.26}$$

Where :

F is the form factor

D_f is the diameter of a fiber

σ is the surface tension

$c\cos\theta$ is the wetting angle

The fiber diameter, porosity, and form factor are all properties of the fabric, while the surface tension is a property of the resin. The wetting angle is a property of the resin and fabric. Its value can vary depending on the measurement method [35]. For the most accurate results in an infusion process, the dynamic contact angle is the most appropriate [36]. It is measured as the fluid is moving in relation to the solid interface. Both an ad-

vancing and receding angle can be determined. However, the static contact angle gives a very good approximation for the resin systems used in RTM, and is easier to measure [36]. Fortunately, the wetting angle is only dependent on the fabric material and not on the fabric architecture. Therefore, once the fabric properties are known for a given fabric, the capillary pressure can be calculated for any resin with that fabric if its surface tension and wetting angle are known. The form factor depends on the fabric architecture and whether the flow is along the fibers or transverse. Transverse flow typically has a form factor with a value from one to two [35]. The porosity is included because as the porosity decreases, the surface area to volume ratio increases, which increases the capillary pressure. Capillary pressure is not very temperature dependent since both the contact angle and surface tension are very weak functions of temperature [35,36,37].

Although the capillary pressure is typically much smaller than the injection pressure, it can change the results of a test by a noticeable amount. Some researchers have claimed that the capillary effect was negligible in their permeability tests while others have claimed capillary pressures had a significant effect [32,34,35,38,39]. The extent of this effect is going to vary depending on the fabric, the resin, and the injection pressures. Luo et al. conducted a study on the capillary pressures of a silicone oil and corn syrup with a couple of fabrics [39]. The largest capillary pressure they found was approximately 5 kPa for the silicone oil and was less for the corn syrup although they did not give a specific value. This is consistent with the result found by Rossell for the capillary pressure of a polyester resin transverse to the fibers of 3 kPa [18].

Another phenomenon of unsaturated flow arises from the fact that there is flow occurring between the fiber tows as well as within them. During a saturated permeability test, the flow in both these regions is factored into the total permeability. Because of the presence of macroscopic channels between tows and microscopic channels within them, a fabric is commonly referred to as a dual scale porous media. The consequence of this dual nature in unsaturated flow is that the flow in the macroscopic channels will advance much faster than the inside of the tows can be saturated. Cairns et al. found that the equivalent permeability of the channels between tows could be an order of magnitude larger than the permeability within the tow [6]. This effect is shown in Figure10.

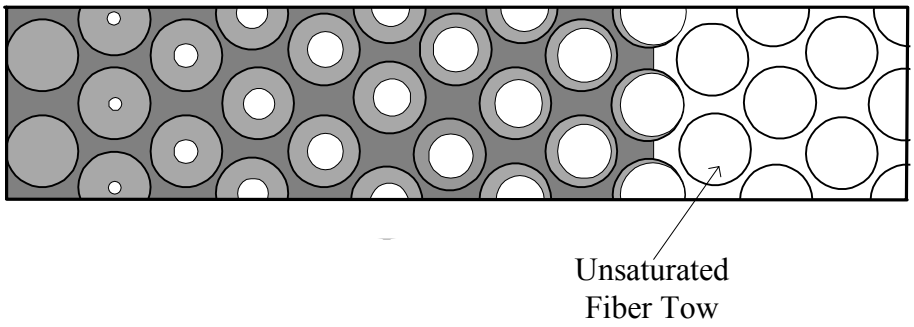


Figure 10: Illustration of dual scale flow.

This can be a problem in modeling as well as for part quality. Acheson et al. found that the effect on flow modeling was minor [40]. This is mostly due to the fact that this only occurs at the flow front, and not in the saturated regions. It was determined, however, that this could have a large impact on part quality. This is why the use of a vacuum pump has become so critical in reducing porosity in RTM processes. The use of a vacuum reduces the amount of air that is trapped as the resin encircles a fiber tow.

Fabric Compressibility

Fabric compressibility is very important in all RTM processes, and affects both the material and processing properties of the part. As the fabric is compressed by fluid pressure or the mold surface the fibers get compacted and the fiber volume fraction increases. This decreases the thickness of the part, decreases the permeability, and decreases the porosity. Compressibility is possibly more important to understand in one-sided molding processes than in closed-mold processes [40]. In a closed mold process the permeability and fabric thickness are fixed at a certain value which is determined by the mold gap. Throughout the process the permeability is a constant and independent of the injection pressure. In one-sided molding processes the compaction of the fabric can lead to several important phenomena. In processes where the flow is in the plane of the fabric such as VARTM and SCRIMP™, a part with non-uniform thickness can be created since the net compaction pressure varies throughout the mold [40].

In processes where the resin is forced though the thickness, the pressure applied to the fluid is also the pressure compacting the fabric. Therefore, the permeability and fabric thickness can change throughout a process and depend on the pressure at which the process is taking place. This can create an interesting competing mechanism in these types of processes. According to Darcy's law, an increase in pressure will increase the velocity of the fluid though the fabric. However, increasing the pressure of the fluid will increase the compaction pressure and lower the permeability. It could be possible in certain cases for an increase in pressure to increase injection time, although this is not common. For most fabrics the decrease in thickness tends to compensate for the de-

creased permeability in through thickness flow. The effect of compaction on permeability is very dependant on the fabric architecture, which means some fabrics are more affected than others.

Fabric compaction also affects the porosity of the fabric, which will affect the saturation time for unsaturated flow. This fact adds yet another complication to the problem. Although permeability decreases with compaction, the decrease in porosity can increase the velocity of the fluid through a preform. Decreasing the porosity also increases the capillary pressure. However, in most cases these effects are minor.

As a fabric is compressed there are three distinct regimes that have been identified [15]. The first is where the spacing in the fabric caused by the stitching and weaving is compressed. This occurs at very low pressures, and results in fiber on fiber contact. This region is also very linear in nature. In the second regime, both the solid and the voids are compressed. This is the most complex region, and is the most studied. Very complex models have been generated to predict the behavior of the fabric in this region. Although the fibers are touching, they are still moving due to fiber bending, slippage, and nesting [41]. The third region is where the fabric has been fully compressed. Most fabrics are fully compressed with 1-2 MPa pressure [15]. In the third regime, all the fibers have been manipulated into a stable position and cannot be moved any further. The only compression occurring in this regime is due to the solid material compressing. Many fabrics have compressed to half their original thickness by this point [15].

Overall, the relationships between pressure, ply thickness, and fiber volume fraction are very non-linear. In order to get accurate values for fabric compaction many tests

may be required. Typically, the results from these tests can be represented with logarithmic or power law fits [15,42]. However, the results from these fits do not contain any real physical significance in the parameters used to fit the curves. They may also only fit limited regions of the data, with problems in extrapolating. Chen et al. have proposed a method for creating fabric compaction models using four to five parameters [15]. These parameters are the initial fiber volume fraction, the final fiber volume fraction, the initial fiber perform bulk compressibility, the fiber compressibility and an empirical index. The initial and final fiber volume fractions can easily be determined by the areal density, the fiber density, and the ply thickness.

$$s_0 = \frac{\varsigma}{\rho\, T_0} \tag{3.27}$$

and $$s_f = \frac{\varsigma}{\rho\, T_f} \tag{3.28}$$

Where :

s_0 is the uncompressed fiber volume fraction
s_f is the fully compressed fiber volume fraction
ς is the fabric aereal desity
T_0 is the uncompressed fabric thickness
T_f is the fully compressed fabric thickness
ρ is the density

The fiber compressibility is simply the modulus of the fiber material. The bulk compressibility must be experimentally determined by taking a data point in the first linear regime. The empirical constant k is the only constant that would require a number of tests to determine. Fortunately, it has been found that for all the E-glass fabrics tested and for AS4 carbon that $k = 2$. This means these fabrics can be represented by only four

constants. The procedure for determining and combining these constants is described in detail in [15]. The resulting equations are:

$$P = \frac{1}{C_b(T)}\left(1 - \frac{T}{T_0}\right) \tag{3.29}$$

and

$$P = \frac{1}{C_b(s)}\left(1 - \frac{s_0}{s}\right) \tag{3.30}$$

where

$$C_b(T) = \frac{1 - \left(s_0 \frac{T_0}{T}\right)}{1 - s_0}\left(\frac{1 - \frac{T_f}{T}}{1 - \frac{T_f}{T_0}}\right)^k C_{b0} + \left(2 - \frac{s_0 T_0}{T} - \left(1 - \frac{s_0 T_0}{T}\right)\left(\frac{1 - \frac{T_f}{T}}{1 - \frac{T_f}{T_0}}\right)^k\right) C_s \tag{3.31}$$

and

$$C_b(s) = \frac{(1-s)(s_f - s)^k}{(1-s_0)(s_f - s_0)^k} C_{b0} + \left(2 - s - \frac{(1-s)(s_f - s)^k}{(s_f - s_0)^k}\right) C_s \tag{3.32}$$

Where :

P is the compaction pressure

$C_b(T)$ is the bulk compressibility based on thickness

$C_b(s)$ is the bulk compressibility based on fiber volume fraction

C_{b0} is the initial bulk compressibility

C_s is the fiber compressibility

With these formulas, curves for ply thickness and fiber volume fraction versus pressure can be generated. A similar model has also been developed by Gutowski which also uses the uncompressed and fully compressed fiber volume fractions [40,43]. This relationship is described by

$$\sigma_z = A_s \frac{\left(\sqrt{\frac{s}{s_0}} - 1\right)}{\left(\sqrt{\frac{s_f}{s}} - 1\right)^4} \tag{3.33}$$

Where :

σ_z is the compaction stress

A_s is an experimentally determined constant

Another phenomenon that is important to be aware of is the viscoelastic behavior of fiber performs. Bickerton et al. found that dry fiber mats had rate dependant compaction properties, as well as hysteresis [41]. In many manufacturing processes this could add one more complication to any process modeling. This could be especially important in SCRIMP™ where the fabric starts in a compressed state, and then is assumed to bounce back to its uncompressed state as the fabric is saturated. The effect of hysteresis could mean the fiber mat would not bounce back to its original thickness. This also has importance in permeability testing which will be discussed later.

Calculating Saturation Time

The ultimate goal of understanding the flow through a fabric is to be able to predict the time required to saturate a part of a given thickness or length. Although the process examined here involves more than just flow through the fabric, some valuable lessons can be learned by looking at the fabric flow independently in one dimension. By manipulating the modified Darcy equation (equation 3.25) the saturation time required for a part of a given thickness was created. First it was recognized that

$$v = \frac{dz}{dt} \tag{3.34}$$

It can also be shown that for this particular problem dP/dz can be re-expressed as

$$\frac{dP}{dz} = \frac{\Delta P}{z} \tag{3.35}$$

This comes about because as the fluid moves through the preform dz is constantly increasing while dP is fixed. Thus dP/dz is constantly decreasing and the fluid is moving slower and slower. This effect is shown in Figure 11.

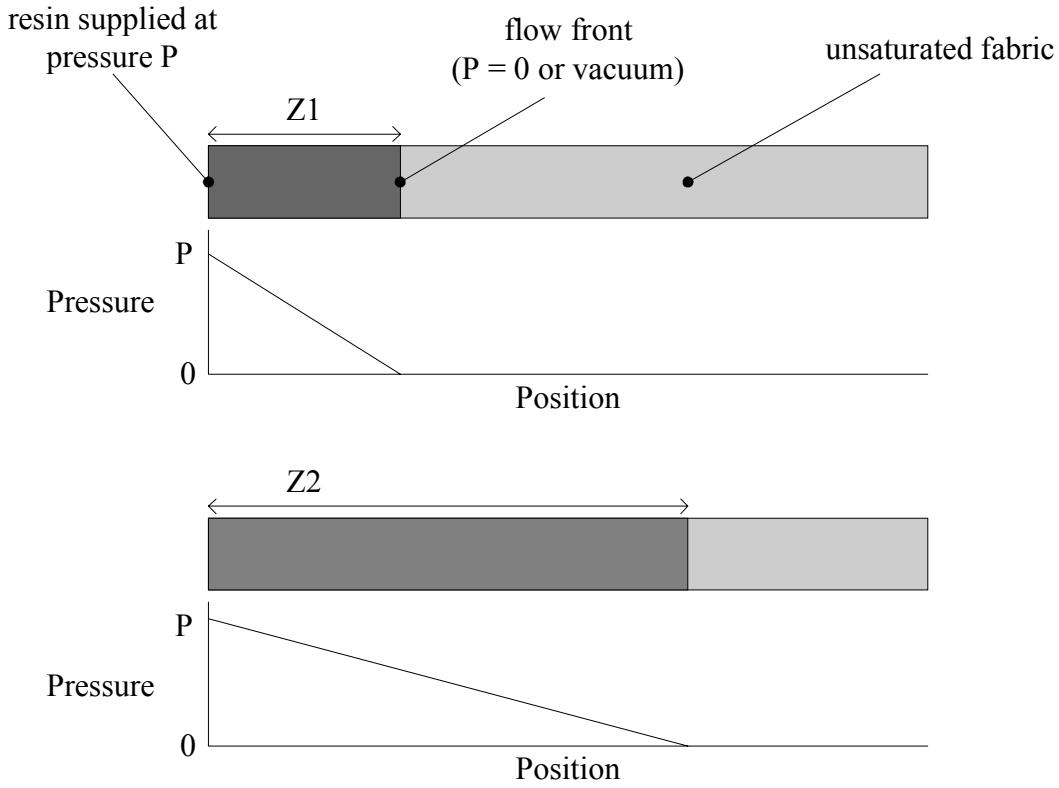


Figure 11: Pressure gradient as flow front progresses.

Equation 3.25 can now be expressed as

$$\frac{dz}{dt} = \frac{K_f}{\mu\, e}\frac{\left(\Delta P + P_{cap}\right)}{z} \tag{3.36}$$

which can be separated into

$$z\, dz = \frac{K_f}{\mu\, e}\left(\Delta P + P_{cap}\right) dt \tag{3.37}$$

Finally, the left side of the equation is integrated from z = 0 to z and the right side is integrated from t = 0 to t giving

$$\frac{z^2}{2} = \frac{K_f}{\mu\, e}\left(\Delta P + P_{cap}\right) t \tag{3.38}$$

$$\text{or} \qquad t = \frac{z^2\ \mu\, e}{\left(\Delta P + P_{cap}\right) K_f\ 2} \tag{3.39}$$

This is a very important result since it shows how the saturation time is a function of the part thickness or length squared. This is why it is very hard to make long parts when flowing through the fabric only. This equation can be useful in determining the limiting cases for RTM processes.

Comprehensive Model

Methodology

The purpose of examining the flow of the resin through the different regions was to come up with governing equations for each and then combine them in a comprehensive model. Since resin is flowing though the injection system, distribution channel and fabric simultaneously, a model was needed that could simulate this interaction. This becomes a

very complex problem because of the transient nature. The flow front is constantly moving and the pressure at any point in the system is constantly changing. Additional complexity comes from the fact that the fabric's thickness, porosity, and permeability are all changing throughout the process. The method used to solve this problem was to do it numerically in very small time steps and treat each instant as a quasi-steady-state problem. Each part of the system was broken into cells of hose, channel, and fabric. Each region has its own governing equation. The method used to solve this problem is similar to the Hardy Cross method for flow through a system of pipes [24]. In the Hardy Cross method, each section of pipe is given an effective permeability as discussed earlier, and the pipe junctions are treated as nodes. Several pressures and flow rates are assigned to the nodes as boundary conditions, and the rest are unknowns. The unknowns are determined simultaneously, and may require iterations if there is non-linearity in the flow equations, as in turbulent flow. The main difference between the Hardy Cross method and the one used here, is that the resistance to flow through the fabric is constantly changing due to the transient nature, and the number of cells engaged is increasing as the flow progresses. A schematic of how the mold was divided is shown in Figure 12.

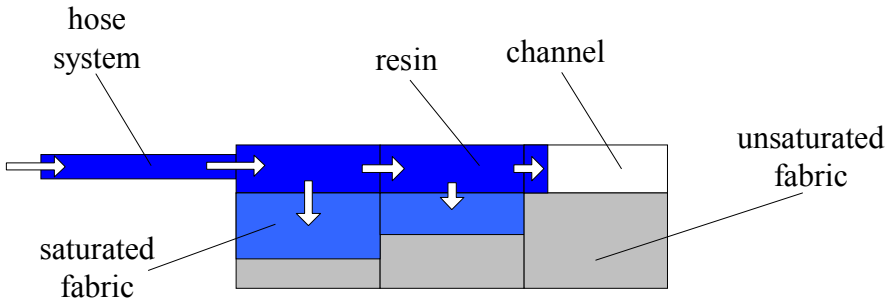


Figure 12: Division of mold into cells.

One important simplification to note is that the fabric is only divided along the length to create fabric columns. These columns are not divided through the thickness. This is important because it greatly reduces the number of cells required to solve the problem. If the fabric were divided vertically, a very large number of cells would be required for accurate results. Since the fabric was not divided into cells, the position of the fluid front in each cell is stored separately after each time step. The reason that this could be done for the fabric and not in the channel is because the pressure gradient in the fabric could be assumed to be linear because the flow in the plane of the fabric is small. For almost all cases examined, this assumption would cause only very minor error since almost all the in-plane flow is taking place in the channel above the fabric. This could not be done in the channel because as the fluid passes over each column of fabric some of the fluid enters the fabric. This means the flow rate though the channel is decreasing from left to right in Figure 12. Since the flow rate is decreasing, the pressure drop is also decreasing resulting in a nonlinear pressure profile above the fabric.

Building the Matrix

Because of the transient and non-linear behavior in the problem, all the unknown flow rates and pressures at each point were determined simultaneously for each time step. For the real model the channel was broken into many cells. For illustration purposes, the three cell model of Figure 12 will be used to show how the solution matrix was constructed. In order to fully define the problem, four sets of equations were used. These were compatibility, conservation of mass, the governing flow equations, and the boundary conditions. In order to solve the problem it is important to know the pressures and

thus the flow rates of the fluid at each cell boundary. Figure 13 is Figure 12 broken into its individual cells, with all the relevant variables labeled.

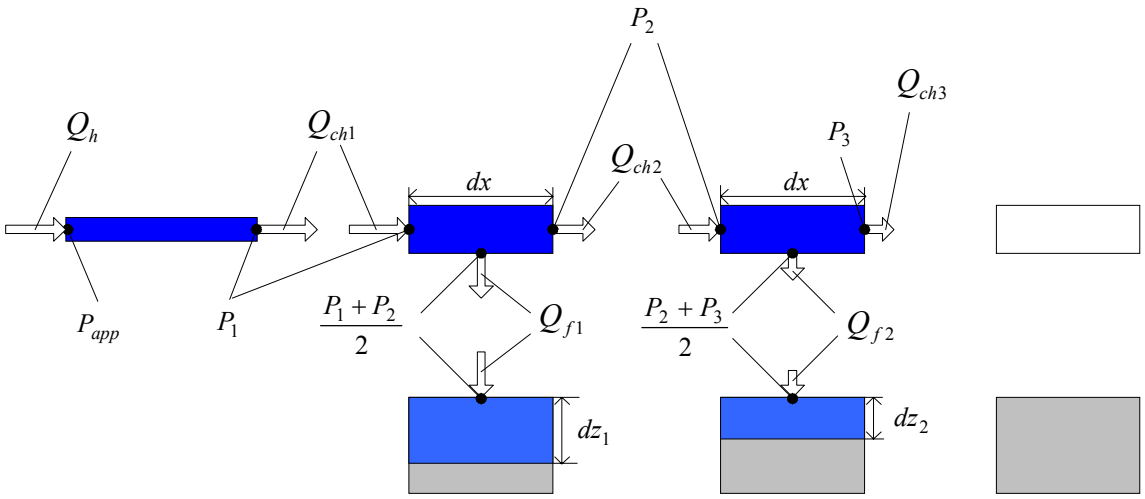


Figure 13: Schematic of flow model with variables labeled.

Fortunately, compatibility implies that all the properties at adjacent cell boundaries must be equal as indicated in Figure 13. It should be noted that the pressure over the fabric is defined as the average pressure from the cell above it. By conservation of mass, the input to each cell is equal to the output since no accumulation is occurring. This provides the following equations for the three cell model in Figure 13.

$$Q_h = Q_{ch1} \tag{3.40}$$

$$Q_{ch1} = Q_{ch2} + Q_{f1} \tag{3.41}$$

$$Q_{ch2} = Q_{ch3} + Q_{f2} \tag{3.42}$$

The next step in determining the unknown quantities was to recall the governing equations determined for each region. Here is where it was helpful to have all the equations in

an analogous form where the flow rate is proportional to the equivalent permeability and the gradient in pressure. The hose system is treated as a single cell described by

$$Q_h = \frac{K_h \left(P_{app} - P_1\right)}{\mu} \tag{3.43}$$

Each cell of the channel is described by

$$Q_{ch2} = \frac{A_{ch1}\ K_{ch1} \left(P_1 - P_2\right)}{\mu\ dx} \tag{3.44}$$

$$Q_{ch3} = \frac{A_{ch2}\ K_{ch2} \left(P_2 - P_3\right)}{\mu\ dx} \tag{3.45}$$

And each fabric column is described by

$$Q_{f1} = \frac{A_f\ K_{f1}}{\mu} \frac{\left(\frac{P_1 + P_2}{2} + P_{cap}\right)}{dz_1} \tag{3.46}$$

$$Q_{f2} = \frac{A_f\ K_{f2}}{\mu} \frac{\left(\frac{P_2 + P_3}{2} + P_{cap}\right)}{dz_2} \tag{3.47}$$

In order to solve for the unknown values of pressure and flow rate the boundary conditions were also included in the solution matrix. The boundary conditions changed depending on what point of the process was being looked at.

Before the resin reaches the end of the channel

$$P_3 = 0 \tag{3.48}$$

Once the resin reaches the end of the channel

$$Q_{ch4} = 0 \tag{3.49}$$

These equations were then simplified and put in matrix form. The compatibility equations were not included individually, but are embedded in the final equations in the matrix. The equations were expressed in the form.

$$[A]\{x\}=\{B\} \tag{3.50}$$

Where {x} are the unknown flow rates and pressures. The expanded matrix is shown below in Figure 14. The case shown is for before the resin reaches the end of the channel.

$$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & -\frac{A_f K_{f1}}{2\mu\, dz_1} & -\frac{A_f K_{f1}}{2\mu\, dz_1} & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & -\frac{A_f K_{f2}}{2\mu\, dz_2} & -\frac{A_f K_{f2}}{2\mu\, dz_2} \\ -1 & 0 & 1 & -1 & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 1 & -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & -\frac{A_{ch} K_{ch}}{\mu\, dx} & \frac{A_{ch} K_{ch}}{\mu\, dx} & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & -\frac{A_{ch} K_{ch}}{\mu\, dx} & \frac{A_{ch} K_{ch}}{\mu\, dx} \\ 0 & 0 & 1 & 0 & 0 & \frac{K_h}{\mu} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} Q_{f1} \\ Q_{f2} \\ Q_h \\ Q_{ch2} \\ Q_{ch3} \\ P_1 \\ P_2 \\ P_3 \end{pmatrix} = \begin{pmatrix} \frac{A_f K_{f1} P_{cap}}{\mu\, dz_1} \\ \frac{A_f K_{f2} P_{cap}}{\mu\, dz_2} \\ 0 \\ 0 \\ 0 \\ 0 \\ \frac{K_h P_{app}}{\mu} \\ 0 \end{pmatrix}$$

Figure 14: Expanded matrix for 3 cell example.

By solving this matrix, all the unknown flow rates and pressures are calculated. These are then used to find the new positions of the fluid fronts at the next time step. The matrix is then recreated using the new values of the fluid fronts and this process is repeated. It should also be noted that the matrix shown is only for the case where two cells of channel contain resin. Once the resin fills the next cell, the matrix must grow to incorporate the new cell. In the real model the matrix starts out with one or two cells of channel full and

continues to grow as more cells are engaged. For example, a model with the channel divided into 100 divisions will start with an 8x8 matrix and end up with a 302x302 matrix once the fluid reaches the end of the channel.

For stage two, when the inlet is closed off and pressure is applied to the bagging, the matrix is no longer necessary since theoretically the pressure at each point in the channel is the same. This means there is no flow in the channel and only flow into the fabric. Since the pressure above the fabric is the applied pressure, there is no need to solve for it. In order to find the flow into each fabric column, at this point Darcy's law is used with the specific permeability and dz of each cell. Again, as the fluid reaches the bottom of a cell, the permeability is set to zero. The model is run until the fluid reaches the bottom of the last column. The structure of the program is illustrated schematically by a flow chart in Figure 15.

One step of particular importance in the model is the accounting for fabric compression. Most importantly, fabric compression changes the fabric permeability and thickness. In the model, the properties of the fabric were changed for each column after each time step. The properties were adjusted according to the pressure above each column of fabric. Since compression of the saturated fabric can take a long time, only the unsaturated fabric was compressed at each step. Although this means the fabric behind the flow front could have a varying permeability, it was assigned a constant value. When the fabric is compressed, there must be a new volume of fluid injected into the channel to fill the new volume created. This was also accounted for in the model. In Figure 16 the propagation of the flow front is shown at three different times in a process.

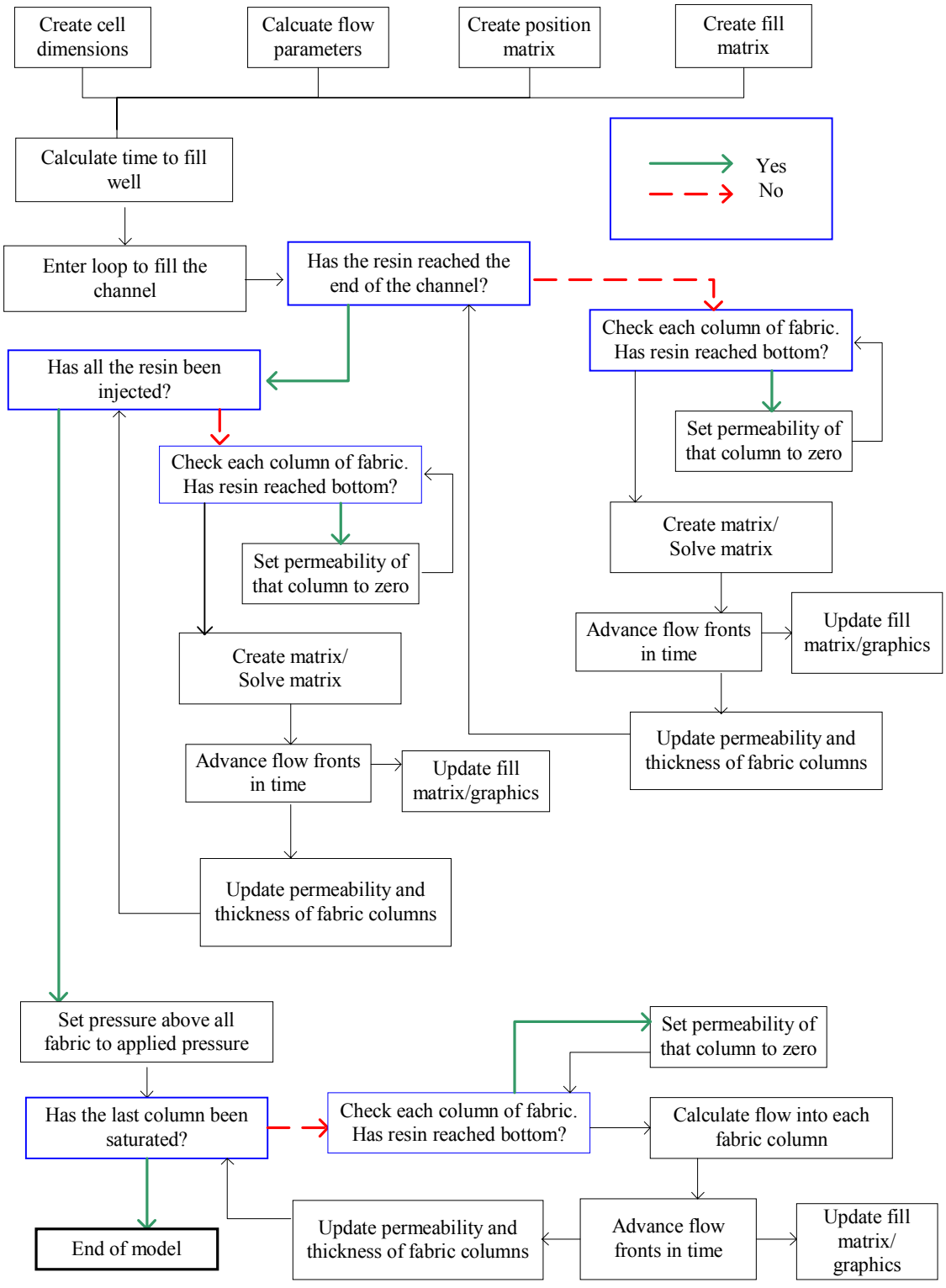


Figure 15: Flow chart for model.

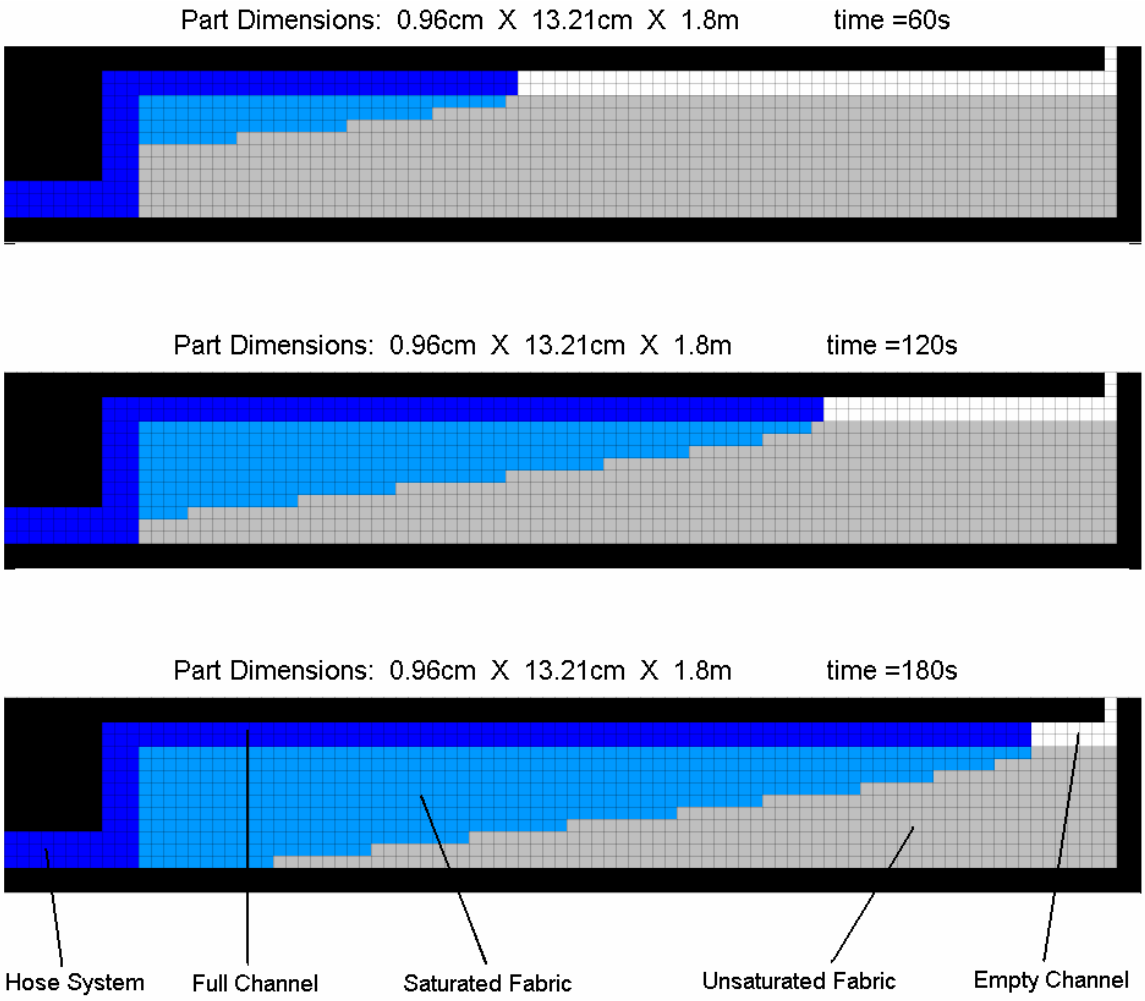


Figure 16: Example output from model at three different times.

Also included in the model output is a plot of pressure vs. position which shows where the major pressure drops are at different times in the process. The pressure drop in the hose system during stage one and the pressure profile over the fabric are illustrated in Figure 17.

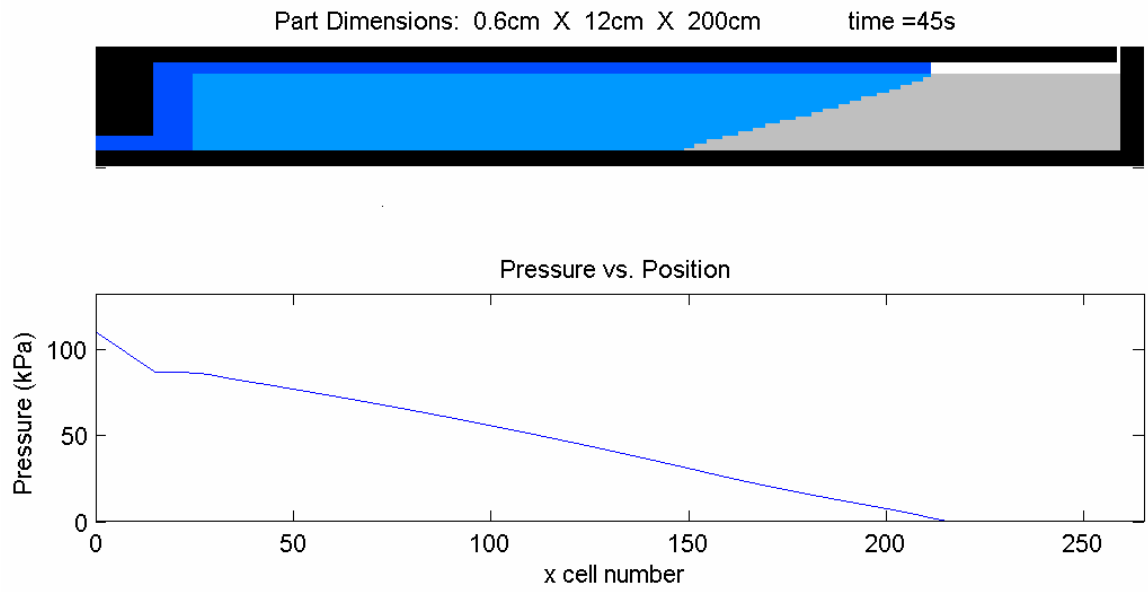


Figure 17: Pressure profile in hose and channel.

Assumptions

There are several assumptions made in the model that should be identified at this point. The first is that the flow in the plane of the fabric is small. In most cases this should lead to a negligible error, since the in-plane flow occurs in the channel, and the flow in the fabric occurs through the thickness. This is typical of high volume infusion processes. It is also assumed that the equation for the channel flow is valid despite the flow into the fabric. For the cases considered, this should be a good assumption based on the work done by Hammami et al. [28]. Another assumption is that the permeability everywhere is the same. The permeability values used in the model are only average permeability values. Therefore, some regions of the mold may saturate faster than predicted, and others slower. The more plies of fabric that are included in the part, the less

variability. The model also does not account for any fluid flowing around the edges of the fabric, or "racetracking." Racetracking could lead to a non-uniform flow front which could trap air pockets in the part. Because the results of racetracking would be so undesirable, it was assumed that proper precaution would be taken to minimize this effect. Possibilities for accomplishing this will be discussed later. In some cases, the model uses average values to represent things that change throughout the process such as the resin viscosity and pressure.

CHAPTER 4

EXPERIMENTAL PROCEDURES AND EQUIPMENT

Test Fluid

For all the experiments carried out in this work, a mixture of corn syrup and water was used to simulate resin. The corn syrup was chosen because it would not harm any of the testing equipment, it was easy to clean up since it was water soluble, and it was easily disposed of.

This mixture has also been found to be Newtonian, which is important since most resins are also Newtonian before they cure [39]. The NIST database on fabric permeability also used corn syrup as a test fluid, and this test fluid has accepted validity as a simulated resin [9,31,34,38,39,44]. It has also been found that aqueous corn syrup has similar wetting behavior as resin [9,39]. Silicone oil is also a popular test fluid [8,32,36,39,42].

Another important aspect of the test fluid is the effect of temperature on viscosity. Both the corn syrup and resin can be dramatically affected by temperature [35,39]. An example of the effect of temperature on viscosity for the fluid used in these tests is shown in Figure 18. In this case, a one degree Celsius change in temperature corresponds to about a 10% change in viscosity. Although the viscosity is fit well with a linear function in this range, over a larger interval viscosity is typically a logarithmic function with temperature [35,39].

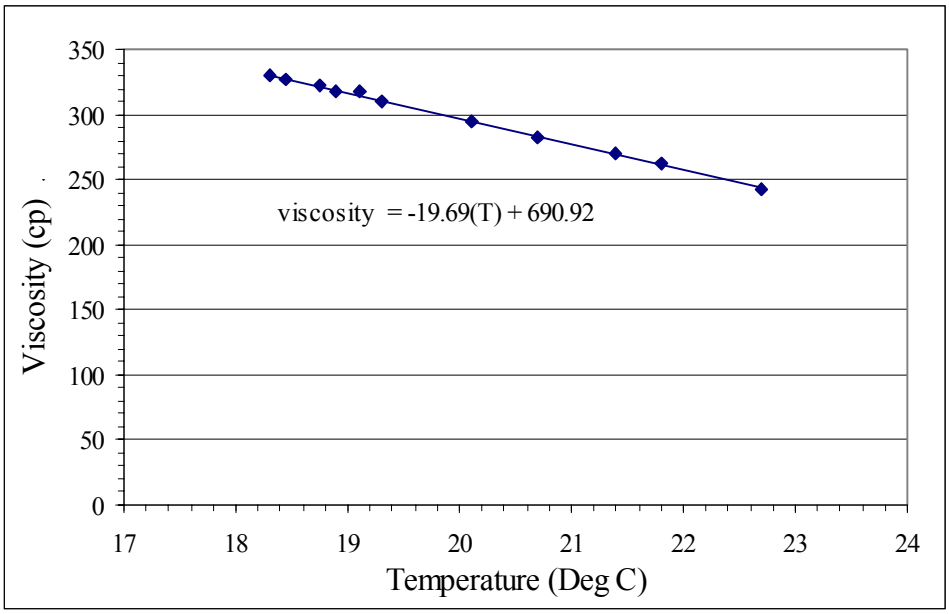


Figure 18: Effect of temperature on viscosity.

Because of this effect, it was important to monitor the temperature of the fluid throughout each test to determine the viscosity of the resin within the test apparatus. For temperature measurements Omega K-type thermocouples were read with an Omega BS6001 multi-channel thermocouple readout. Before each test, the fluid was characterized to generate a viscosity vs. temperature curve as in Figure 18. A Gilmont 100-1000 cp GV-2300 falling ball viscometer was used to determine the fluid viscosity. It was very important to keep the fluid at a stable temperature during a test. To accomplish this, the viscometer was placed inside a graduated cylinder filled with water during a test. The temperature of the water bath could be used as the fluid temperature, or the fluid temperature could be measured directly. As long as enough time was given for the system to come to equilibrium, the two temperatures were the same.

By knowing the temperature of the fluid during the test, the corresponding viscosity could be determined and used for calculations. In practice, this strong temperature dependence could lead to significant error when applying a flow model to a real manufacturing process. If the resin or the mold is heated beforehand there could be a large amount of heat transfer occurring, and large temperature differences throughout the mold. In this case it would not be accurate to assume a constant viscosity, and may be very difficult to predict how the viscosity is changing throughout the mold.

One aspect of a resin's behavior that was not simulated with the corn syrup was the changing viscosity with time. With a real resin, the viscosity changes constantly with time due to cross linking and the change in temperature caused by the reaction [45]. This could have major implications in modeling a real process. Although this effect was not modeled, it could be done easily by making the viscosity a function of time to match a given resin.

Injection System Tests

In order to test and validate the flow model created for the injection system a series of simple tests were performed. A PVC pressure pot was filled with resin and a constant pressure was applied to the fluid with compressed air. At the outlet of the pressure pot a cross fitting with three outlets and a pressure port was used. The pressure in the fitting was measured using an Omega 0-35 kPa PX139 pressure transducer. The transducer was calibrated using an Omega 0-100 kPa type T precision test gauge. This fitting is shown in Figure 19 and was the basis for the development of equation 3.14.

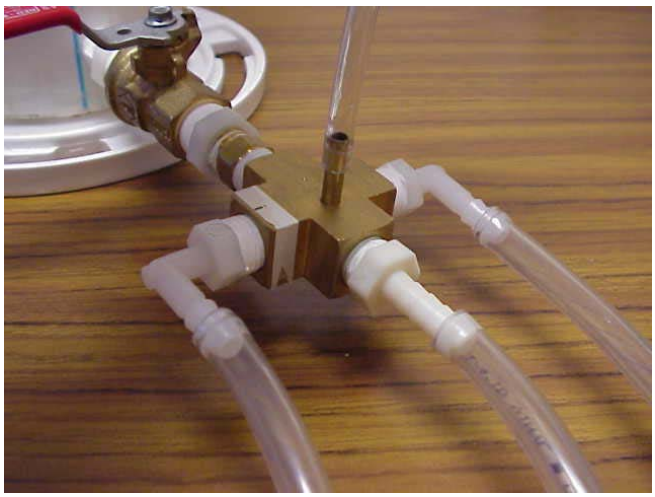


Figure 19: Injection manifold.

During the test the pressure on the tank was held constant by regulating the air pressure. The ends of the hoses were placed in a graduated cylinder open to atmospheric pressure. This means that the pressure drop in the hose system was equal to the pressure measured by the pressure transducer in the manifold. A valve just up from the cross fitting was opened for a fixed amount of time, and the corresponding volume of fluid passed though the system was recorded. Thermocouples were placed in the resin tank and at the outlet of the hoses to calculate an average temperature and viscosity of the fluid. The results from these tests were then compared to the predictions from equation 3.14. The injection system was tested using 6.35 mm and 9.5 mm hoses.

Channel Flow Tests

The next element of the model to test was the flow channel. As mentioned before, the channel used for these tests was a thin rectangular channel. A transparent test mold was created using polycarbonate sheets reinforced by steel clamps. A polycarbonate spacer

was placed inside the mold to take the place of the fabric to create a thin channel above it. A schematic of the test setup is shown in Figure 20.

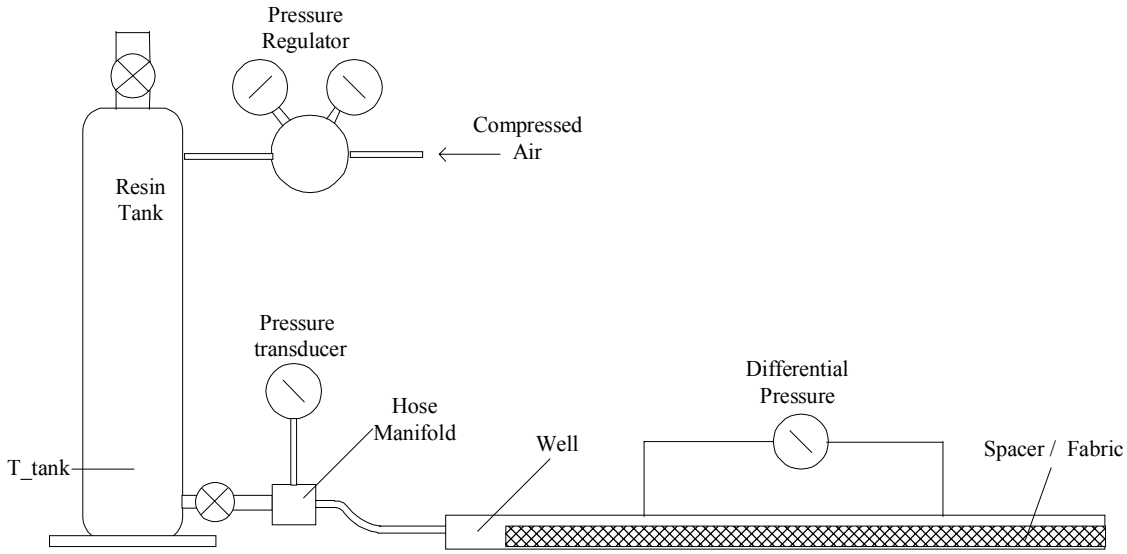


Figure 20: Schematic of channel flow experimental setup.

The test mold was used in two ways. The first was the transient test where the time for the resin to fill the mold was calculated and then verified. The second was in a steady state mode where the resin flowed continuously through the mold and the pressure gradient between two points was measured. For both tests, thermocouples were placed in the resin tank and at various locations within the channel. A time weighted average of the thermocouple readings was used to give a representative viscosity of the fluid during the test. For the transient test, the time required for the resin to reach the end of the mold was determined using equations 3.14 and 3.19. Since the hose system is full throughout the process the equivalent permeability of the hoses is fixed. In the channel, the flow front is moving so the pressure gradient is changing throughout the process. This equa-

tion is separated and integrated in the same fashion as Darcy's law was to form equation 3.39. Again, the time required is a function of the length of the channel squared. The resulting equation is:

$$t_{tot} = \frac{\mu}{P_{app}}\left(\frac{L_{chan}{}^{2}}{2 * K_{chan}} + \frac{A_{chan} * L_{chan}}{K_{hose}}\right) \tag{4.1}$$

For the steady state tests equation 3.16 was used directly.

Fabric Flow Tests

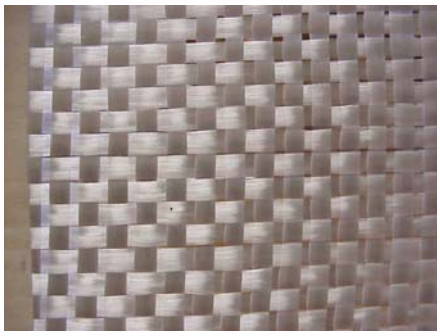
Fabrics Tested

For the permeability tests conducted, an assortment of fabric architectures were tested. The testing focused on thick materials that might be used on very large structures such as wind turbine blades. The fabrics tested included a unidirectional fabric stitched to a thin random mat, a woven roving, a double bias fabric, and a tri-axial woven carbon fabric. The fabrics tested are shown in Figure 21.

In addition to testing existing fabrics, another part of this study was to look at alternative ways to build up a part that might be more appropriate for large structures. One idea was to create a composite made with an arrangement of pre-cured strips and glass plies. In addition to possible manufacturing advantages, this concept could increase strength by reducing fiber waviness caused by stitching and processing. Preliminary testing has demonstrated the ability to create thick parts that are built up rapidly, have high permeability, and high strength. For testing, strips 1.5 mm thick and 22 mm wide were arranged in a staggered pattern with a ply of D155 at 45 deg. placed between each layer.

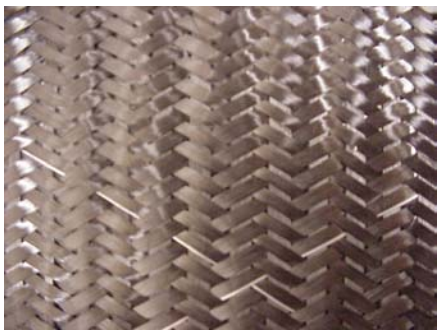
The D155 ply had every other tow removed to create flow channels within the part. A diagram of the cross section is shown in Figure 22.

Uni+mat (Ahlstrom 42024L/M50)



Woven Roving (Fiberglast #223)

Double bias (Knytex DB240)



Woven triax carbon

Figure 21: Fabrics tested for permeability.

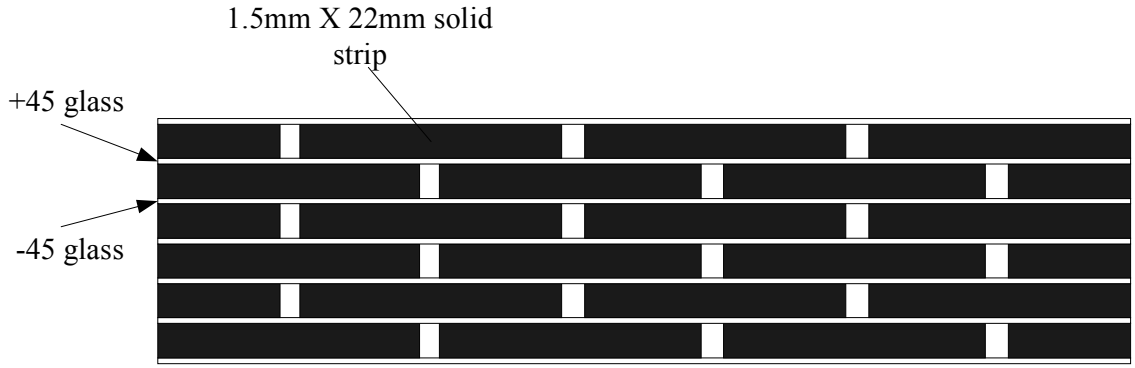


Figure 22: Cross section of hybrid composite stack.

Fabric Compaction Data

In calculating the fabric permeabilities and in further modeling, it was important to know how each fabric behaved under pressure. The fabric compaction data used for this study was taken from tests reported in reference 10. This data was obtained by placing various weights on a fabric mat just after it had been wet out by hand. This created regions with varying compaction pressures which altered ply thicknesses and fiber volume fractions. The ply thickness and fiber volume fractions were then measured after the part had cured.

Air Permeability Tester

The first testing apparatus constructed to measure permeability was intended to be used with air. The goal was to have a permeability tester that could test a wide variety of fabrics very quickly. By using air, there would be no messy cleanup between tests. In addition, fabric coupons could potentially be reused to perform different tests. The fabric coupons used were round with a diameter of about 6 cm. This allowed them to be punched out to speed up the cutting process. To prevent edge leakage circular disks were punched out of a 0.07 mm thick sheet of plastic to be placed between each ply. These disks could be reused for each test. They also had a hole in the center that created a constant flow area. A single ply from a test coupon is shown in Figure 23.

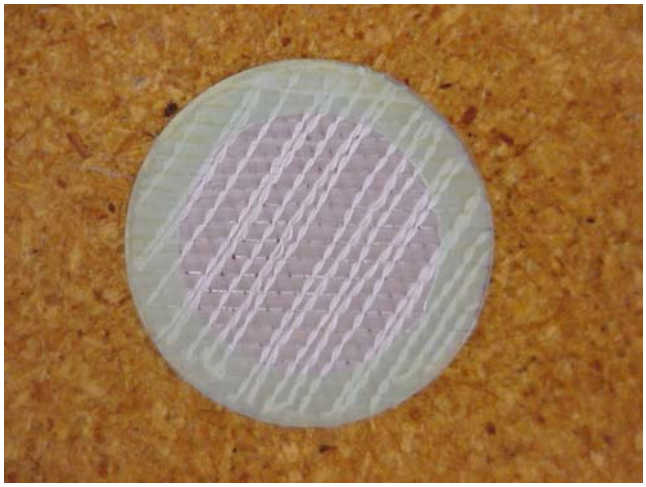


Figure 23: Air test coupon.

To calculate the permeability, the pressure drop across the sample was measured with a water manometer, and the flow rate was measured by an Omega FL-3840C rotameter style flowmeter. The air permeability tester was used to look at the variability between samples, and the uncompressed permeability of several fabrics. It was hoped that the uncompressed permeability could give a good relative comparison between fabrics, and possibly a prediction of its compressed permeability. A cross section of the test apparatus is shown in Figure 24. The entire setup is shown in Figure 25.

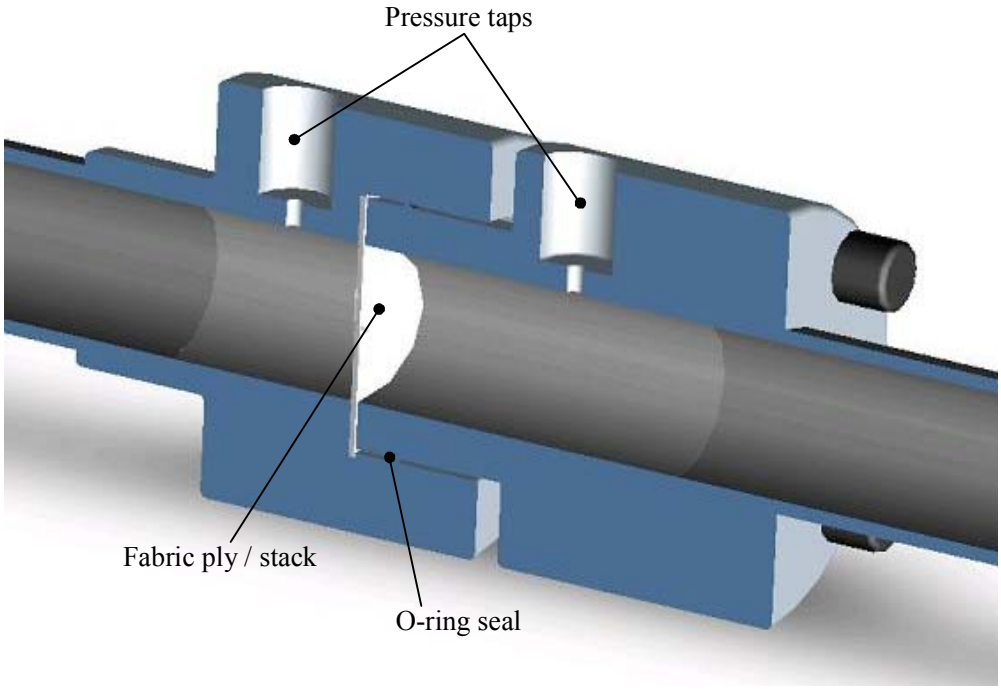


Figure 24: Cross section of air permeability tester.

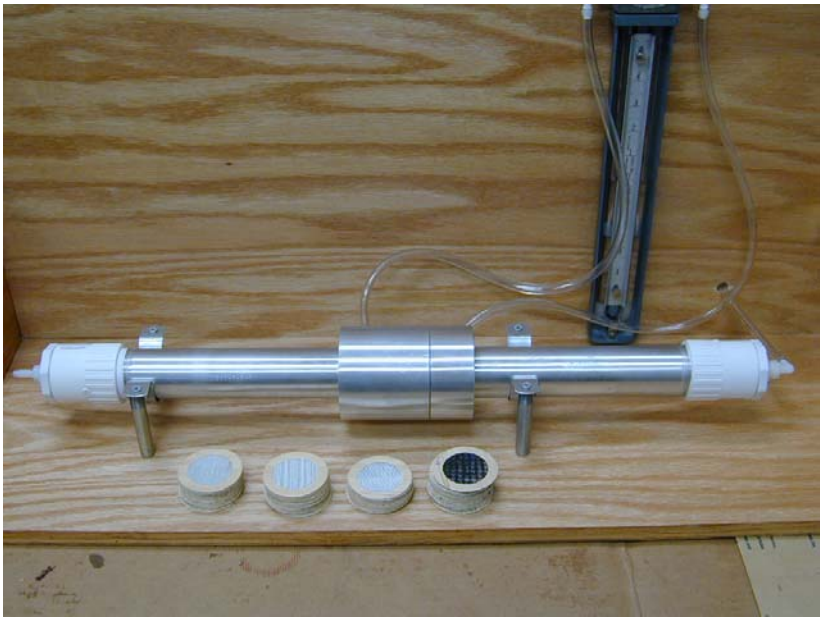


Figure 25: Air permeability test setup.

Liquid Permeability Tester

The next permeability tester created had multiple evolutionary changes to improve its validity and accuracy. This test apparatus gave a fabric flow area of 161 cm^2 to reduce scatter in the data caused by the random variation in permeability. It also used a honeycomb support structure placed below the fabric to support it under pressure while still allowing the flow to pass through. The sides of the test apparatus were made from 20 mm thick polycarbonate strips. This allowed the user to visually verify that no fluid was flowing around the edges of the sample. Leakage around the edges, or racetracking, is the largest potential source of error in permeability experiments [34]. Pressure taps were placed on the top and bottom faces of the tester along with an Omega differential pressure transducer to give the pressure drop though the fabric. Thermocouples were also placed on both sides of the fabric to give the temperatures needed in calculating viscosity. The test apparatus is shown in Figure 26.

Figure 26: Liquid permeability tester.

Permeability Testing Procedures

The test procedures for preparing a test and conducting a test both became very time consuming in an attempt to eliminate all sources of error. The first step in preparing the fabric was to create the flow area by applying masking tape around a 12.5 cm square template. Then the outer edge of the fabric was cut to 14 cm square. The masking tape helped to create and keep a clean edge on the fabric during cutting and handling. Once all the plies for a fabric stack had been cut, the testing apparatus was prepared for the sample. Clear packaging tape was applied to the inside of the polycarbonate windows to aid in the removal of the specimen after the test. This prevented the silicone from sticking to the windows and leaving a residue. Each ply of fabric was then placed into the test apparatus and a bead of silicone was run around the perimeter of the fabric in a 3 mm gap. This bead was then smeared by hand to make sure it was adhering to the fabric and the wall. Once all the plies had been siliconed into the apparatus a heat lamp was placed overhead to help the silicone cure faster. This usually took about two days. Figure 27 is of a single ply after taping and cutting the edges as well as a stack of fabric that has been siliconed into the apparatus.

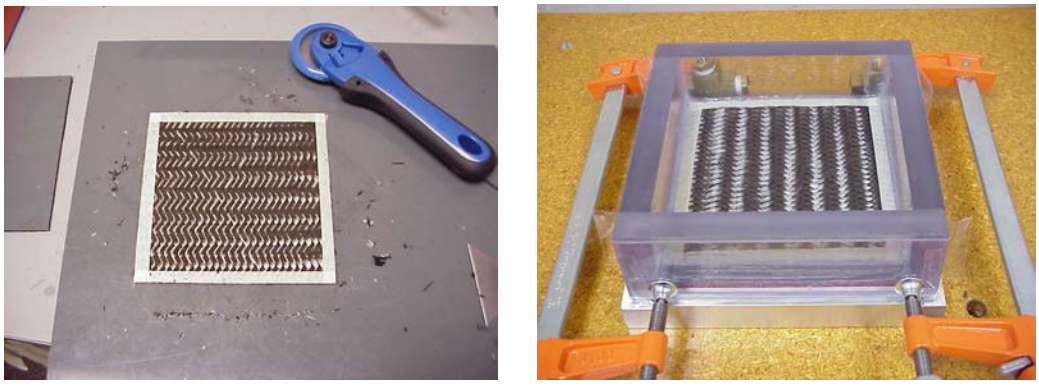


Figure 27: Test sample being prepared.

Once the silicone had dried the test apparatus was bolted together. A pressure pot was used to supply resin to the fabric at a constant supply pressure. It was very important to slowly fill the test apparatus from the bottom up to avoid creating any bubbles in the system. The same is true when saturating the fabric. The fabric was saturated from the bottom up at a low pressure to give the air plenty of time to escape. Trapped air can also be a significant source of error in permeability testing [34]. Once the system was full, the fluid was allowed to flow through for a few minutes before a reading was taken. When going from a lower supply pressure to a higher supply pressure it was very important to give the fabric time to compress. Because the fabric has a higher porosity at lower pressures it contains more resin. Since these tests are conducted in the saturated state, when a higher pressure is applied it takes time for the fabric to reject this extra resin as it compresses to the next state. Therefore, multiple readings were taken at each point until the values leveled off. At each point, the differential pressure was recorded throughout the test with a data logging multi-meter. From this, the average pressure during the test was determined and used in the calculations. Usually the pressure did not change more than a few percent during a test. The temperature was also recorded during the test to get the viscosity. The volumetric flow rate was calculated by measuring the time required to fill a graduated cylinder to a given volume. From this the velocity was calculated by knowing the cross sectional area. The last bit of information required to determine the permeability was the fabric thickness. As mentioned before, due to compressibility this value changed at different applied pressures. Unfortunately, measuring the thickness directly at the different pressures would be very hard to do during the test. To get around

this, data from separate compressibility tests were used along with the uncompressed thickness as recorded before the test. From the compressibility tests a percent reduction in thickness could be calculated at different pressures and used to calculate the new thickness. This method of backing out the fabric thickness could lead to some error due to the fact that the compressibility of a fabric can vary from one stack to the next [34]. However, it could prove just as difficult to measure the thickness of the fabric in-situ with the current test apparatus.

Another important procedure in the testing was to always work from low pressures to higher pressures. This is because once the fabric has been compressed by a high pressure it will not spring back to its original state as might be expected, although some spring back may occur. There are a couple possible explanations for this. One is that it takes a force to get the fiber tows to mesh with each other, but they are not necessarily in a strained state once this occurs. Another is the possibility that since the fabric is saturated, for it to spring back it would have to pull resin in to fill the voids created as it expands. It could be that fabric does not have enough of an elastic force to draw in the resin in a reasonable amount of time. It may be possible that the fabric would uncompress if given enough time, but this could possibly take hours or days. As mentioned previously, Bickerton et al found that glass fabric could exhibit viscoelastic behavior with hysteresis [41]. This phenomenon has also been noted by Parnas [34].

Capillary Pressure Tests

A series of tests were performed on the Ahlstrom fabric using the diluted corn syrup to get an approximate value of the capillary pressure for this fabric and resin pair.

In most of the research, the capillary pressure was calculated by monitoring the flow front at different times [35,36]. Recall equation 3.39.

$$t = \frac{z^2 * \mu * e}{(\Delta P_{mech} + P_{cap}) * K_f} \tag{3.39}$$

By knowing the distance that the resin had traveled in a given time and the fabric permeability, the capillary pressure could be determined. In order to calculate the capillary pressure through the thickness this approach was used. A clear top was placed on the permeability tester so the time required for the resin to flow through the thickness of the coupon could be recorded. By using equation 3.39 the capillary pressure could then be calculated.

Comprehensive Model Tests

In order to validate the comprehensive model a series of tests were preformed. For these tests, the transparent mold from the channel flow experiments was used.

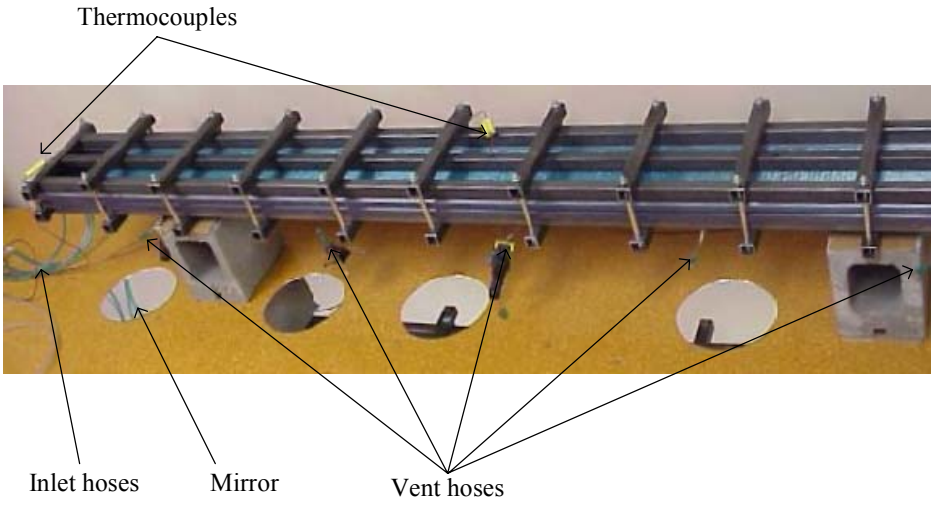


Figure 28: Test apparatus for testing channel flow and comprehensive model.

A series of vents were placed on the bottom side of the mold to allow air to escape as the mold was filled. Mirrors were also placed below the mold to monitor the underside of the fabric. Figure 28 is a labeled photo of this setup. Extreme care was taken in handling and preparing the fabric for each test. For these tests, the masking tape used for the permeability testing could not be used, so keeping the fabric intact during cutting and handling was a bit difficult. As the fabric was laid into the mold, a bead of silicone or caulk was run around the perimeter and smoothed out by hand as in the permeability testing. The aqueous corn syrup was again used as the test fluid and was supplied at constant pressure from the pressure pot. The fabrics used were the Ahlstrom unidirectional fabric and the glass woven roving.

A series of tests were performed to evaluate the accuracy of the model at different stages in the process. The first two tests performed examined the interaction between the flow in the channel and flow though the fabric. In these tests, the flow fronts in the channel and at the bottom of the fabric were observed in the transparent mold. The fluid fronts on the top and bottom of the mold are shown in Figure 29.

Figure 29: Upper and lower flow fronts.

The next test performed was to examine both stage one and two of the process by injecting resin until the part was saturated. In the first case, the flexible bagging was not used to force the resin through the fabric. Instead, the inlet was left open and under pressure so resin was fed in until the part was saturated. The purpose for this was to test the through thickness stage without the added uncertainty of how the bagging was affecting the process.

Finally, the process was tested to completion using the flexible bagging for stage two. In this test, once a given volume of resin had been injected the inlet was closed, and a pressure was applied to the bagging to force the resin though the thickness. Once the part was saturated, the inlet was opened to allow any excess resin to exit the mold. An exit port was also opened on the far end of the mold.

For all the tests, the pressure at the inlet manifold was recorded throughout the test by a data logging multi-meter. Temperature readings were taken in the tank and at various points in the test apparatus in order to calculate a representative viscosity.

CHAPTER 5

EXPERIMENTAL RESULTS AND ANALYTICAL CORRELATIONS

In this chapter, the results from tests involving the injection system and channel are compared to the equations derived in the previous chapter. The results from tests conducted on the various fabric architectures are also presented. The results from these tests on the individual regions of the process are then used as input to the comprehensive model. Several experiments are then run to validate the comprehensive model. The results from the model and experiments are compared at different stages of the process. The experiments conducted represent processes that are dominated by channel flow and processes that are dominated by fabric flow.

Injection System Test Results

The predicted results for the injection system compared very well to the experimental results, especially for the smaller hoses. For the 6.35 mm hoses, the predicted equivalent permeability of the system was 1.36E-4 cm^3 and the averaged experimental value was 1.31E-4 cm^3. This results in about a 4% error. For the larger hoses, the predicted equivalent permeability was 5.18E-4 cm^3, and the average experimental value was 4.48E-4 cm^3, resulting in a 13% error. One reason why the model was not as accurate for the larger hoses is that in this case, there is much more pressure drop in the manifold and hose fittings. The equations used to develop equation 3.14 are most accurate for fully developed laminar flow. Because of the close proximity of the sharp inlets, exits, and

elbows in the hose manifold, the flow is not fully developed. This was not as noticeable in the case of the small hoses because a larger portion of the pressure drop occurred in the hoses, making the manifold less significant.

For the further experiments involving the hose system, the experimental equivalent permeability value of the hoses was used since it was slightly more accurate. However, if experimental values were not available the predicted value would still give acceptable results.

Table 2: Results from hose system tests.

Hose Diameter(mm)	Predicted Permeability (cm^3)	Experimental Permeability (cm^3)	Error
6.35	1.36E-4	1.31E-4	4%
9.5	5.18E-4	4.48E-4	13%

Channel Flow Test Results

The analytical model for the flow through the channel had good correlation with the experimental results based on the time to fill the channel, and the pressure drop. Although the fluid entered the channel through three points, the flow front became straight and uniform after a very short distance. An average fluid temperature value was determined from the various readings taken throughout the process. Temperature changes of 2° C were observed from the supply tank to the end of the mold. The average supply pressure was also recorded and averaged. This pressure remained very constant, and changed mainly due to the change of the fluid height in the tank. The pressure and vis-

cosity values were plugged into equation 4.1 to predict the time required to fill the mold. Each transient test was run once. From the steady state tests, the flow rate, temperatures, and pressure drop between two points was recorded. From the flow rate the velocity in the channel was calculated. Using the velocity and fluid viscosity in equation 3.16, the predicted pressure drop was calculated. The pressure drop for three tests was averaged. This value was compared to the experimental value. The results from these tests are presented in Table 3. Both tests were run for two different mold gaps, one being 3.7 mm and the other 2.1 mm.

Table 3: Results from channel flow experiments

Transient Tests			
Mold gap height (mm)	Time to fill mold (s)	Predicted time (s)	%error
3.7	103	99.5	3.4
2.1	78	82	-5.1
Steady State Tests			
Mold gap height (mm)	Pressure drop (kPa)	Predicted Pressure drop (kPa)	%error
3.7	4.91	5.1	-3.9
2.1	10.9	11.4	-4.6

In both cases, the analytical model was in good agreement with the experiment. The model was able to predict the time to fill the channel and the steady state pressure drop within 5%. Since the errors fluctuate from negative values to positive values, it is reasonable to assume that the error is mostly due to the accumulation of measurement errors. Possible error could come from the value used for the equivalent permeability of

the hose system. The measurement of the channel height and its deflection during the test could also be a significant source of error. A minor amount of deflection was evident due to a very small amount of seepage out of the sides of the channel. This would lead to a pressure drop in the experiment lower than predicted, as was seen. Since the pressure drop through the channel is a function of the channel height squared, a small error in its value could be significant. Another source of error is the changing viscosity during the test. Since the temperature of the fluid is changing with position and time, the viscosity is also changing. Using an average temperature value will account for this change to some extent, but it may not be exact. Error in the thermocouples themselves could also contribute.

Fabric Test Results

Fabric Compaction Data

The fabric compaction data for three of the fabrics used are presented below. The effect of compaction pressure on fiber volume fraction is shown in Figure 30 and the effect on thickness is shown in Figure 31. In both figures, the equations of the curve fits that were used in the permeability calculations and in the comprehensive model are shown. As discussed in the background, the logarithmic or power law fits do not have any physical significance; they simply fit the data well. They were used in this case since the data had already been taken in previous research. For a more precise fit using physical parameters the procedure outlined in the background chapter could be used.

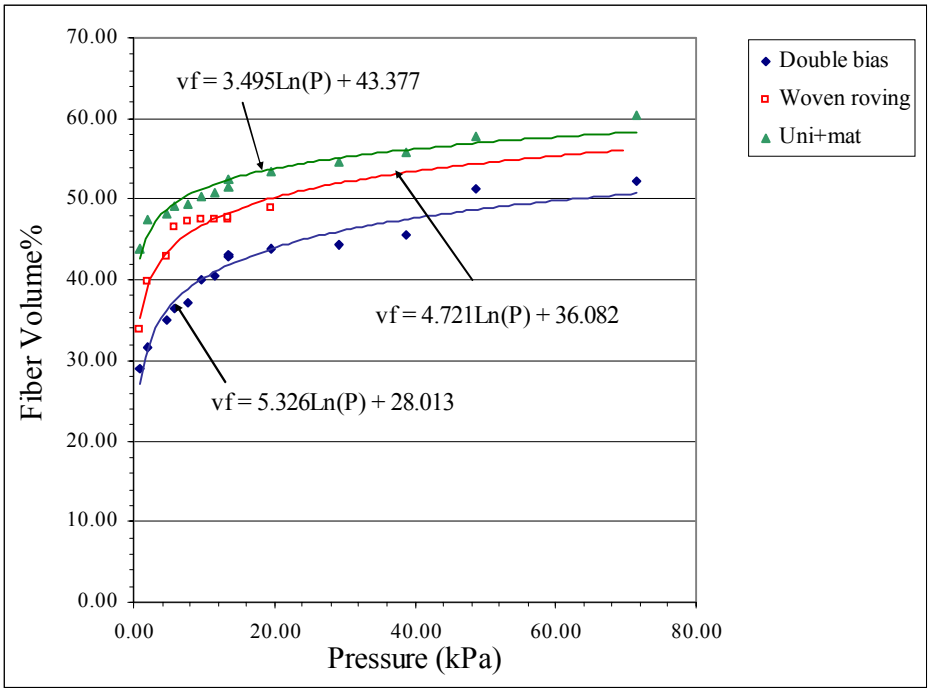


Figure 30: Fiber volume % vs. compaction pressure.

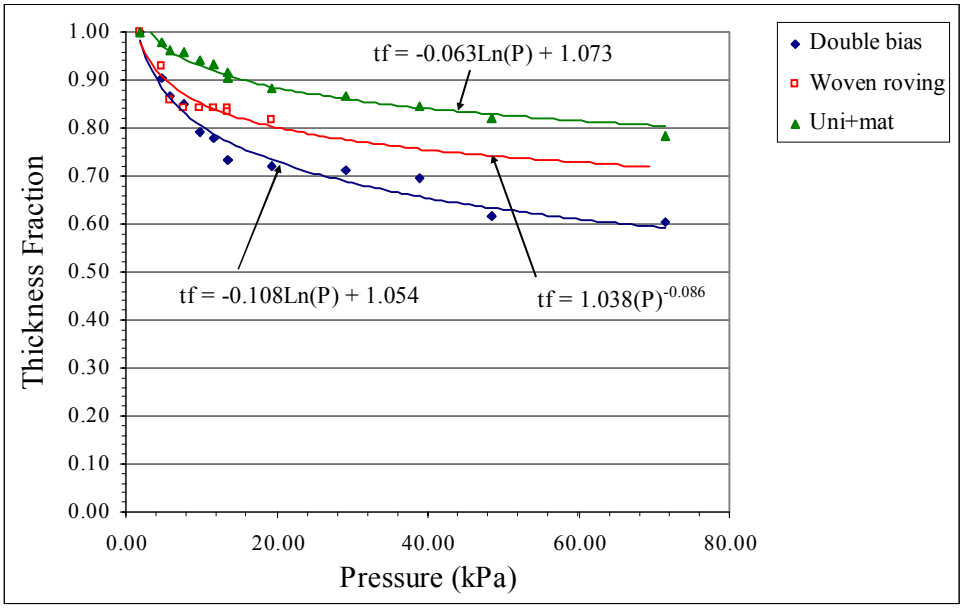


Figure 31: Ply thickness fraction vs. compaction pressure.

It should also be noted that the ply thickness fractions do not start at 1 for zero pressure. This is because a very small amount of pressure was applied to the fabric stacks to take a measurement of the "uncompressed" initial thickness in the permeability tests. Therefore the initial measurement was not at zero pressure.

The fact that compaction effects diminish at high pressures is illustrated in these figures. This is because once all the fiber tows are nested and there is glass on glass contact throughout the part, the fabric will behave almost like a solid slab of glass. This is important in demonstrating that each fabric has a maximum attainable fiber volume fraction. It also demonstrates why the fabric permeability tends to level off at higher pressures because the fabric becomes fully compressed. It should be noted that there could be a small amount of error incurred by applying this data to a thick stack since the tests were performed on lay-ups of two to three plies. According Luce, et al., the compressibility of a fabric can vary depending on the number of plies up to about five plies [34,46]. After five plies the compressibility is consistent. Based on the results presented in reference [46], it appears that the difference between two and five plies should be less than 10%, which is still less than the fabric variability.

Liquid Permeability Test Results

The results from the permeability tests showed a strong relationship between permeability and compaction pressure. All fabrics had a large decrease in permeability in the range tested. In all cases, the permeability tended to level off at higher pressures as the fabric approached its fully compressed state. A plot of the data from the various fabrics tested is shown in Figure 32.

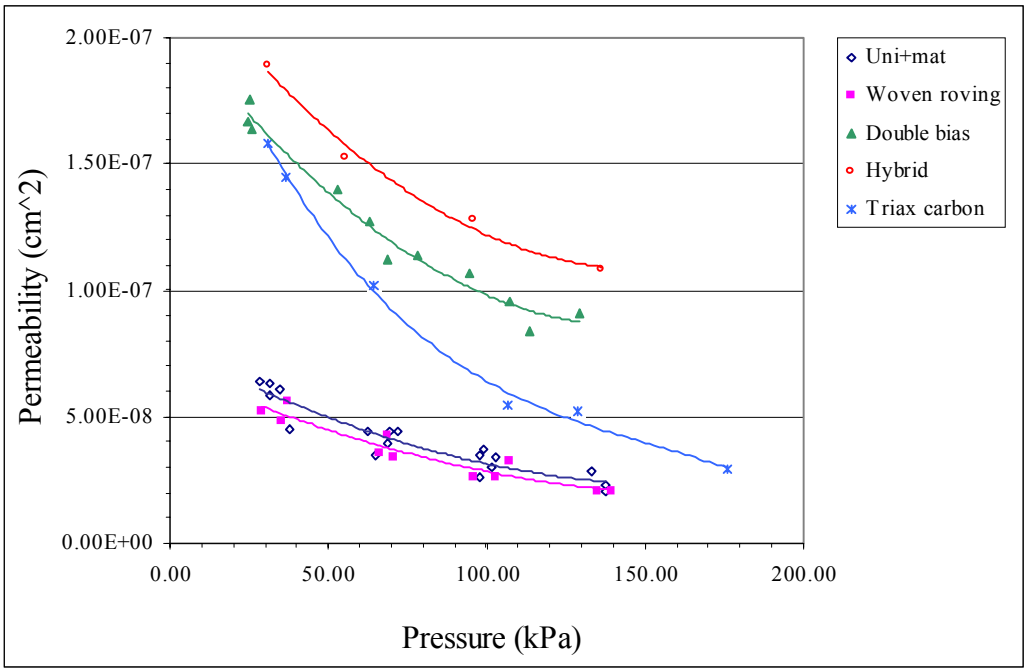


Figure 32: Permeability results for all materials tested.

The fabrics with the lowest permeability were the unidirectional fabric and the 0-90 woven roving. In both these fabrics, the macroscopic passages between the tows were small and could be blocked off as the fabric became compressed.

The double bias fabric had the second highest permeability. Because this fabric was not woven and had layers at 90 deg. to each other, the macroscopic flow passages remained relatively open even with high pressures. The gaps between tows were also larger to begin with than for the unidirectional fabric. Unfortunately, this architecture also limits the fiber volume fraction.

The tri-axial woven carbon fabric started with a very high permeability because of large macroscopic flow passages between the tows created by the weave. This fabric was also very springy due to the particular weave. Once a large pressure was applied to this

fabric, the flow passages were blocked off as the plies were pressed together. Ultimately, this fabric ended up with a permeability close to that of the 0-90 glass woven roving. Because the change in permeability at lower pressures was so large, this fabric was tested to higher pressures to see where the permeability might level off. The results from this test are shown in Figure 33. As can be seen, the permeability does not level off until after 350 kPa. From this point, it could be expected to still decrease by a small amount at even higher pressures.

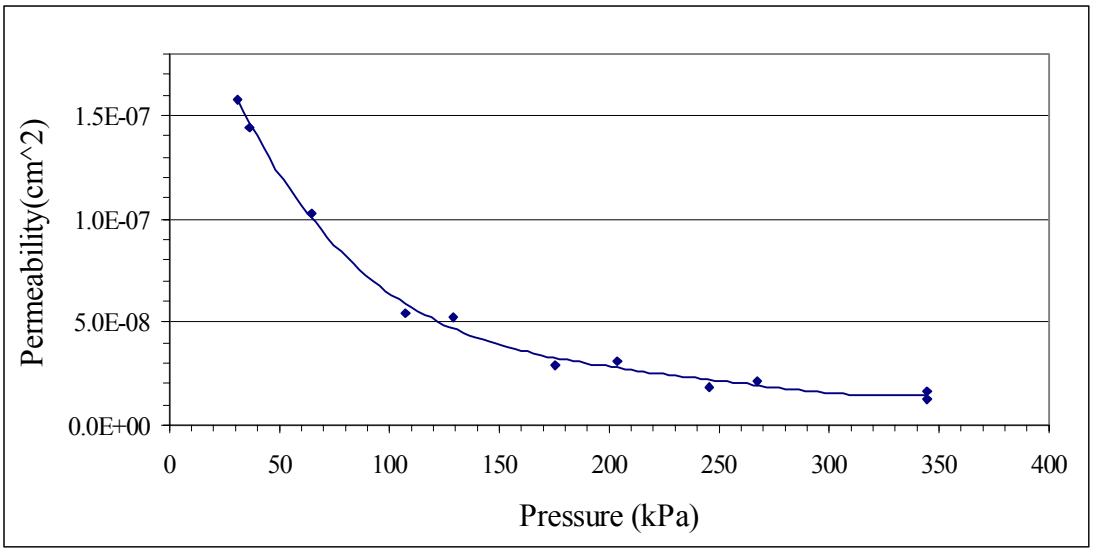


Figure 33: Permeability at high pressures for woven carbon fabric.

The hybrid composite using the solid strips and the glass 45 degree plies had the highest permeability of 1.1E-7 to 1.9E-7 cm^2. Although the fluid was forced to follow a rather long path through the staggered strips, the channels created by the missing tow in the glass layers formed good flow channels. These channels also remained relatively open even at higher pressures. The behavior of this material was similar to that of the

double bias fabric because the architecture did not permit fiber nesting. The strips used were solid and had fiber volume fractions of around 0.7. Therefore, the total fiber volume fraction was still around 50% which is in the same range as the other fabrics. This particular arrangement shows potential due to its high permeability, low compressibility, and relatively high fiber volume fraction. This test just gives an idea of the permeability and fiber volume fractions possible with this type of material. If thicker strips were used, the permeability and fiber volume fraction could be even higher. With 6mm thick strips, fiber volume fractions of around 64% could be achieved. An alternative to the glass ply between the layers would be to create small ridges on the strips as they are manufactured to create flow channels and a bonding surface. This could lead to an even higher permeability and would also mean that the permeability would be almost constant with pressure. This concept could also utilize pre-fabricated round or hexagonal rods that would be built up in a similar fashion.

Another aspect of the permeability testing was to determine the variability of a single fabric due to the random nature of the stacking. Figure 34 is a micro-graph from [10] of how fiber stacking could greatly influence permeability.

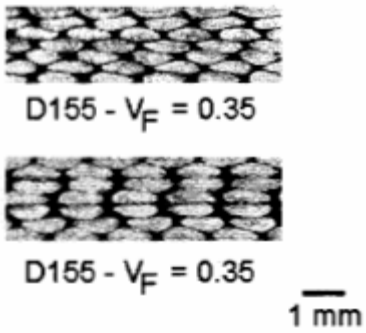


Figure 34: Illustration of flow channel variation [10].

Five tests were performed on the unidirectional fabric to quantify this effect. The maximum deviation from these tests was around 20% from the mean value. This is consistent with the results of others who have found deviations of around 20% [29,34,39]. Some have even found variability of 25-75% [8]. These values for variability are by no means constant and will depend on the particular fabric and the sample size; however, it seems that a 20% deviation is a common result. The results from the five tests are shown in Figure 35. It is interesting to note that although the values change, the trend is nearly the same for each test.

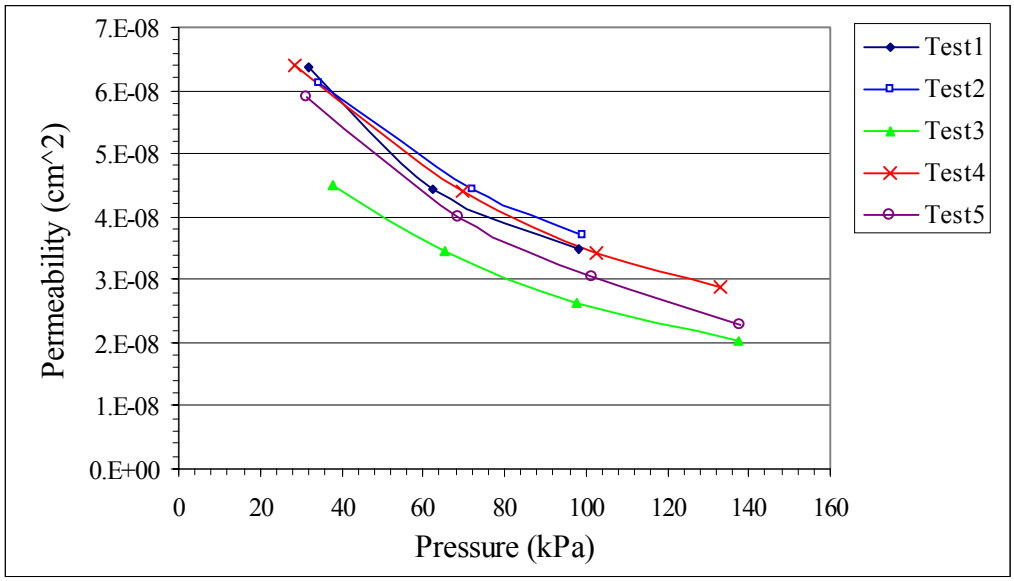


Figure 35: Repeatability study for unidirectional fabric.

Air Permeability Test Results

The air permeability tests were very quick and simple to conduct as expected. Unfortunately, the samples were not as easy to punch out as was hoped. To compare re-

sults with the liquid tests, and to establish the validity of the test method, the Ahlstrom unidirectional fabric and the DB240 were tested in stacks of ten plies. Six stacks of each fabric were tested. Because there was no mechanical clamping on the fabric they were essentially in the uncompressed state. The air was only able to develop a differential pressure of about 2 kPa. To compare these results to those obtained using the corn syrup, the trend lines for these fabrics were extended to 2kPa. The compared values are shown in Table 4.

Table 4: Comparison of air permeability results and liquid permeability results.

Fabric	Pressure (kPa)	Permeability Liquid (cm^2)	Permeability Air (cm^2)	% difference
Uni+mat	2	8.0E-08	1.6E-07	100.0%
Double bias	2	2.0E-07	3.6E-07	80.0%

Capillary Test Results

Determining the capillary pressure through the thickness proved to be difficult. Unfortunately, for through thickness tests there is a large variability and a short distance traveled. In order to use equation 3.39, a specific relationship between injection time and distance must be known. The problem with this method was that the fluid did not pass though the fabric with a uniform flow front and came up through different parts of the coupon at different times. Guittard found that for permeability measurements where an unsaturated flow front was monitored, that the injected distance should be greater than 19 cm [31]. For cases where the permeability is very small, this could be less. For these tests, the injected distance was only 2 cm, which could lead to a significant error. Also

noted by Guittard, was the effect of the dual scale flow on creating an ambiguous flow front [31]. Figure 36 is of the resin as it came though the fabric.

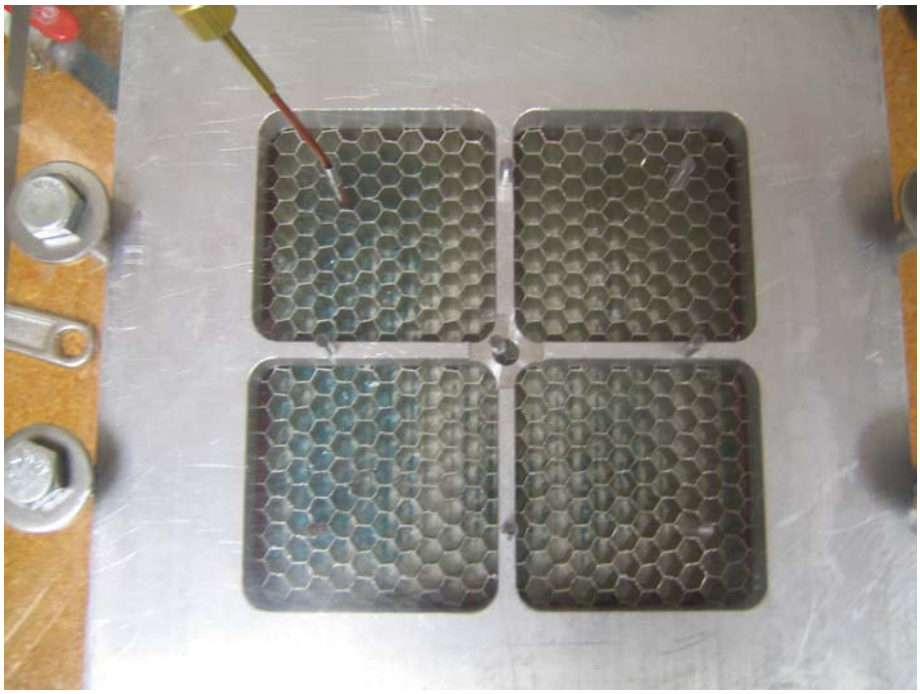


Figure 36: Flow front coming through fabric during capillary pressure test.

In this test, the left side of the sample was saturated after about 100 seconds and the right side took about 158 seconds to saturate. Although using the average of these values can give an approximate value for the capillary pressure, it is very imprecise. The values obtained from these tests were around 4 kPa which most likely means that the capillary pressure is somewhere between 3 kPa and 5 kPa.

These results are in the same neighborhood as the results of Luo et al. and Rossell [18,39]. For future tests, a value for capillary pressure of 4kPa was used which should be a good representative value.

Another way to get an approximate value for capillary pressure would be to do a test across the plane of the fabric, transverse to the fibers. In the case of a unidirectional fabric, this value would be approximately the same as the value though the thickness. Unfortunately, the unidirectional fabric had a random mat stitched to it so this test would still not give a precise value.

Fortunately, this test did show that the value of the capillary pressure was small even though a precise value was not obtained. In most of the RTM processes examined earlier, a vacuum pressure of 70 – 100 kPa would be used. In these cases, a capillary pressure of 4 kPa would provide less than 6% of the total driving force. Because the capillary pressure is small compared to the injection pressure, a somewhat large error in this value will only lead to a small error in subsequent modeling.

Comprehensive Model Test Results

A series of tests were performed to test the validity of the comprehensive model. Tests were performed to compare the model accuracy at different stages of the process. The first tests examined how well the model could predict the simultaneous flow through the channel and into the fabric. For the first test the unidirectional fabric was used. The fabric thickness was about 7.5 mm and the channel height was 2.1 mm. The part length was 1.8 m. The diluted corn syrup was supplied at approximately 30 kPa throughout the test. Fluid was injected until it reached the far end of the channel. The time required for the fluid to reach this point was recorded, as well as the approximate position of the flow front at the bottom of the fabric. These two values were then com-

pared to what the model predicted for that supply pressure. The output from the model is shown in Figure 37.

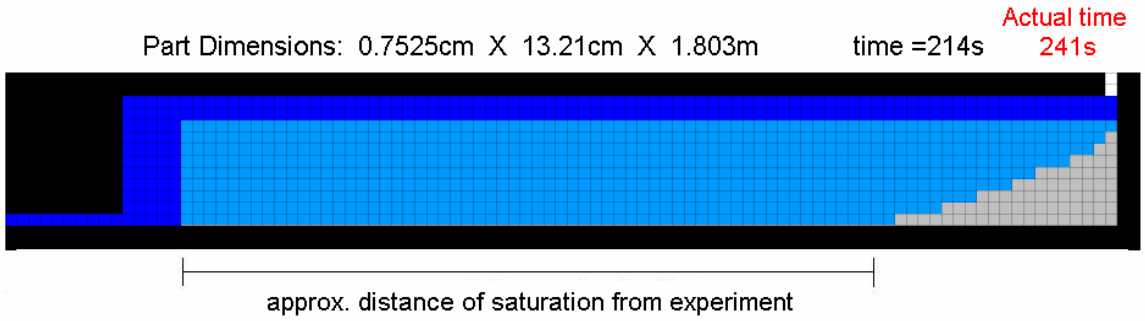


Figure 37: Output from model compared to experimental result (test 1)

Along the bottom of the figure from the model, the actual position of the flow front in the experiment has been inserted for comparison. As can be seen, the model did a good job of predicting the flow through the fabric, as well as the time required to fill the channel. The actual time to fill the channel was 241 seconds, compared to 214 seconds from the model. This results in a -11% error.

A second test was performed in a similar fashion with thicker fabric and larger mold gap. The results from this test are shown in Figure 38.

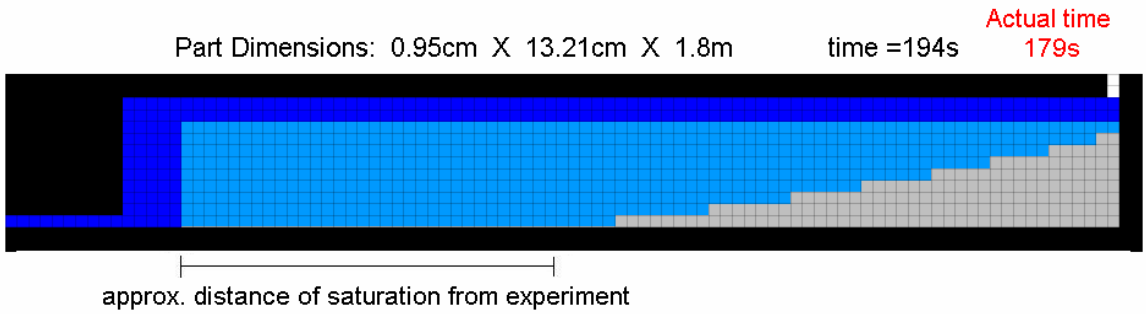


Figure 38: Output from model compared to experimental result (test 2)

For this second case the time prediction was closer to the experiment, and the model still did a good job of predicting the flow front. The actual time required to reach the end of the mold was 179 seconds, while the predicted time was 194 seconds. This results in an 8% error in the time prediction.

The next stage of the testing was to test the model accuracy after the fluid had reached the end of the mold. To get a better idea of how the model would perform for the through-thickness step, the fabric thickness was increased to about 2 cm. The first experiment was run without the use of the flexible bagging to isolate its effect. The resin was forced through the thickness by keeping the inlet open and continuously feeding in resin until the part was saturated. The total time required to saturate the part was recorded to compare to the predicted value. The supply pressure recorded during the test was duplicated in the model. It was difficult to judge when the entire sample was saturated. This made precise comparisons between the model and the experiment difficult. The clear plate on the bottom made it easy to see the resin coming through, but it was hard to pick an exact saturation time. For example, there was about a twenty second interval from when the part appeared to be about 98% saturated to when it was completely saturated. Because of this, the saturation time in the experiment will be presented as a range. For the third test, the saturation time was within 196 – 211 seconds. The model predicted a saturation time of 208 seconds, which was right in the experimental range.

The final experiment added the additional effect of the bagging film. In this case, a given amount of resin was injected and then the inlet was closed. Pressure was then applied to the bagging to force the resin though the thickness. Again, an interval of time

was recorded when the part became fully saturated. During this experiment the inlet pressure changed noticeably, and also dropped off almost completely while the pressure was being switched from the inlet to the bagging. This discontinuity in pressure is a consequence of this particular process. As the resin is being injected there is no pressure on the bagging so the channel stays open. Once the resin has been injected the inlet is closed, and there is a small interval of time that passes as the pressure is being switched from the resin tank to the bagging film. In order to compensate for this in the model, the pressure was entered as a function of time rather than a constant value. The actual pressure profile and the profile used for the model are shown in Figure 39. Key events in the process are also labeled. The numbers are as follows: 1 is when the resin reaches the end of the channel; 2 is when all the resin is injected; 3 is when pressure is applied to the bagging; 4 is approximately when the part was saturated.

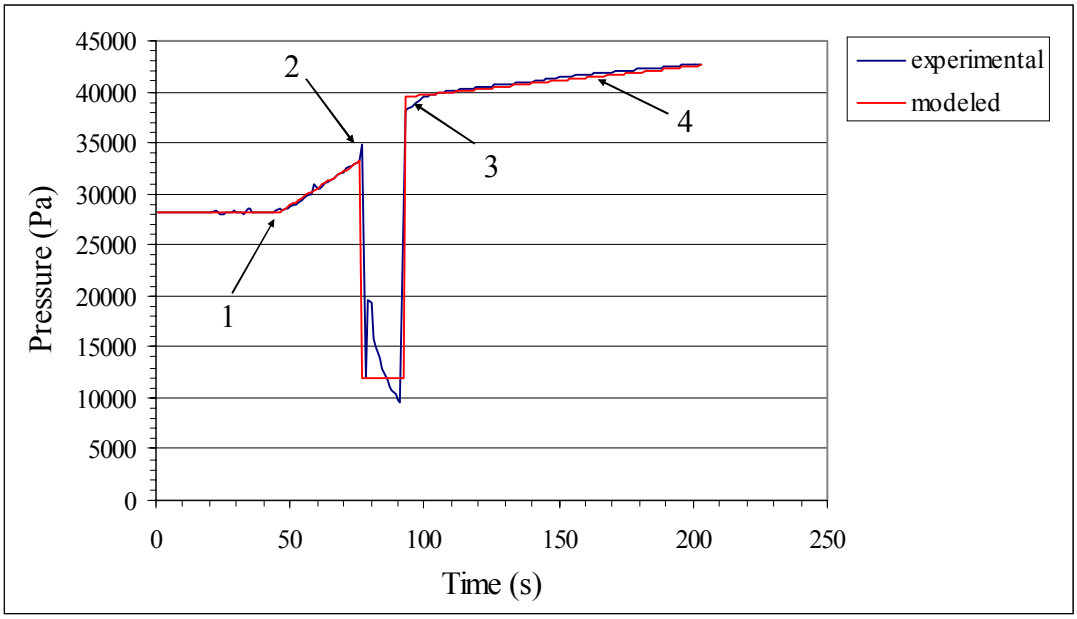


Figure 39: Pressure profile from experiment compared to profile used in model.

For this experiment, the saturation time was between 154 and 174 seconds. The time predicted by the model was 135 seconds. This results in a 12-22% error. A few of the intermediate times in the experiment were also recorded. The time required to fill the channel was within 6% of the actual value, and the time to inject all the resin was within 1% of the actual value. This would indicate that most of the error is due to variability or inaccuracy in the fabric properties such as permeability and compaction. The outputs of the model at these three points in the process are shown in Figure 40.

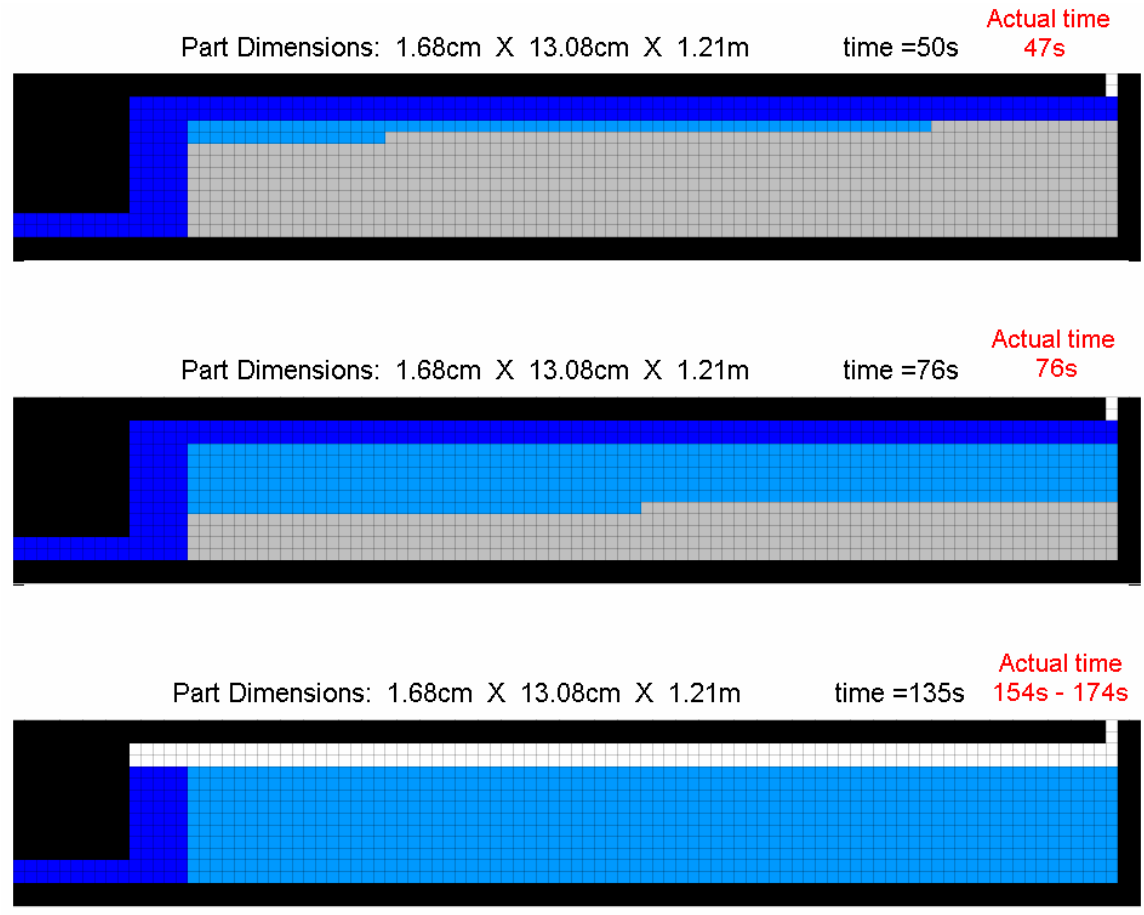


Figure 40: Output from model compared to experimental result (test 4)

In order to ensure that the part was saturated, slightly more resin than was needed was injected. In order to eject this extra resin, the inlet port was reopened after the part was saturated to allow it to escape. There was also a similar port on the opposite end of the mold to let the resin out. Once the part was saturated there was essentially zero flow coming out of the vents at the bottom. This is because the resin would have to flow over large distances through the thickness and in the plane of the fabric to reach one of these vents. This is why the vent ports were included above the fabric and would be critical to any process of this type. This part of the process was not included in the model, but as long as the amount of extra resin is small, it should be minor. A peel ply could also be used to strip any extra resin off the top of the part.

The fabric samples used in the last two tests were also examined for any air pockets or dry spots. The layers of fabric were peeled away and examined. No dry spots were detected during this process.

CHAPTER 6

PARAMETRIC STUDY

Once it was shown that the model was doing a good job of representing a real process, the next step was to use it to investigate how changing process parameters affects the process as a whole. The experiments performed represented a range of processes, but were limited by the size of the mold and the time required to conduct them. In order cover a wider range of process variations, the comprehensive model was used. This is where it was useful to have a model that could be run in a short amount of time, with easy to vary parameters. A part of this study was to see if the total process time could be predicted using the equations derived individually for flow through the thickness (eq. 3.39), and for filling the channel (eq. 4.1). These equations will be referred to as the individual flow equations. Each parameter was examined for a "small" part, and a "large" part, although these are only relative terms. The small part was .6 cm thick, 12 cm wide and 2 m long. The large part was 10 cm thick, 2.4 m wide, and 40 m long, which is approximately twenty times as large as the small part. The injection system was increased in size accordingly.

Channel Height

For the pressure bag molding process, the channel geometry is one of the most important considerations in mold design. In the exploratory studies performed by Larson, it was seen that the channel height could be the difference between a successful and unsuccessful part [17]. To see how the channel height can influence the pressure bag

molding process, the model was run for three different channel heights. The channel heights will be referred to as a percentage of the part thickness. For example, a 20% channel height is 20% of the fabric thickness. The output from the model for three cases is shown in Figure 41.

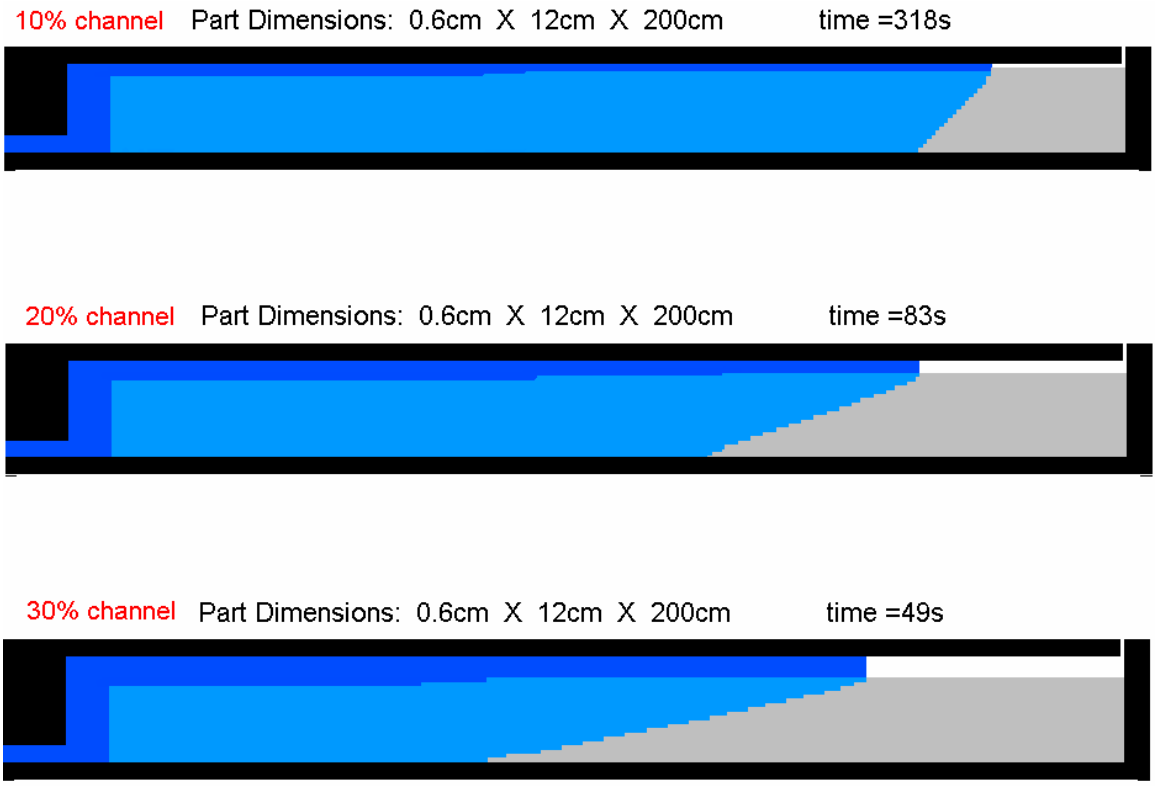


Figure 41: Varying channel height for thin part.

For the model runs in Figure 41, only enough resin to saturate the part was injected. As can be seen, for all three cases so much resin entered the fabric that the channel was not filled. This would be undesirable because the flexible bagging can pinch off the rest of the channel when pressure is applied rather than forcing the resin to fill the channel. This was observed by Larson [17]. In the case of the 30% mold gap, so much

resin was stored in the channel that there was not enough to fill it. For the 10% mold gap there was not as much volume in the channel, but the equivalent permeability of the channel was so much less that much more resin was forced into the fabric. The time required to inject all the resin was much larger as well. There are a couple of options to solve this problem. One would be to inject extra resin to fill the channel; however, this would be wasteful and may not be the most cost effective solution. Another option would be to change the channel geometry. In this case, a couple of channels spaced apart may be preferred to the wide thin channel. What would be optimal is a channel with a small volume, yet a fairly high equivalent permeability. This is why a series of channels may be sufficient for thin parts as in SCRIMP™ or VARTM [7,22,23]. This type of system would require a model for flow in the plane of the fabric and will not be examined here. This is just an example of how the model can be used to locate problems and optimize a process.

Assuming that enough resin is injected to fill the channel, the model was run until the part was saturated. Figure 42 is a plot of the time required to saturate the part for the different channel heights. This figure shows the non-linear relationship between channel height and injection time. This is primarily due to the fact that the channel equivalent permeability is a function of the hydraulic diameter squared. If the height of the channel is small compared to the width, then the hydraulic diameter is linear with channel height. This means the equivalent permeability is ultimately proportional to the channel height squared.

As mentioned, the potential for using the individual flow equations for the channel and fabric were used to see how they might be able to predict the process time. Included in the figure is the predicted time to fill the channel only, neglecting the presence of the fabric (eq. 4.1). In all cases, this time is much less than what it took to fill the channel in the model. This result is actually closer than it should be in this particular case. In the model, the compaction of the fabric from the fluid pressure is accounted for. Recall from Figure 31 that a large amount of fabric compression occurs even at very low pressures. As the resin is being injected into the channel, it is building up pressure over the fabric due to the resistance to flow. This pressure compacts the fabric and makes the channel larger than it originally was, which reduces the injection time.

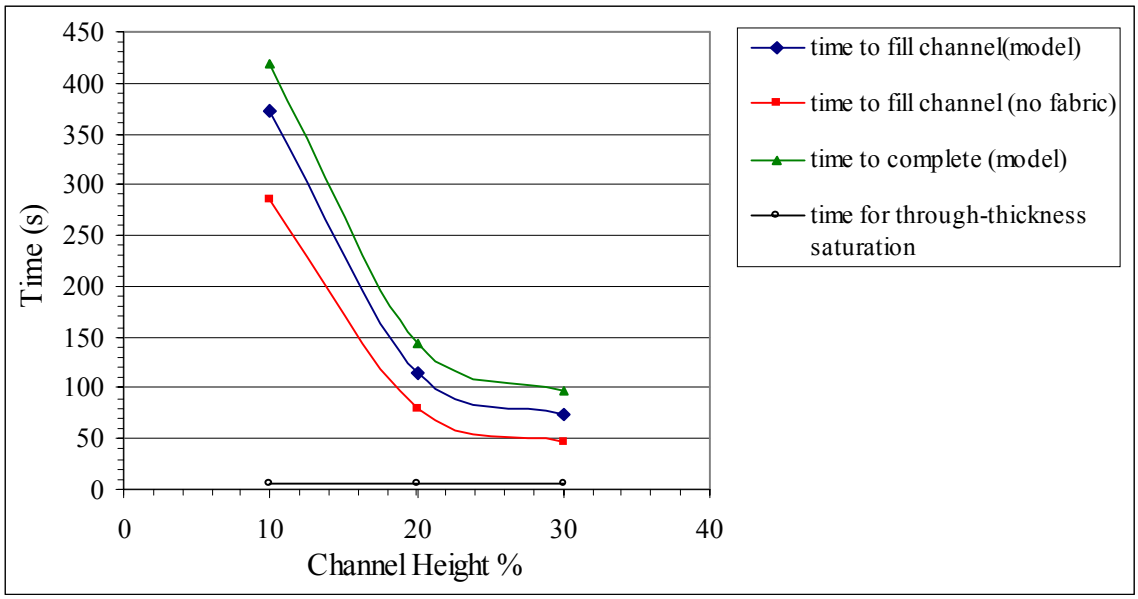


Figure 42: Effect of channel height on small part.

The time that would be required to flow only through the thickness of the fabric is also shown in this figure. Its value is minuscule compared to the actual time to complete

the injection. From this, it can be seen that a thin part is going to be dominated by the channel flow process, and that the flow through the thickness is insignificant. The fabric acts more as a wick that prevents the channel from becoming full, which is why the process still takes much longer than the channel flow problem alone.

The same study was also performed for a much thicker and longer part. Figure 43 shows the flow front after the channel has been filled for the 20% channel case, which was very similar to the other two cases.

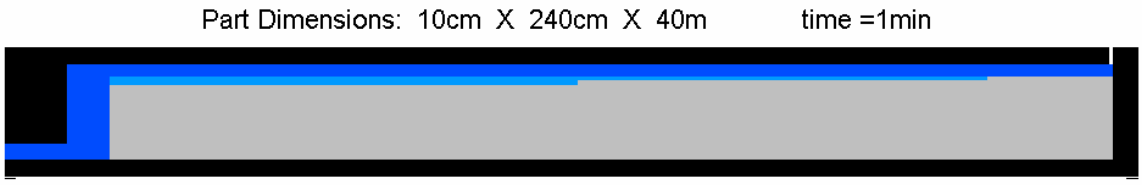


Figure 43: Flow front for thick part, 20% channel height.

In this case, there was very little saturation of the fabric during this process. Although the resin may have penetrated a little over one centimeter, it is still a small portion of the overall thickness. In order to understand why this is so different than the first case, it is important to again look at the governing flow equations. For the channel, the height has increased by almost twenty times, which means the equivalent permeability is almost four hundred times as large. However, the length of the channel has also increased by twenty times. From equation 4.1, it was shown that the time required to fill the channel increases by the length squared. Thus, the time required to fill the channel is essentially the same for the small and large part. Since this process takes about the same amount of

time, roughly the same amount of fabric saturation occurs. However, 1 cm of saturation in the large part is a small portion of the total thickness. One should also remember how the pressure gradient decreases as the flow front moves deeper into the fabric. This means it is very easy for the resin to penetrate that first few millimeters, but it soon starts to slow down.

The positions of the flow fronts after all the resin has been injected are shown in Figure 44. Because there was no problem in filling the channel in all three cases, the most important thing is how long it takes to saturate the part. The total saturation time is shown in red.

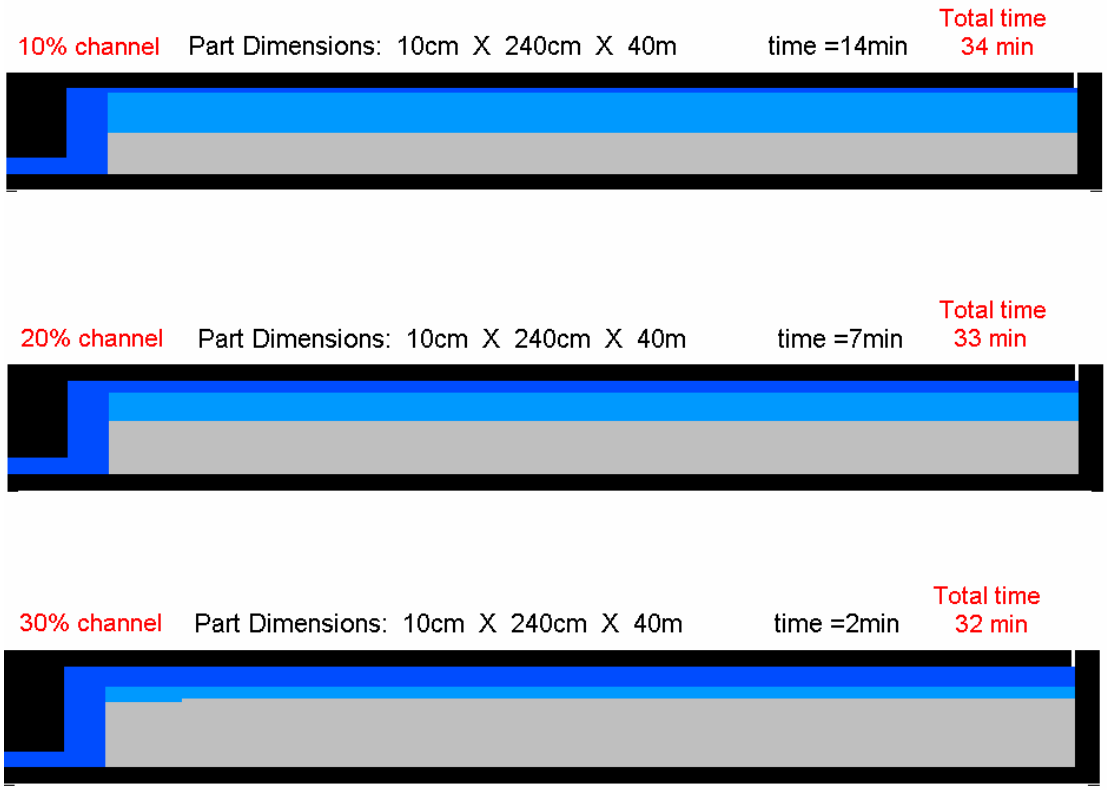


Figure 44: Flow fronts after resin is injected and total process time for large part.

In the 30% channel case the resin is injected very quickly, but there is a lot of volume contained in the channel. In the case of the 10% mold gap it takes seven times as long to inject the resin, but much more resin has gone into the fabric. As a result, the total time for all three cases is almost the same. This illustrates the fact that something entirely different is going on in this case compared to the thin part. Due to the thickness of this part, the process is governed almost entirely by the through-thickness step, which is why the channel height is not very important. In a case such as this, where a smaller channel does not slow down the process much, it would probably be preferable to a large one. There will always be a bit of unpredictability to how the bagging film will react when pressure is applied to it. The bagging could possibly push the resin to one side of the mold if the film was not uniform in thickness. However, this was not observed during the tests preformed at MSU.

Figure 45 was generated to show how the total process time is very close to the time that would be required to go through the thickness only. The actual time required to fill the channel, and the time that would be predicted using eq. 4.1 are also shown. Again, these values are not very close, but in this case the channel flow process is very minor. The time from the model is less due to fabric compaction. If one were to add the individual times for filling the channel and flowing through the thickness, this would give a very close result to the computer model.

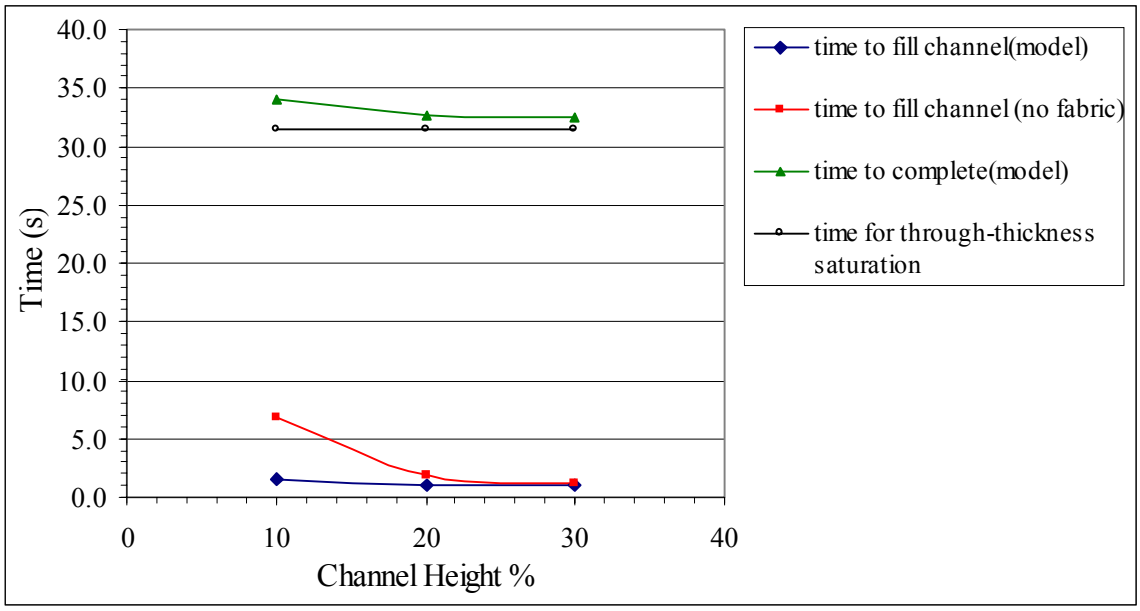


Figure 45: Effect of channel height on large part.

Injection System

The next parameter that was examined was the number of hoses in the injection system. Since the channel has a very high equivalent permeability a significant amount of the pressure drop occurs in the hoses, especially as the channel is being filled. To examine this effect the model was run with different injection system permeabilites, while keeping everything else constant. The model was first run for the 0.6 cm thick part with a 20% channel height. The injection pressure was 70 kPa. The model was run for hose system permeabilites ranging from 1E-5 cm^3 to 2E-4 cm^3. For reference, the system used in the experiment with three 0.635 cm diameter hoses had an equivalent permeability of 1.31E-4 cm^3. The results for this test are shown in Figure 46.

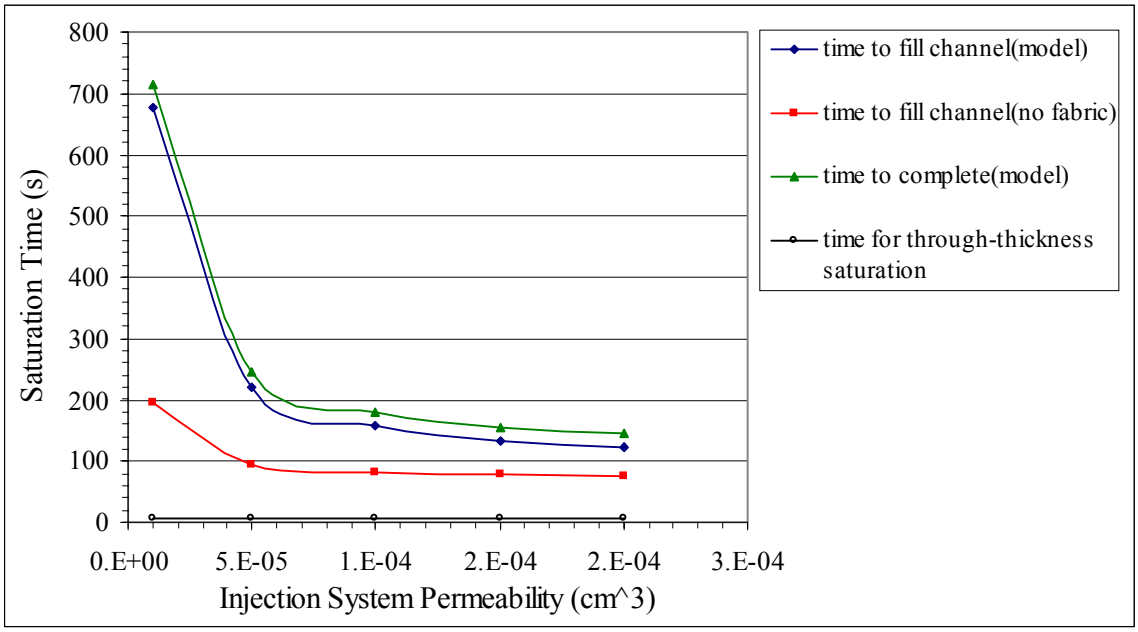


Figure 46: Effect of hose system on saturation time for .6 cm thick part.

Increasing the number of hoses can dramatically reduce the process time, up to a point, as shown in Figure 46. As the number of hoses increases the benefit for each additional hose is starting to decrease, as more of the pressure drop is occurring in the channel. The predicted times from the model and from equations 3.39 and 4.1 are again shown. As in the last case, the compaction of the fabric under pressure has made the prediction for filling the channel using equation 4.1 closer than it should be. Although eq. 4.1 cannot predict the process time accurately, it does do a good job of predicting the trend, and when the injection system is sufficiently large.

This study was also performed on the thick part. The hose system equivalent permeability was varied from .01 cm^3 to .5 cm^3. For reference, a hose system with 10 hoses, each 2 m long with 3 cm ID has an equivalent permeability of .1 cm^3. Again, there

was a significant effect of the injection system on the process. The results from this test are shown in Figure 47.

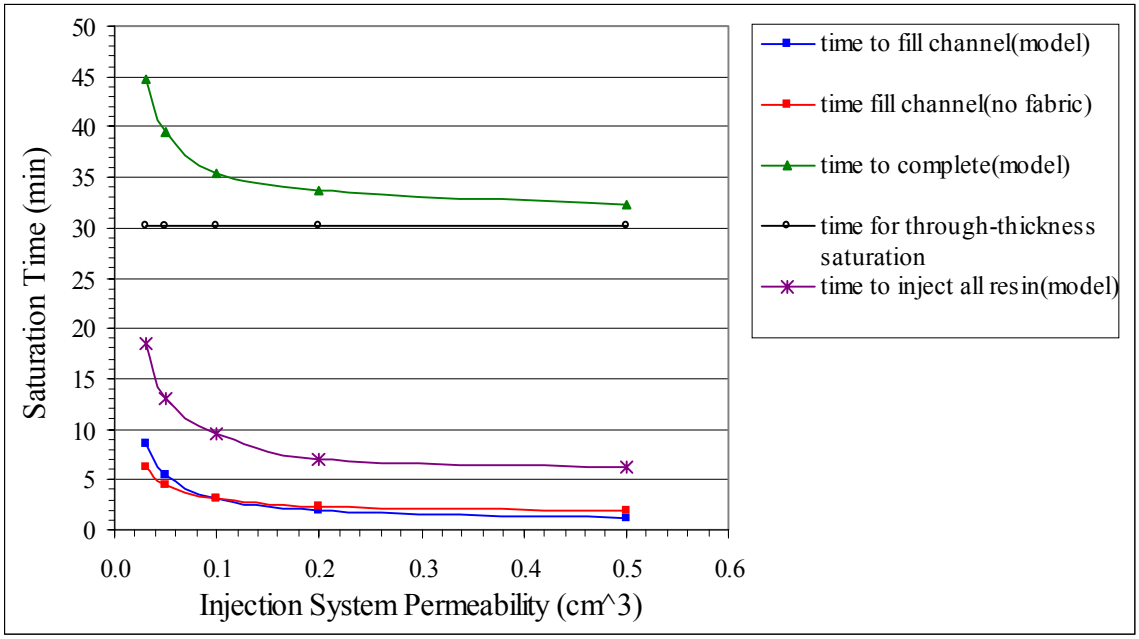


Figure 47: Effect of injection system on process time for 10 cm thick part.

The effect was not quite as large in this case, since the large part is dominated by the through thickness step. Equation 4.1 could give an accurate prediction of how the time required to fill the channel would change with the injection system. However, the change in the injection system also increased the time between when the channel was full, and when all the resin was injected. During this stage, resin is still being fed through the injection system, through the channel, and through the fabric. If a significant pressure drop occurs in the hoses, there will be less pressure to force resin though the fabric during this stage. The time required to inject all the resin is also shown in Figure 47 to show this compounding effect. This is only noticed at the lowest permeability values. In the cases

with high permeabilities, the individual equations for channel flow and through thickness flow could give a good prediction of the process time when added together. For the cases with lower permeabilites, this would still give an acceptable approximation, but the error is notable.

Injection Pressure

The effect of injection pressure is also an important consideration, since its effects can be non-linear. The injection pressure affects the compaction pressure on the fabric, which changes its thickness and permeability. This can have effects on the channel flow and the flow through the thickness.

Using the model, injection pressure was varied from 30 kPa to 110 kPa. This would be from a weak vacuum to a complete vacuum. This effect was first tested on the thin part.

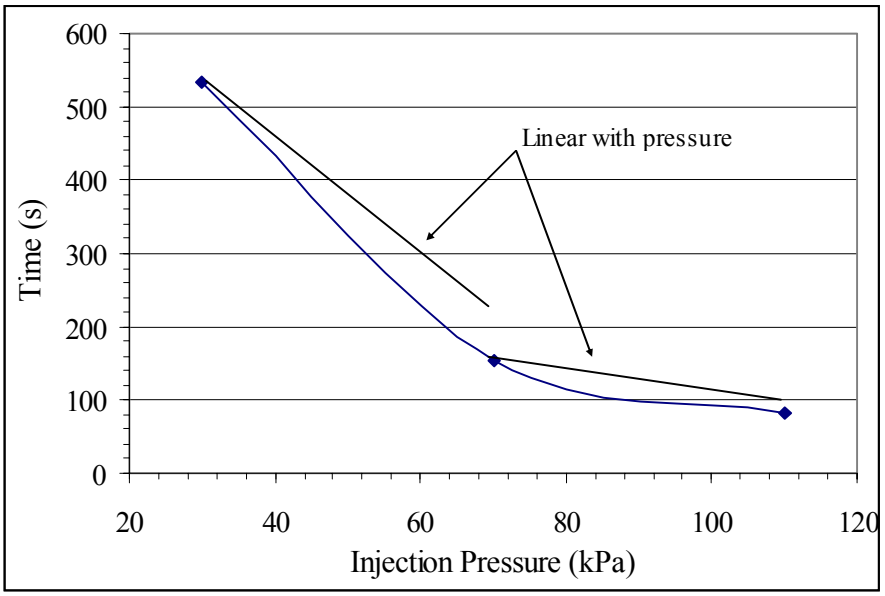


Figure 48: Effect on injection pressure on process time for .6 cm thick part.

The mold gap was again 20% of the fabric thickness. These results are shown in Figure 48.

It has been shown previously that the thin part is dominated by the channel flow. One might expect a linear relationship with pressure in this case, according to eq. 4.1. However, the injection pressure affects the overhead pressure on the fabric, which compresses the fabric and increases the channel height. This is why increasing the injection pressure has a more dramatic effect than might be expected, especially at lower pressures where the fabric is very compressible. In Figure 48 a line is drawn between the first point and the second which represents a linear decrease with pressure. From comparing this line to the line from the model, one can see that the compaction of the fabric played a significant role. From the second point to the third, a similar line is shown. In this case, the difference in times almost follows a one-to-one relationship with pressure. This is because at 70 kPa the fabric is almost fully compressed, and increasing the pressure beyond this has less effect on changing the channel height.

When varying the injection pressure for the thick part, the relationship was again non-linear. Since the thick part is dominated by the through thickness step, a good prediction of the process time could again be determined by using eq. 3.39 alone, as long as the change in permeability and fabric height were accounted for. The effect of injection pressure on the thick part is shown in Figure 49. Shown in the figure, are the calculated times for the channel flow, the through thickness step, the time to fill the channel from the model, and the time to complete the process from the model.

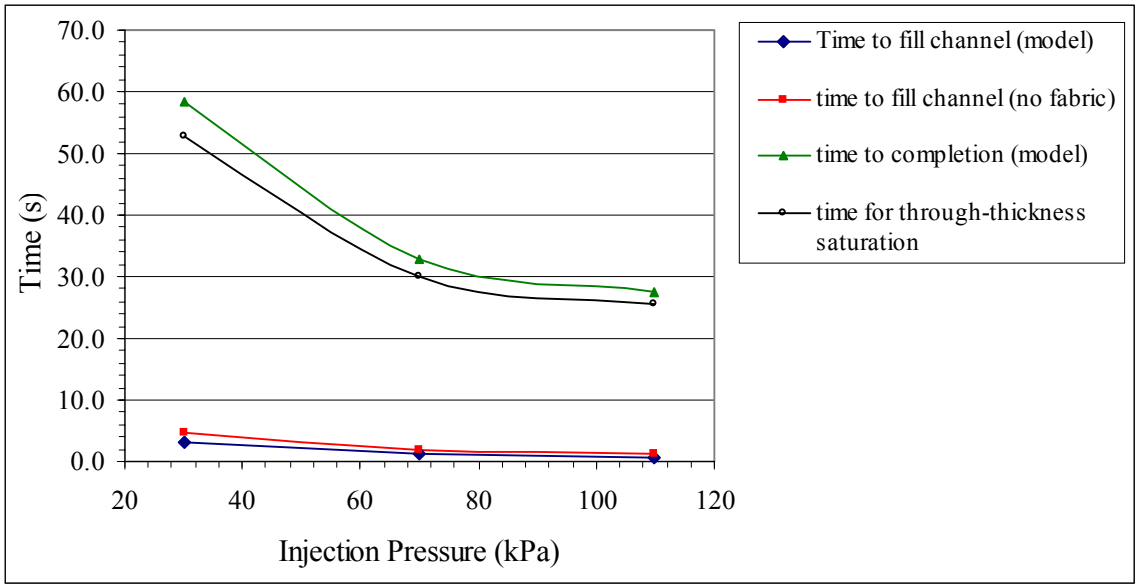


Figure 49: Effect of injection pressure on process time for 10cm thick part.

Fabric Permeability

Another parametric study was done to determine the effect of the fabric permeability on the process time. Again, the first case examined was for the .6 cm thick part with 20% mold gap. The injection pressure was 70 kPa. The permeability was varied from 1E-8 to 2E-7 cm^2, which is the approximate range of permeabilities from the fabrics tested. The results from this test are shown in Figure 50.

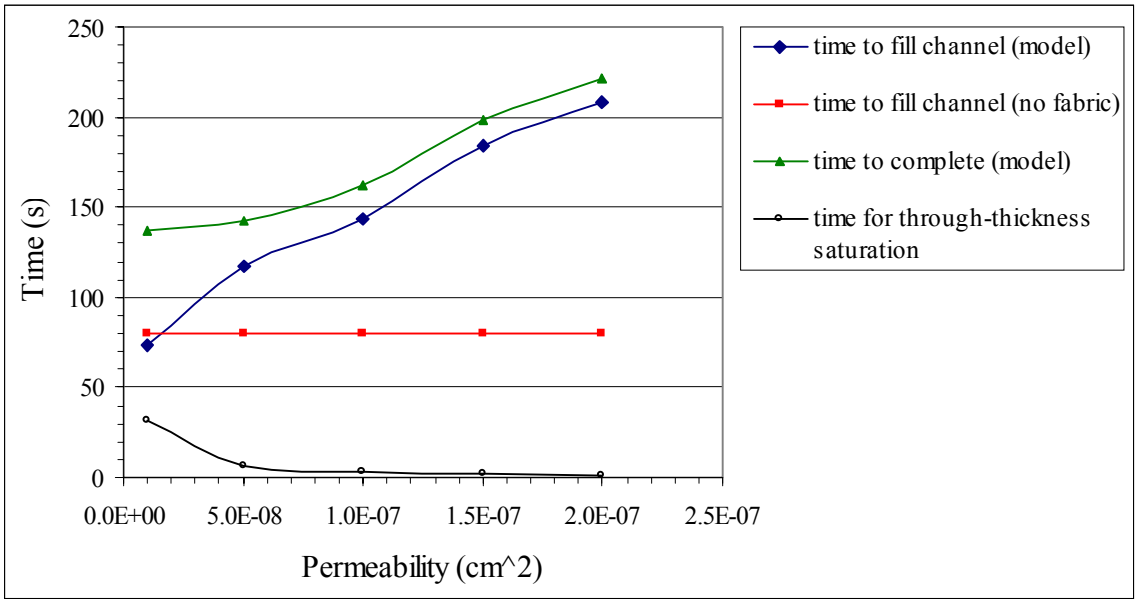


Figure 50: Effect of fabric permeability on process time for .6 cm thick part.

The results from this study were somewhat counter-intuitive. Increasing the fabric permeability actually increased the process time. It can be seen in Figure 50 that the time required for the through thickness step is small compared to the time to complete the process, except for the fabric with the lowest permeability. This means the process is still dominated by the channel flow, at least for the cases with the large permeability. In this situation, having a larger permeability means less pressure is generated in the channel above the fabric. Less pressure above the fabric means less compaction, so the channel is not opened up by pressure as much as the permeability increases. For the case with the smallest permeability, the through thickness step is becoming more significant in relation to the channel flow portion. In fact, if the through thickness time and the channel flow time were added they would give a reasonably close approximation to the time predicted for the whole process by the model.

For the large part, the influence of fabric permeability was as expected. Since the large part is dominated by the through thickness step, the total process time followed the same trend as for through the thickness only. These results are shown in Figure 51.

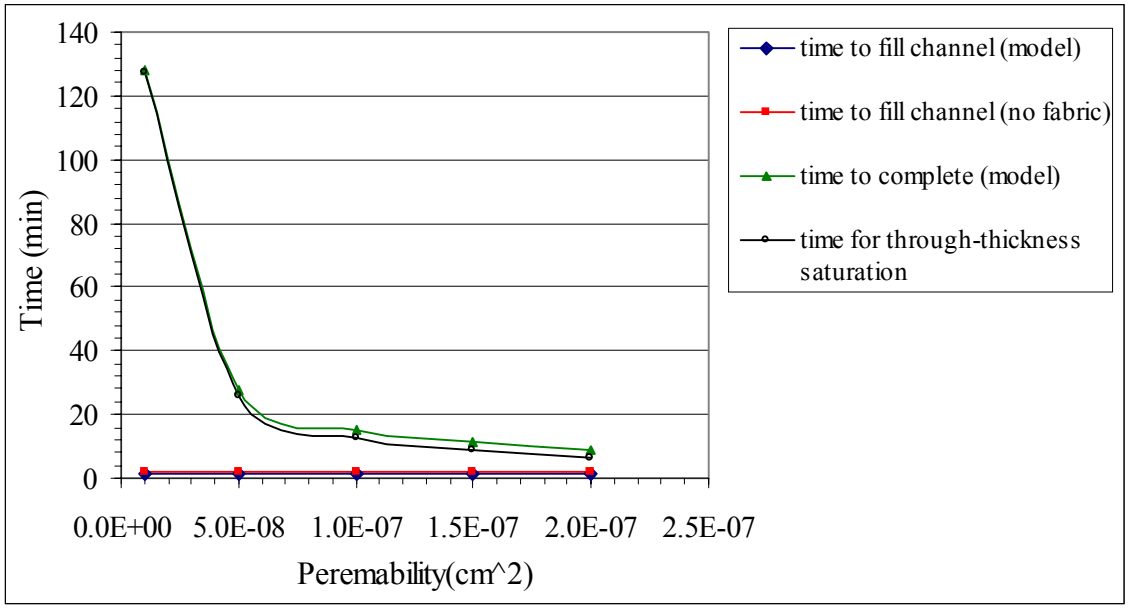


Figure 51: Effect of fabric permeability on process time for 10 cm thick part.

Fabric Thickness

In the previous examples, it has been shown that for a part where the channel flow takes much longer than the through thickness step, the individual flow equations cannot predict the total process time. For the very thick part, the through thickness stage dominates and the individual equations give a good correlation with the model. However, most parts will be somewhere in between the small part, and the large part examined here. In order to find where the individual flow equations start to become valid, the fabric thickness on the small part was increased until it became fabric dominated. The

channel height and injection system were also scaled accordingly. For this study, the relative times for the channel flow and fabric flow processes were calculated, and an error was computed at each point between the model and the prediction using equations 4.1 and 3.39. The times from the model, as well as process times from the individual equations are shown in Figure 52.

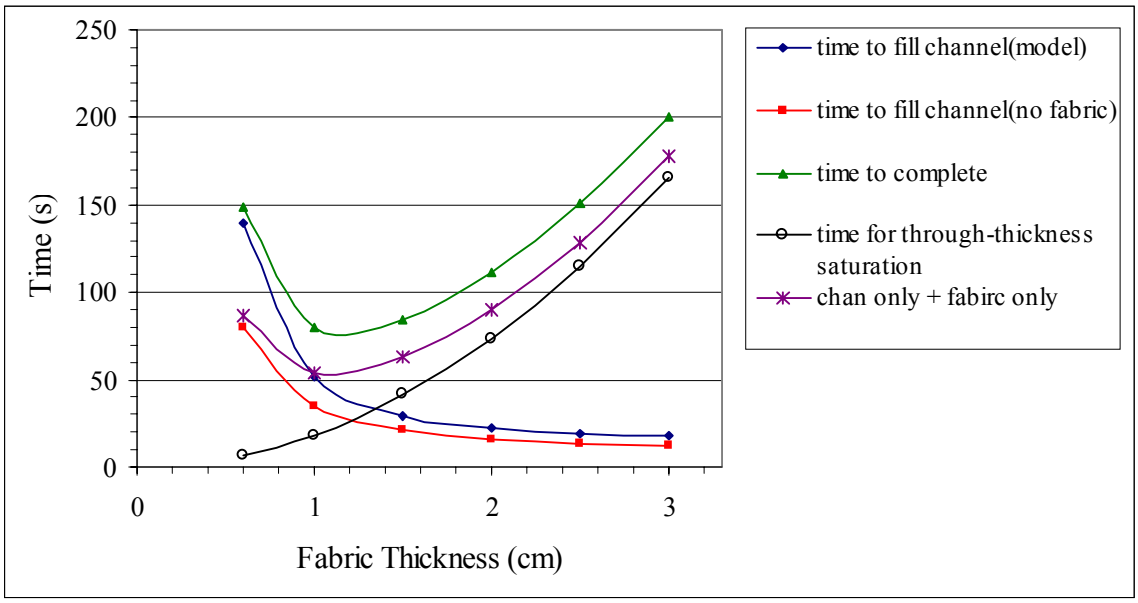


Figure 52: Effect of fabric thickness on process times.

As can be seen in the figure, the process starts out very channel dominated and ends being fabric dominated. As the process becomes more fabric dominated, the time from the individual equations is becoming much closer to the time from the model. The error, or difference between these two methods, is shown in Figure 53. Also shown in the figure is the ratio of the fabric flow process to the channel flow process. The two values are within 20% of each other when the fabric step is five times the channel flow step. For an difference of less than 10%, the fabric flow portion must be over fifteen times greater.

For the 10 cm thick part from before, the time though the thickness was approximately 30 times larger than the channel flow process.

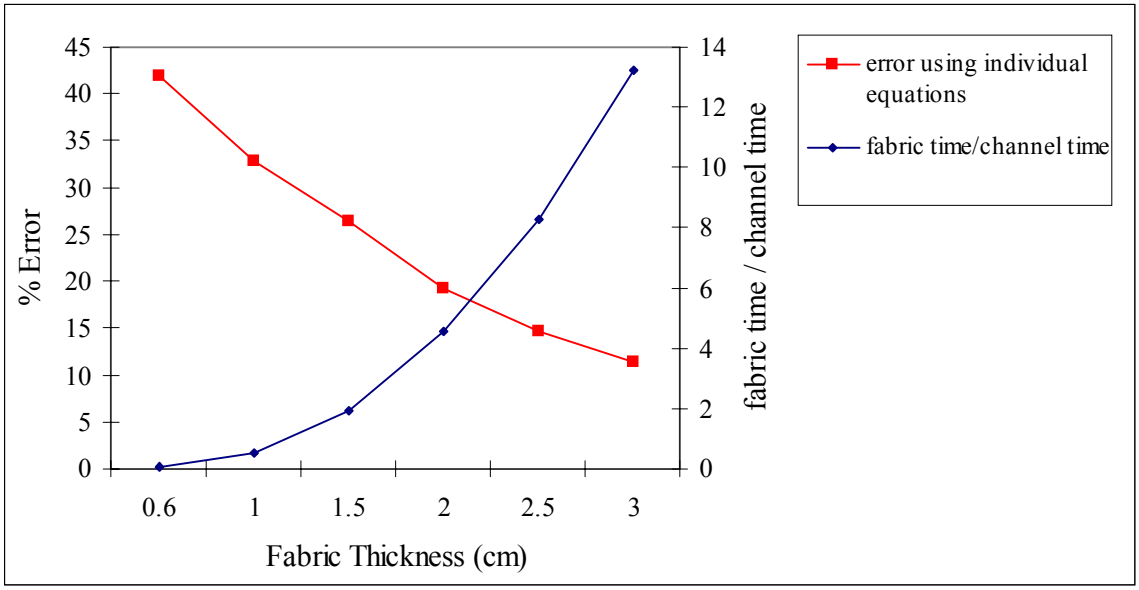


Figure 53: Error when using individual equations compared to fabric thickness.

CHAPTER 7

DISCUSSION OF RESULTS

Fabric Tests

The fabric tests demonstrated multiple important aspects of flow through porous media. Most important was the dramatic effect of compaction pressure on the fabric permeability. For the fabrics tested, the permeability decreased by a factor of 2 to 3 between 30 kPa and 140 kPa. This effect could greatly influence decisions made by mold designers. As the processing pressure increases a more robust mold will be required, which will be more costly. If increasing the operating pressure does not significantly reduce the process time, the added cost of the mold may not be justified. However, considerations such as the fiber volume fraction may dictate the compaction pressure more than processing time.

The tests also showed that the fabric thickness and fiber volume fraction were also greatly influenced by pressure. Fortunately, as the fabric is compressed the distance that the resin must flow to saturate the part through the thickness decreases. Since the saturation time was shown to be a function of the thickness squared, this can reduce the effect of the decreased permeability. In order to illustrate how these effects interact, a plot was generated to show the saturation time for a part with an initial thickness of 10 cm. For this example, the woven carbon was chosen since it had a large change in permeability and thickness with pressure. The trend from Figure 33 was extrapolated to obtain guess values for the permeability at pressures greater than 350 kPa. The results

from this study are presented in Figure 54. It can be seen in this figure how increasing the pressure over the fabric has a non-linear effect on the saturation time. In the region between 100 kPa and 300 kPa, increasing the injection pressure has a very small influence on the saturation time of the fabric. It isn't until the fabric is fully compressed that the relationship between pressure and saturation time becomes close to linear.

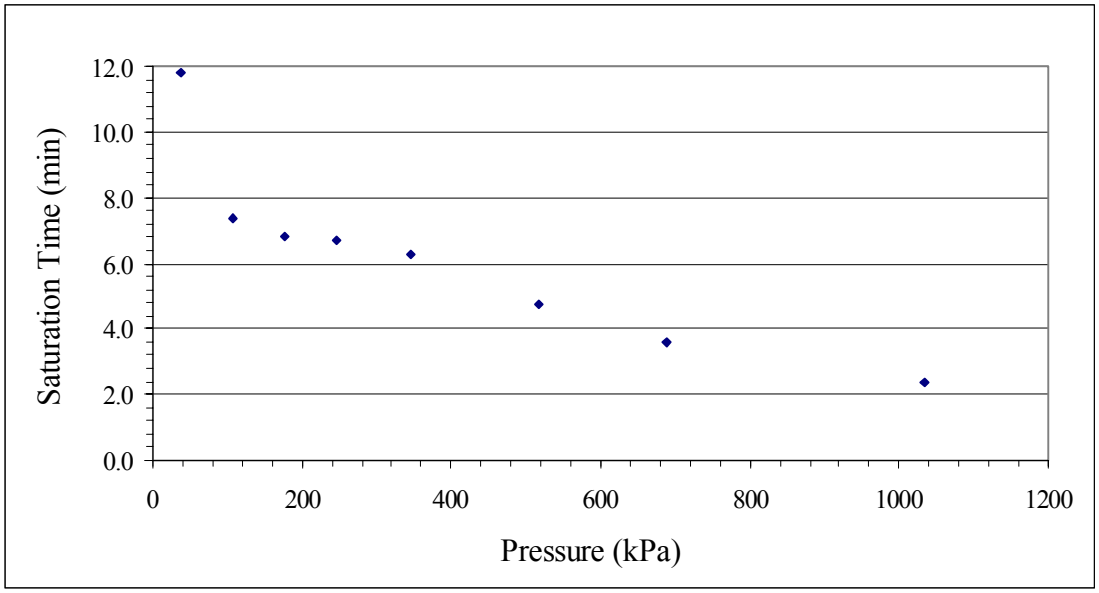


Figure 54: Effect of injection pressure on saturation time (10 cm initial thickness)

These tests also demonstrated a very large variability in the fabric permeability. Between the five coupons tested in the repeatability study, the values fluctuated within 20% of the mean value. This limits the capability to develop models with a high degree of accuracy. It also influences the repeatability of a process. Even for parts with very large areas, this variability will still be influential. As the area of a part increases, the average permeability over the whole part will approach a mean value. However, what is of most concern is the local permeability. A large part will still have regions with very high

and low permeabilities. The larger the part, the greater the chances of having very extreme local cases. If high permeability regions exist near low permeability regions, there is a risk of entrapping air pockets. This was also found to be true for in-plane flow through preforms composed of different fabrics [44]. This also means that the total process time is going to be dictated by the region with the lowest permeability. An example of this will be discussed shortly. With enough data, a statistical approach to processing could be employed where a successful part would be produced 99% of the time, rather than always planning on the worst possible case. Fortunately, since most of the variability in the through thickness permeability is due to the random alignment of the flow channels, as the part gets thicker this variability will decrease.

Air Permeability Testing

In both cases tested the permeability value from the air tests was about twice as high as the interpolated value from the liquid tests. There are a couple explanations for this result. The first is that Darcy's law was intended for creeping flow, while the air in these tests was moving at a very high velocity. In tests performed by Calhoun and Yuster, the permeability values obtained with air were higher than the ones from liquid tests. They attributed this to the fact that the mean free path of the air molecules was on the same order of the spacing between fibers [18,47]. Another major contributor to the larger values is flow around the edges. The edges were not siliconed as in the liquid tests to keep with the idea of having a rapid test procedure, so the seal was not perfect. The disks that were punched out and placed between the plies had a close fit with the inside edge of the tube, but did not create a perfect seal. These disks could have also created

enough of a space between the plies to increase the permeability, since there was no pressure to press the plies together. This would probably be a minor effect though since the disks were only 0.07 mm thick. It is possible that siliconing the edges would have given results much closer to those of the liquid tests, but this would have defeated the purpose of the air tester which was to make testing much more rapid. The use of silicone would have meant at least a day would have been required between tests. One other possibility that was not examined would be to use a thick grease or something that could be smeared around the edges to create a seal. This could not be used for the fluid tests because the pressurized fluid would have pushed it out of the way and formed a channel. However, for the air tests, since the pressures were very low a thick grease might have stayed in place. This would add a little more time in preparation and cleanup, but would still result in a very quick test.

The other drawback of the air tests is that they don't give any indication of the trend as the compaction pressure is increased. Since each fabric has a different trend at higher pressures, there is no way to predict this from just the uncompressed value. The test apparatus could be designed so that a mechanical clamping pressure could be applied to the sample rather than relying on the fluid pressure. If the sample could be clamped together by hydraulic cylinders it may be possible to know the clamping pressure, as well as the sample thickness during a test. This clamping pressure could then be adjusted to develop a curve. This is similar to the apparatus described by Hoes et al., although theirs was for in-plane permeabilities [9,46]. Another possibility would be to clamp the sample mechanically to a given thickness, and then determine the corresponding compaction

pressure through a separate test. This would be opposite to the approach used for the liquid tests.

Although the air permeability tests did not duplicate the results from the liquid tests, there is still potential in developing this technique. By improving the seals and allowing the fabric to be mechanically compressed, the tests could still be performed with relative ease compared to liquid tests. Ding et al. have achieved permeability results using air that were very close to the values from liquid tests [48]. One difference that made their tests more successful is performing in-plane tests rather than through-thickness tests. For in-plane tests they were able to flow air though the fabric over a long distance. This allowed them to develop a pressure drop that was measurable, while still keeping a low enough velocity for Darcy's law to be valid. For the through thickness tests performed in this study, the thickness of the samples was around 1 cm. This meant the velocity through the fabric had to be very high in order to generate a measurable pressure drop. The use of a much more sensitive pressure transducer, along with much thicker samples, could improve the through thickness air tests.

Comprehensive Model

Overall, the comprehensive model did a very good job of predicting the flow through the mold(e.g. Figure 37, Figure 38, Figure 40). The model was accurate in predicting the flow fronts for relatively thin parts, as well as thick parts. In all four tests, the model predicted key events with errors typically less than 15%. Given the large variability in the fabric, as well as the accumulation of errors in the input to the model, this was a very good result. The model required experimental values as input for the equivalent

permeability of the injection system, the permeability of the fabric, the compressibility of the fabric, the resin viscosity and the capillary pressure. Any errors in these values are transferred to the model before it is even run. For this reason, it is hard to identify whether the errors in the experiment are due to inaccurate input values or inadequacies within the model. However, to achieve these results, both had to be reasonably accurate.

The first two tests involved relatively thin parts, with thin channels. Both of these were represented well by the model. The fact that the part with less fabric and a thinner channel had a greater error could be expected. As the channel gets thinner the assumption that the transverse flow can be neglected in formulating equation 3.20 becomes less valid. However, since the saturation time was still within 11% of the experimental value this still appears to be a reasonable assumption. In both the first two tests, the model did a fairly accurate job of predicting the flow front on the bottom of the mold as well (Figure 37 + Figure 38).

The results from the third experiment were very encouraging. In this case the model predicted a saturation time right in the approximate range from the experiment. There are a couple of reasons for this. Having a much larger channel would have reduced the amount of transverse flow during stage one of the process. Since the fabric was also thicker, this made the process more dominated by the through thickness step. Since there were five tests done on this fabric the permeability of the fabric was well represented. Also, the fabric compaction data was very clean and fit well with a logarithmic curve. Although the fluid came through the fabric somewhat randomly at the end, there was no air trapped in the mold. The results from this test were also good since the bagging was

not used to force the resin through the thickness, which eliminated any additional complication.

The fourth test involved all aspects of the process. The test was run to completion with the use of the bagging to complete stage two of the process. When comparing the model for the saturation time to the experiment, an error of 12 - 22% was seen. There are several explanations for this. The first is the complication in the usage of the bagging. Since the pressure had to be cut off and switched from the hoses to the bagging during the process, there was a rather chaotic pressure profile to match. Another larger source of error could have come from the fabric data used in this test. The fabric used in this test was the woven roving which had less permeability data, and more scatter in the compaction data. It was also noticed during the test that a small amount of edge leakage occurred. This eventually caused the vents to be covered before the whole part was saturated, leaving a strip of unsaturated fabric down the middle. This did not occur until the very end of the process, so the amount of trapped air was small. Eventually, these regions were wet out, possibly by capillary pressure. The small amounts of trapped air must have resulted in micro-porosity, since no dry spots were found on subsequent inspection. The fact that small pockets of air were trapped would explain why it took much longer to saturate these regions than the model predicted. It is also an important illustration of the effect of fabric variability and edge leakage. This occurred in large part due to the fact that no vacuum was used to evacuate the air. The use of a vacuum would almost eliminate this possibility, although an absolute vacuum cannot be used since it would boil the resin.

Limitations of the Model

In applying this model to real manufacturing processes it will be important to understand the consequences of the assumptions, and where the limitations of the model exist. This particular model has limitations due to the fact that it is only two dimensional; however, these are not limitations of the modeling technique. The technique could be extended to three dimensions, but his would come with a great increase in complexity.

One of the assumptions that was referred to earlier was the fact that the model does not account for any racetracking. Since in the experiments the sides of the fabric were siliconed, this was only a minor issue. However, in real processes using silicone would not be practical. In the experiments, the part was relatively thick compared to its width. For example, the thickness was around 2 cm while the width was only about 12.5 cm. For a part such as a wind turbine blade, or a boat hull, the width could be 100 times the thickness. In this case, even if resin leaked around the edge it would have to flow back towards the center of the part. Once the edges were saturated this flow would essentially stop. Edge leakage could also be prevented in the design of the mold. If the distribution channel did not extend all the way to the edge, the resin would be forced to flow in the plane of the fabric before it could reach the edge. In addition, the mold could also be made to clamp down on the edges to make them very impermeable. For these reasons, the fact that the model does not account for racetracking is not considered to be a major limitation.

Another consequence of the two dimensional model is that the flow in the channel must be nearly one dimensional. In the experiments, the spacing of the injection hoses on

the leading edge of the mold was very much smaller than the length of the mold. This made the flow front normal to the flow direction. This was also aided by the well at the front of the mold. Although the resin entered the well at three points, it left as a uniform flow front. This configuration was chosen for this model since it was geared to parts such as turbine blades which are very long compared to their width. For parts of a different geometry such as a square panel, the accuracy of the model would depend on the injection system. If there were injection points at regular intervals along one edge of the part, the model would still be quite accurate. If there was only one injection port the model could loose much of its accuracy in stage one. In some processes the injection ports may not be only at one end. They could be in the middle of the part, or in multiple locations along the length of the part. This could be accounted for in the model simply by changing the boundary conditions and adding more equations. Elements of hose could be attached to any of the channel cells.

This particular model is also geared to processes where the distribution channel covers the whole surface of the part, or close to it. This is most accurate for the pressure bagging process and FASTRAC. In the parametric study, it was shown that for thick parts this would be the fastest way to saturate a part. Thinner parts on the other hand, may require a different strategy such as SCRIMP™. For processes such as SCRIMP™ where the distribution system is a series of channels which may have a large distance between them this model would not work. However, the same modeling technique could still be used, but the two dimensions would be in the plane rather than one in the plane and one in the thickness. This approach was used successfully by Han et al. to model the

processing of a boat hull using SCRIMP™ [7]. This method required all the same data that was obtained here, but the permeability values were for in the plane.

It is almost impossible to come up with any general rules as to the limitations of the model since everything is interrelated. What may be true for one case may not be true for the other. This was illustrated in the parametric study. In any case, the designer would have to use common sense and any past experience to assess how much error these assumptions will cause.

For any case, a three dimensional model is going to provide the most accurate results. However, this comes at a cost. A three dimensional model will be much more time consuming to create, and will take much more computational power to run. For example, the model created here is not a true 2D model, since it does not account for flow in the plane of the fabric. In order to make it a true 2D model the fabric would need to be broken into cells through the thickness. This would increase the number of equations by increasing the number of cells. Also, each cell would have more unknowns since the flow through all four faces would have to be determined. For a 3D model more cells would have to be added in the width of the part, and each cell would have flows through six faces. In addition to having more equations, if a finite difference technique were used the matrix would no longer be banded. This means the process of solving for the unknowns in the matrix and storing the values would be less efficient as well. It will also require much more testing to determine the permeability in all three principle directions. The complexity of the model will most likely be beyond the capability of many manufacturing engineers, and may require independently developed software packages. In many

cases, these added costs will not be worth the added accuracy over a two dimensional model.

Although some finite element packages have a porous media element, many don't. One possibility for a three dimensional model would be to use existing finite element software for heat conduction problems. With the technique that has been developed in this research, all the governing flow equations are analogous to Fourier's law of heat conduction. For example,

$$q_x = kA\frac{\partial T}{\partial x} \qquad (7.1)$$

$$v_x = \frac{K_x}{\mu}\frac{\partial P}{\partial x} \qquad (7.2)$$

Equation 7.1 is Fourier's law of heat conduction, and equation 7.2 is Darcy's law. It can be seen that the flow of energy in equation 7.1 is analogous to the flow of a fluid as in equation 7.2. Each is proportional to a resistance to flow, a flow area, and a gradient in the driving force. By letting the conductivity of a material represent the permeability divided by the viscosity, and letting temperature represent pressure a heat conduction model could be adapted for flow modeling. The mass diffusion equation is another analogous equation that could be used [25].

For this technique the commercial package would be used primarily to create the mesh, apply boundary conditions, and solve the simultaneous equations. The program would have to be capable of modeling materials with anisotropic conductivity. Even with the use of a commercial package, a large amount of programming by the user would still be required. The user would have to be able to change the geometry of the part after each time step to simulate the compressing of the fabric, as well as change in permeability.

This approach has been used successfully by Liu [21]. However, that particular model was for a closed mold process that did not have to deal with changing material properties.

One last limitation that was noticed with this model was that for very thin parts with thin channels, the solution could become unstable. In these cases the matrices would become ill conditioned. As a result, the solution vector could have negative or imaginary solutions, which are physically impossible. The .6 cm thick part with the 10% mold gap approached this condition. This condition was easy to spot since the solution would not converge or would have an imaginary solution. To alleviate this effect, increasing the number of cells in the channel helped, as well as adding a small amount of initial saturation in the fabric. Fortunately, the cases where this occurred were ones where this process would not be optimal anyway, as mentioned in the parametric study.

Parametric Study

In the parametric study a variety of parameters were examined. The purpose for this study was twofold. The first was to observe how changing the individual parameters affected the process as a whole. The other was to see how equations 3.39 and 4.1 might be useful in predicting the effects of any changes to the process.

In every case the parameters that were varied had non-linear effects on the process, some were predictable and some were not. The small part was found to be dominated by channel flow. Therefore, anything that changed the channel geometry had the largest effect. The fabric compaction under pressure significantly influenced the results since the equivalent permeability of the channel is quadratic with the channel height.

The large part was very dominated by the through thickness step. The influence of the parameters was fairly predictable.

The individual flow equations were found to be useful in predicting trends, and in some cases, gave accurate predictions for the whole process. For the thin part, the individual equations gave predictions that were very far from the values given by the model. This is because the thinner part was dominated by the channel flow. This means the time required to flow through the thickness was very small compared to the time required to fill the channel. As a result, the channel flow and fabric flow happened simultaneously. This blurs the division between channel flow and fabric flow. The fabric essentially creates an additional volume that has to be filled by passing resin through the channel.

For the thick part, these equations had good agreement with the model. This is due to the quadratic effect of fabric thickness on saturation time, which made the thick part dominated by flow through the thickness. In this case, the time to fill the channel is significantly less than the time to flow through the thickness. This also means only a small portion of the fabric is saturated during the filling of the channel. As a result, the process is almost divided into two distinct processes.

A study was done specifically to determine when the individual equations become valid. It was found that if the through thickness step was fifteen times greater than the channel flow step the individual equations were within 10% of the comprehensive model. However, there may be exceptions to this rule. A summary of the results from the parametric study is shown in Table 5. In cases where the process is channel dominated, these may only be useful in identifying trends, and not in giving definite increases in times.

Table 5: Effect of varying parameters

INJECTION SYSTEM	Effect	Comments
# of hoses	$K_{hose} \propto$ # of hoses	Eq. 3.12
Diameter of hoses	$K_{hose} \propto D^2$	Eq. 3.7
Length of hoses	$K_{hose} \propto \frac{1}{L_{hose}}$	Eq. 3.7
CHANNEL FLOW		
Channel height	$K_{chan} \propto h^2$	Eq. 3.15, Eq. 3.20
Channel length	$t \propto L_{chan}^2$	Assuming injection system is sufficiently large. Eq. 4.1
Injection system permeability	$t \propto \frac{L_{chan}^2}{K_{chan}} + \frac{L_{chan} A_{chan}}{K_{hose}}$	Eq. 4.1
Injection pressure	Increases permeability of channel(fabric dependant).	Higher injection pressure increases channel height through fabric compaction
Fabric permeability	Higher permeability increases time to fill channel.	Results in more fabric saturation. Reduces compaction pressure over fabric.
FABRIC FLOW		
Fabric thickness (z)	$t \propto z^2$	Eq. 3.39
Injection pressure	$t \propto \frac{(z(P))^2 (e(P))}{(K_f(P)) P}$ (fabric dependant)	All fabric properties change with compaction pressure. Eq. 3.39

Where:

K_{hose}	is the hose permeability	L_{chan}	is the length of the channel
D	is the diameter of the hoses	A_{chan}	is the area of the channel
L_{hose}	is the length of the hoses	z	is the thickness of the fabric
h	is the height of the channel	e	is the fabric porosity
K_{chan}	is the channel permeability	K_f	is the fabric permeability
t	is the time to fill/saturate	P	is the fluid/compaction pressure

CHAPTER 8

CONCLUSIONS AND FUTURE WORK

Pressure bag molding, and similar processes, show great potential for meeting the challenge of producing mega-watt scale wind turbine blades. In this study, the pressure bag molding process has been examined and modeled in detail. The underlying physics involved in the flow through the different regions of the process have been examined individually, and combined in a comprehensive model. The model created was successful in duplicating a series of experiments, and in revealing the effects of certain critical parameters. Through the individual equations developed, and the computer model, scaling effects in these types of processes can be determined. A procedure for locating and minimizing rate limiting steps has also been developed.

Application to Manufacturing

To summarize the work performed in developing the numerical model, a process outline has been created. The necessary data and tests that must be performed to construct a similar model are presented here.

- Tests must be performed on the fabrics to determine the permeability in the directions where most of the flow is expected to occur. Permeability values must be calculated at varying compaction pressures to create a curve fit.
- An approximate value for capillary pressure is needed. If the value is low compared to the injection pressure, it may be insignificant. However, some fabric and

resin systems have high capillary pressures, so it is important to know at least an approximate value to determine if it will be a factor.

- Tests relating compaction pressure to ply thickness and porosity must be conducted. The data should be sufficient to create an accurate compaction curve, especially at low pressures. If the compaction data can be obtained concurrently with the permeability tests this would be optimal.
- From knowledge of the fabric properties and the largest distance that the resin must flow though the fabric, the time for the fabric flow only can be determined.
- The equivalent permeability of the injection system must be determined either experimentally or by use of the equations developed here. Any fittings can create a significant pressure drop and must be included in the analysis.
- The equivalent permeability of the distribution system must be determined. For simple geometries Stokes flow equation can be used to calculate equivalent permeability. For more complex geometries, or high permeability layers, the permeability may need to be calculated experimentally.
- By knowing the equivalent permeabilities of the injection system and channel(s), and the length of the channel(s), the time for the channel flow process only can be determined
- By comparing the individual times for the fabric flow and channel flow the process the limiting step can be identified and minimized. For processes that are very largely fabric flow dominated the individual equations can be reasonably accu-

rate. For parts that are channel flow dominated, the individual equations can predict trends but are inaccurate.

- For the most accurate predictions a 2D or 3D model must be used. The model that is created must account for the effect of the net compaction pressure on permeability, fabric thickness, and porosity. These values should be continuously updated throughout the process. It should be noted that dry fabric can be compressed almost instantly, while saturated fabric takes time to compress. On the other hand, dry fabric has a limited amount of spring-back when pressure is reduced, while saturated fabric may not spring back much at all. These effects must be considered when creating a model.

Injection System / Channel Flow Modeling

The modeling of the injection system and the distribution channel used traditional pipe flow theory based on Stokes flow. The subsequent experiments performed were well represented by the analytical models. The fact that steady state equations were used to model a transient process was not an issue. This was due to the low Reynolds numbers involved and negligible surface tension effects. Also, the equations developed for flow through the channel were still accurate despite the presence of the fabric. This was due to the low permeability of the fabrics used.

Injection System / Channel Flow Future Work

For the cases examined, the equations for the injection system and channel were sufficient. For cases with very thin channels, or very high permeability fabric, the chan-

nel equation may need to be modified. In these cases the flow into the fabric may be significant enough to change the flow characteristics of the channel.

Fabric Tests

A major part of this work was to develop a permeability tester and use it to see how compaction pressure would affect the flow through the fabric. Tests revealed a very dramatic relationship between pressure and permeability. As the pressure was increased, the permeability could decrease by almost an order of magnitude. This reduction was most dramatic at lower pressures, and leveled of at high pressures when the fabric became fully compressed. In the tests performed, the experimental data had a range of +/- 20% from the mean. This has important implications in using a single permeability value to model a real process.

The capillary pressure proved to be very difficult to measure with the existing setup. This was due to the short distance traveled, and the non-uniform flow front. This test is further complicated by the dual scale flow involved in unsaturated tests.

The air permeability tests were not successful in duplicating the results from the fluid tests. However, there is still potential in using air for permeability tests. Several improvements were identified that would help the air tester to give accurate values, yet still make testing very quick and easy. These are identified in the future work section.

It has also been found in this study that the compaction of fabric can have a dramatic effect on one-sided molding processes. Most fabrics will compress from 50% to 70% of their original thickness. This compaction influences the through thickness flow step, as well as the channel flow stage by changing the channel geometry. The effect of

pressure is very extreme at low pressures, and eventually levels off once the fabric is fully compressed. Fabric thickness versus pressure can be fitted with power law, or logarithmic fits. However, it is best fit by non-linear techniques that divide the process into three distinct regions.

Compaction pressure also has similar effects on the fabric porosity. As the pressure is increased, the porosity is decreased. This increases the velocity through a preform by reducing the effective flow area. Porosity also affects capillary pressure, but this may be neglected in many cases since the capillary pressure is small to begin with.

Fabric Test Future Work

One of the largest sources for error in generating the data for the model was in how the thickness was determined during the permeability tests. Rather than using compaction data from separate tests, it would be much better to measure the fabric thickness directly during the test. This would require at least a modification to the existing apparatus, or possibly a new apparatus.

Fabric compaction tests should also be done on thick stacks of fabric (> 5 plies). The data used in this study was generated from points taken from different fabric stacks. This gives a good representation of the scatter in the data, and gives a good average value. However, it may be better to develop a method where the same stack of fabric is compressed through the range of pressures, so the data can be fit better with a curve. The best fit would be a piecewise fit as presented by Chen et al. [15]. This method would also require a minimum of tests.

The air permeability tester also deserves further development. Possible improvements could come from thicker coupons, with lower velocities. This would require a very sensitive pressure transducer, but may improve data by reducing the Reynolds number. Better sealing could also be accomplished by the use of a silicone grease around the fabric. This should give a good seal, and still be fast to apply and clean up. The last improvement would be to compress the fabric mechanically. Either the fabric thickness or the clamping pressure would need to be known in this case, or both.

Comprehensive Model

The experiments performed to validate the comprehensive model were in good agreement with the model. The model did a good job of predicting the movement of the flow fronts, and the time to saturate the part. Errors of less than 15% were typical. It was observed that the variability of the fabric as well as edge effects can create non-uniform flow fronts. A non-uniform flow front can cause the process to take measurably longer than the model predicts. Although the permeability used in the model is an average value, the process could be limited by the region with the lowest permeability. It tuned out to be very important to account for changes in permeability and fabric thickness in the model. Both of these could change by a factor of two during the process. The assignment of the hoses and distribution channel with efffective permeabilites proved to be a valid technique. This enabled a control volume technique similar to the Hardy Cross method to be used. Equivalent permeabilites could also be use with finite difference or finite element analysis.

It was also shown that the individual governing equations for each region of the mold could be useful in determining how changing parameters affects the process. For processes that are largely channel flow dominated, these equations were only capable of predicting trends. For parts that are largely dominated by the through thickness step, these equations gave good predictions of the total process time.

Comprehensive Model Future Work

Improvements to the comprehensive model might be made by a more accurate model of fabric compression. In the current model, the saturated fabric is considered to be uncompressible, and assigned a uniform permeability. In reality, it may compress slowly over time as it rejects extra resin. It may also have a varying permeability through the thickness. To be very precise, these things would have to be accounted for. However, this would require a more sophisticated model, and may be overshadowed by much larger sources of error such as fabric variability.

For modeling very thin parts, the matrices may need to be reconditioned or constrained to positive values. In extreme cases, the model could become unstable due to ill conditioned matrices.

The model could also be adapted to account for the gelling of the resin. The resin viscosity could easily be entered as a function of time rather than a constant value. This would make the model more accurate for processes using real resin.

For testing purposes, a test mold with more pressure transducers above the channel would give more means of comparing the model to the experiment. In the tests performed here, only the flow fronts and saturation time were compared.

REFERENCES CITED

1. B. D. Agarwal, L. J. Broutman, *Analysis and Performance of Fiber Composites*, Wiley, New York, 1980.

2. P.K Mallick, *Fiber Reinforced Composites: Materials, Manufacturing, and Design*, Marcel Dekker Inc., New York, 1988.

3. H.J. Sutherland, "On the Fatigue Analysis of Wind Turbines," SAND99-0089, July 1999.

4. R.S. Parnas, *Liquid Composite Molding*, Carl Hanser, Munich, 2000.

5. D.A. Griffen, T.D. Ashwill, "Alternative Comoposite Materials for Megawatt-Scale Wind Turbine Blades: Design Considerations and Recommended Testing," 2003 ASME Wind Energy Symposium, AIAA-2003-0696, 191-201.

6. D. S. Cairns, D.R. Humbert, J.F Mandell, "Modeling of Resin Transfer Molding of Composite Materials with Oriented Unidirectional Plies," *Composites Part A: Applied Science and Manufacturing*, Mar 1999, Vol. 30, 375-383.

7. K. Han, S. Jiang, C. Zhang, B.Wang, "Flow Modeling and Simulation of SCRIMP™ for Composites Manufacturing," *Composites Part A*, Jan 2000, Vol. 31, 79-86.

8. R. Pan, Z. Liang, C. Zhang, B. Wang, "Statistical Characterization of Fiber Permeability for Composite Manufacturing," *Polymer Composites*, December 2000, Vol.21, No.6, 996-1006.

9. K. Hoes, D. Dineseu, H. Sol, M. Vanheule, R. Parnas, Y. Luo, I. Verpoest, "New Set-up for Measurement of Permeability Properties of Fibrous Reinforcements for RTM," *Composites Part A* 2002, Vol 33, No. 7, 959-969.

10. J.F. Mandell, D.D. Samborsky, D.S. Cairns, "Fatigue of Composite Materials and Substructures for Wind Turbine Blades," SAND 2002-0771, March 2002

11. J. A. Schey, *Introduction to Manufacturing Processes*, McGraw-Hill, New York, 2000.

12. D.R. Askeland, *The Science and Engineering of Materials*, PWS Publishing Co., Boston, 1994

13. J.F. Mandell, D.D. Samborsky, N.K Wahl, H.J. Sutherland, "Testing and Analysis of Low Cost Composite Materials Under Spectrum Loading and High Cycle Fatigue Conditions," Proceedings of The 14th International Conference

on Composite Materials (ICCM-14), Society of Manufacturing Engineers, San Diego, California, July 14 - 18, 2003. Paper 1811. (2003)

14. J.D Skramstad, "Evaluation of Hand Lay-Up and Resin Transfer Molding in Composite Wind Turbine Blade Manufacturing," Master's Thesis in Mechanical Engineering, Montana State University-Bozeman, August 1999.

15. B. Chen, A.H.-D. Cheng, T.-W. Chou, "A Nonlinear Compaction Model for Fibrous Preforms," *Composites Part A: Applied Science and Manufacturing*, May 2001, Vol. 32, 701-707.

16. B.R. Gebart, "Permeability of Unidirectional Reinforcements for RTM," *Jounal of Composite Materials,* 1992,Vol. 26, No.8, 1100-1133.

17. E. Larson, "Pressure Bag Molding: Manufacturing, Mechanical Testing, Nondestructive Evaluation, and Analysis," Master's Thesis in Mechanical Engineering, Montana State University-Bozeman, January 2004.

18. S. Rossell, "Fluid Flow Modeling of Resin Transfer Molding for Composite Material Wind Turbine Blade Structures," Master's Thesis in Chemical Engineering, Montana State University-Bozeman, August 2000.

19. P. Simacek, E.M. Sozer, S.G. Advani, "User Manual for DRAPE 1.1 and LIMS 4.0 (Liquid Injection Molding Software)," University of Deleware Center for Composite Materials Technical Report, CCM Report 98-01, 1998.

20. S.G. Advani, *Composite TechBrief: Liquid Injection Molding Simulation (LIMS),* University of Deleware Center for Composite Materials, 2004, http://www.ccm.udel.edu/Pubs/techbriefs/LIMS.pdf

21. X.L. Liu, "Isothermal Flow Simulation of Liquid Composite Molding," *Composites Part A: Applied Science and Manufacturing*, Dec 2000, Vol. 31, 1295-1302.

22. M. K. Kang, W.I Lee, H.T. Hahn, "Analysis of Vacuum Bag Resin Transfer Molding Process," *Composites Part A: Applied Science and Manufacturing,* Nov 2001, Vol. 32, 1553-1560.

23. W.D Brouwer, E.C.F.C van Herpt, M. Labordus, "Vacuum Injection Moulding for Large Structural Applications," *Composites Part A: Applied Science and Manufacturing*, Jun 2003, Vol. 34, 551-558.

24. H. Cross, "Analysis of Flow in Networks of Conduits or Conductors," University of Illinois Bulletin No. 286. November 1936.

25. R. B. Bird, W. E. Stewart, E. N. Lightfoot, *Transport Phenomena*, John Wiley & Sons, New York, 2002.

26. F. White, *Fluid Mechanics*, McGraw-Hill, New York, 1999.

27. H. D'arcy, Les Fontaines Publiques de la Ville de Dijon, Paris, 1856

28. A. Hammami, R. Gauvin, F. Trochu, "Modeling the Edge Effect in Liquid Composites Molding," *Composites Part A: Applied Science and Manufacturing*, Jan 1998, Vol. 29, 603-609.

29. J.F. Delerue, S.V. Lomov, R.S. Parnas, I. Verpoest, and M. Wevers, "Pore Network Modeling of Permeability for Textile Reinforcements," *Polymer Composites*, June 2003, Vol. 24, No. 3, 344-357.

30. P. Simacek, S. G. Advani, "Permeability Model for a Woven Fabric," *Polymer Composites*, December 1996, Vol. 17, No. 6, 887-899.

31. P. Ferland, D. Guittard, F. Trochu, "Concurrent Methods for Permeability Measurement in Resin Transfer Molding," *Polymer Composites,* February 1996, Vol. 17, No. 1, 149-158.

32. Y. Lai, B. Khomami, J. L. Kardos, "Accurate Permeability Characterization of Preforms Used in Polymer Matrix Composite Fabrication Processes," *Polymer Composites*, June 1997, Vol. 18, No. 3, 368-377.

33. K. L. Adams, L. Rebenfeld, "Permeability Characteristics of Multilayer Fiber Reinforcements. Part 1: Experimental Observations," *Polymer Composites*, June 1991, Vol. 12, No. 3, 179-185.

34. R. Parnas, K. Flynn, M. Dal-Favero, "A Permeability Database for Composites Manufacturing," *Polymer Composites*, October 1997, Vol. 18, No.5, 623-633.

35. K. J. Ahn, J. C. Seferis, J. C. Berg, "Simultaneous Measurements of Permeability and Capillary Pressure of Thermosetting Matrices in Woven Fabric Reinforcements," *Polymer Composites*, June 1991, Vol. 12, No. 3, 146-152.

36. L. Skartsis, B. Khomami, J.L. Kardos, "The Effect of Capillary Pressure on the Impregnation of Fibrous Media," *SAMPE Journal,* October 1992, Vol. 28, No. 5, 19-23.

37. R.F. Probstein, *Physiochemical Hydrodynamics*, Butterworth-Heinemann, Boston, 1989

38. R. Parnas, J.G. Howard, .T L. Luce, S. Advani, "Permeability Characterization. Part 1: A Proposed Standard Reference Fabric for Permeability," *Polymer Composites*, December 1995, Vol. 16, No.6, 429-445.

39. Y. Luo, I. Verpoest, K. Hoes, M. Vanheule, H. Sol, A. Cardon, " Permeability Measurement of Textile Reinforcements with Several Test Fluids," *Composites Part A*, 2001, Vol. 32, No. 10, 1497-1504.

40. J. A. Acheson, P. Simacek, S.G. Advani, "The Implications of Fiber Compaction and Saturation on Fully Coupled VARTM Simulation," *Composites Part A: Applied Science and Manufacturing*, Feb 2004, Vol. 35, 159-169.

41. S. Bickerton, M.J. Buntain, A.A. Somashekar, "The Viscoelastic Compression Behavior of Liquid Composite Molding Preforms," *Composites Part A: Applied Science and Manufacturing*, May 2003, Vol. 34, 431-444.

42. C Lekakou, M. A. K. B. Johari, and M. G. Bader, "Compressibility and Flow Permeability of Two Dimensional Woven Reinforcements in the Processing of Composites," *Polymer Composites,* October 1996, Vol. 17, No. 5, 666-672.

43. T. G. Gutowski, Z. Cai, J. Kingery, S. J. Wineman, "Resin Flow/Fiber Deformation Experiments," SAMPE Q 1986; 17(4), 54-58.

44. J. Mogavero, S. G. Advani, "Experimental Investigation of Flow through Multi-Layered Preforms," *Polymer Composites,* October 1997, Vol. 18, No. 5, 649-655.

45. H. Lee, K. Neville, *Handbook of Epoxy Resins*, McGraw-Hill, New York, 1967

46. T. Luce, S. Advani, J. G. Howard, R. Parnas, "Permeability Characterization. Part 2: Flow Behavior in Multiple Layer Preforms," *Polymer Composites,* December 1995, Vol. 16, No. 6, 446-458.

47. J.C. Calhoun, S.T. Yuster, "A Study of the Flow of Homogeneous Fluids through Porous Media," *Drilling and Production Practice*, 1946

48. L. Ding, C. Shih, Z. Liang, C. Zhang, B. Wang, "In Situ Measurement and Monitoring of Whole-Field Permeability Profile of Fiber Preform for Liquid Composite Molding," *Composites Part A: Applied Science and Manufacturing*, Aug 2003, Vol. 34, 779-789.

49. J.R. Weitzenbock, R.A. Shenoi, P.A. Wilson, "Measurement of Three-Dimensional Permeability," *Composites Part A: Applied Science and Manufacturing*, Jan 1998, Vol. 29, 159-169.

APPENDICES

APPENDIX A

MATLAB PROGRAM FOR ENTIRE PROCESS

MATLAB PROGRAM FOR ENTIRE PROCESS

```
function final_cm= final_cm(K_h, Lh, Lw, Hm, Wm, Lm, Hc, C, Papp, rho, mu)
% stage1(Kh, Lh, Lw, Hm, Wm, Lm, Hc, C, Papp, rho, mu)

%  final_cm(1.31E-4,100,6, .72, 12, 200, .12, 93, 7, .0013,.00003)

%definition of inputs

%   K_h = permeability of hose system (cm^3)
%   Lh = length of hoses (cm) (for plotting purposes only)
%   Lw = length of the well (cm)
%   Hm = Height of the mold (cm) (fabric + channel)
%   Wm = width of the mold (cm)
%   Lm = length of the mold (cm) (or fabric length)
%   Hc = height of the channel (cm)
%   C = correction term for channel aspect ratio
%   Papp = Applied pressure (N/cn^2)
%   rho = fluid density (kg/cm^3)
%   mu = fluid viscosity (N*s/cm^2)

% this program will simulate the filling of a mold and give plots of the
% resin progress as a function of time as well as calculate the total time
% required to fill the mold.

%setting up time increment
t = 0;
dt = 1;

%%%%%%%%%%%%%%%%%%%%%%%% creating the cells %%%%%%%%%%%%%%%%%%%%%%%%

Ndiv_Lh = 15;                                   %this is the number of nodes in the hose
Ndiv_Lw = 10;                                    %this is the number of nodes in the length of the well
Ndiv_Lm = 140;                                   %this is the number of nodes in the length of the mold

Ndiv_Ltot = Ndiv_Lh + Ndiv_Lw + Ndiv_Lm;        %calculating the total length of the mold

Ndiv_Hm = 23;                                   %this is the number of nodes in the height of the mold
Ndiv_Hc = 3;                                    %this is the number of nodes in the mold channel
Ndiv_Hf = Ndiv_Hm - Ndiv_Hc;                     %this calculates the number of nodes in the fabric
Hfl = Hm - Hc;                                   %this calculates the height of the fabric

Ndiv_Hh = 3;                                    % number of divisions in the height of the hose

Ndiv_Hfl = Ndiv_Hm - Ndiv_Hc ;                  %this calculates the number of nodes in the fabric

height = Hfl;                                    %definitions for plot title
width = Wm;
length = Lm;

%%%%%%%%%%%%%%%%%%%%%%%% initial parameters %%%%%%%%%%%%%%%%%%%%%%%%

K_f = inline('(2.02*10^-10 * P^2 - 6.7*10^-9 * P + 7.82*10^-8)') ;      %permeability of the fabric
%K_f = inline('(4*10^-8)') ;                                             % constant permeability
%K_f = inline('(0)') ;                                                   %no fabric


Tf = inline('(-.0631*log((P+.001)*10) + 1.073)');                       %ply thickness fraction
%Tf = inline('(1)')                                                     %no compaction

hyd_dia = 2 * Hc * Wm / (Hc +  Wm)                                      %defining the hydraulic diameter
```

```
K_ch = (hyd_dia^2)*2/(C)                                        %permeability of the channel

del_x = Lm / Ndiv_Lm ;                                          %length of each fabric column
A_f = (Wm *del_x);                                              %area of each fabric column
A_ch = Wm * Hc ;                                                %area of channel

P_cap = .4;                                                     %capillary pressure

fib_vol = .5;                                                   %fiber volume fraction
e = 1 - fib_vol;                                                %porosity

fig = figure;
set(gcf,'Color',[1,1,1]);
cmap = [1 1 1; .75 .75 .75;0 .6 1;0 .3 1; 0 0 0 ];              %creating custom colors for plots
colormap(cmap)

V_inj = Hf1  * Wm * Lm * e *1.3                                 %volume of resin to inject
%V_inj = .0022

%%%%%%%%%%%%%%%%%% Filling in Xposition matrix  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%
for j = 1 : Ndiv_Hm;
   for a = 1:Ndiv_Lh;
      Xpos(j,a) = (a)*Lh/(Ndiv_Lh);                             % nodes for hose
   end

   for b = Ndiv_Lh : Ndiv_Lh + Ndiv_Lw
       Xpos(j,b) = Lh + (b-Ndiv_Lh)*Lw/Ndiv_Lw;                 % nodes for well
   end

   for c = Ndiv_Lh + Ndiv_Lw : Ndiv_Ltot
      Xpos(j,c) = Lh + Lw + (c - Ndiv_Lh - Ndiv_Lw)*Lm/Ndiv_Lm; %nodes in mold
   end
end
%%%%%%%%%%%%%%%%%% creating Y position matrix  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%
for j = 1 : Ndiv_Ltot
   for a = 1 : Ndiv_Hc
      Ypos(a,j) = Hm - a*Hc/Ndiv_Hc;                            %nodes in the channel
   end
   for b =  1 : Ndiv_Hf1
      Ypos(b + Ndiv_Hc,j) = Hm - Hc - b*Hf1/Ndiv_Hf;            %nodes in the fabric
   end
end
%%%%%%%%%%%%%%%%%% Creating the fill matrix for plotting %%%%%%%%%%%%%%%%%%%%%%%%%%%%%

% creating fill matrix color background
for i = 1:Ndiv_Hm+9
   for j = 1:Ndiv_Ltot+7
       F(i, j) = 1;
   end
end
% creating fill matrix color for hose
for i = 1 : Ndiv_Lh
   for j = Ndiv_Hm-Ndiv_Hh : Ndiv_Hm
       F(j+4,i)=0;
   end
end
% creating fill matrix color for well
for i = Ndiv_Lh + 1 : Ndiv_Lh + Ndiv_Lw
   for j = 1 : Ndiv_Hm
       F(j+4,i) = 0;
   end
end
% creating fill matrix color for mold gap
for i = Ndiv_Lh + Ndiv_Lw + 1 : Ndiv_Ltot
    for j = 1 : Ndiv_Hc
       F(j+4,i) = 0;
    end
```

```
end

 F(1,Ndiv_Ltot) = 0;       %creating vent
 F(2,Ndiv_Ltot) = 0;
 F(3,Ndiv_Ltot) = 0;
 F(4,Ndiv_Ltot) = 0;


% creating fill matrix color for fabric
for i = 1 : Ndiv_Lm
    for j = Ndiv_Hc+1 : Ndiv_Hm
        F(j+4,i + Ndiv_Lh + Ndiv_Lw) = .25;
    end
end

%%%%%%%%%%%%%%%%%%%%%%%% filling the hoses  %%%%%%%%%%%%%%%%%%%%%%%%
   %updating fill matrix for hose
   for i = 1 : Ndiv_Lh
      for j = Ndiv_Hm-Ndiv_Hh : Ndiv_Hm
         F(j+4,i)=.75;
      end
   end

%%%%%%%%%%%%%%%%%%%%%%%% filling up the well %%%%%%%%%%%%%%%%%%%%%%%%

Vol_well = Hm * Wm * Lw;                                        %defining volume of well
flow_hose = K_h * Papp / mu;                                    %defining flow rate through hoses
height_well = 0;                                                %setting initial height of the well

while height_well < Hm
   t = t+dt;

   flow_hose = K_h * Papp / mu;
   height_well = flow_hose * t / (Wm*Lw);                       % height of fluid in well

      %updating fill matrix
      for i = Ndiv_Lh + 1 : Ndiv_Lh + Ndiv_Lw
         for j = 1 : Ndiv_Hm
            if height_well > Ypos(j,i)
               F(j+4,i) = .75;
            end
         end
      end
end

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%filling the mold gap and fabric (Stage 1A)  %%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

ti = t;                                         % defining initial time
mu2 = mu*1;                                     % correction for different temperature in mold
V_tot = 0;                                      % defining initial value for total volume
dt = 1;                                         % re-defining time step
x_chan = .02*Lm;                                % initial value of x_chan to avoud division by zero in first calculation

P(Ndiv_Hm,Ndiv_Lm) = zeros;                     %initial values in the pressure matrix above fabric

P_chan = .01*Papp;                              %initial pressure in the mold

for i = 1:Ndiv_Lm

   K_f_P(1,i) = K_f(P_chan);                    %initial permeability matrix

   Tf_P_new(1,i) = 1;                           % initial thickness fraction matrix

   Ycol(1,i) = .04 * ( Hf1 );                   % initial penetration into the fabric to avoid division by zero
```

```
   Hf_u_new(1,i) = Hf1*.96;                          %initial height of unsaturated fabric

    H_chan(1,i) = Hc ;                               %initial channel height above each column

    hyd_dia_mat(1,i) = 2 * Hc * Wm / (Hc+  Wm);   %defining the hydraulic diameter

    K_ch_mat(1,i) = (hyd_dia^2)*2/(C) ;              %permeability of the channel

    A_ch_mat(1,i) = Wm * Hc;                         % area of channel above column

end

%%%%%%%%%%%%%%%%%%%%%%%%%%% entering first loop %%%%%%%%%%%%%%%%%%%%%%%%%%%
while x_chan < Lm

   if V_tot > V_inj                                  %checking to see if all the resin has been injected
      break
   end

   x_cells = x_chan/del_x;                           %calculating the number of cells needed in the matrix
   x_cells = round(x_cells);                         %rounding to nearest integer

   for i = 1:3*x_cells+2                             %setting initial matrix values to zero
      for j = 1:3*x_cells+2
         Coef_mat( i, j) = 0;
         S_mat(i,1) = 0;
      end
   end

   %generating solution vector
   S_mat(3*x_cells+1,1) = Papp*K_h/mu;

   for i = 1 : x_cells
         if Hf_u_new(1,i) > 0                        %checking to see if resin has reached the bottom of the mold
            S_mat(i,1) = A_f * K_f_P(1,i) * P_cap / (mu * Ycol(1,i));
         else
            S_mat(i,1) = 0;                          %if resin has reached bottom Kf for that cell is zero
         end
   end

%%%%%%%%%%%%%%%%%%%%%%%% generating coefficient matrix %%%%%%%%%%%%%%%%%%%%%%%%

    for d = 1 : x_cells

    Coef_mat(d,d) = 1;

         if Hf_u_new(1,d) > 0                        %checking to see if resin has reached the bottom of the mold
            Coef_mat(d,2*x_cells + 1+d) = -A_f * K_f_P(1,d) / ( 2 * mu2 * Ycol(1,d));
            Coef_mat(d,2*x_cells + 2+d) = -A_f * K_f_P(1,d) / ( 2 * mu2 * Ycol(1,d));
         else
            Coef_mat(d,2*x_cells + 1+d) = 0;         %if resin has reached bottom Kf for that cell is zero
            Coef_mat(d,2*x_cells + 2+d) = 0;
         end

    Coef_mat(x_cells+d,d) = -1;
    Coef_mat(x_cells+d,x_cells+d) = 1 ;
    Coef_mat(x_cells+d,x_cells+1+d) = -1;

    Coef_mat(2*x_cells+d,x_cells+1+d) = 1;
    Coef_mat(2*x_cells+d,2*x_cells+1+d) = -A_ch_mat(1,d)*K_ch_mat(1,d)/(mu*del_x);
    Coef_mat(2*x_cells+d,2*x_cells+2+d) = A_ch_mat(1,d)*K_ch_mat(1,d)/(mu*del_x);

    Coef_mat(3*x_cells+1 , x_cells+1) = 1;
    Coef_mat(3*x_cells+1 , 2*x_cells+2) = K_h/mu;

    Coef_mat(3*x_cells+2 , 3*x_cells+2) = 1;
```

```
 end

Coef_mat;
S_mat;
Unk_mat = Coef_mat\S_mat;

%now calculate the flow into each column of fabric
flow_fabric = 0;                                        %initial value

      for i = 1:x_cells
            v_column(1,i) = Unk_mat(i,1)/(A_f*e);     %porosity term added to get actual velocity for each column
            Ycol(1,i) = Ycol(1,i) + v_column(1,i)*dt;
            del_Ycol(1,i) = v_column(1,i)*dt;
      end

%%%%%%%%%%%%%%%%%% accounting for fabric compressing %%%%%%%%%%%%%%%%%%%%%

      for i = 1:x_cells                                 %updating permeability of each column as function of pressure
         K_f_P(1,i) = K_f(Unk_mat(2*x_cells+1+i));
      end

      Tf_P_old = Tf_P_new;
      Hf_u_old = Hf_u_new;
      vol_add = 0;

      for i = 1: x_cells                                                    % thickness fraction matrix

      Tf_P_new(1,i) = Tf(Unk_mat(2*x_cells+1+i));
                    if Tf_P_new(1,i)>1                                      % thickness fraction cannot exceed one
                        Tf_P_new(1,i) = 1;
                     else  Tf_P_new(1,i) = Tf_P_new(1,i);
                    end

      Hf_u_new (1,i)= (Hf_u_old(1,i) - del_Ycol(1,i)) *  Tf_P_new(1,i) /  Tf_P_old(1,i) ;

      H_chan(1,i) = Hm -Ycol(1,i) - Hf_u_new(1,i);                          %height of channel above fabric

      hyd_dia_mat(1,i) = 2 * H_chan(1,i) * Wm / (H_chan(1,i) +  Wm);        %defining the hydraulic diameter

      K_ch_mat(1,i) = (hyd_dia_mat(1,i)^2)*2/(C) ;                          %permeability of the channel

      A_ch_mat(1,i) = Wm * H_chan(1,i);                                     % area of channel above column

      delta_Hf = (Hf_u_old(1,i) - del_Ycol(1,i)) - Hf_u_new(1,i);           % calculating the change in fabric height

      vol_add = vol_add + delta_Hf * Wm*del_x;                              %calculating the extra volume created
     end

 t = t + vol_add / flow_hose ;                                              % accounting for time to fill new volume
 V_tot = V_tot + vol_add;

%%%%%%%%%%%%%%%%%%%%%% flow through channel %%%%%%%%%%%%%%%%%%%%%%%%%%

   flow_chan = Unk_mat(2*x_cells+1,1);                                      %calculating the flow through the last cell of channel
   flow_h = Unk_mat(x_cells+1,1);
   V_tot = V_tot + flow_h * dt;
   P_1 = Unk_mat(2*x_cells+2,1);
   x_chan = x_chan + flow_chan / A_ch_mat(1,x_cells)* dt;                   %calculating new position of fluid front

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%% graphic dispay %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

   % updating fill matrix through mold gap

     for i = Ndiv_Lh + Ndiv_Lw + 1 : Ndiv_Ltot
        for j = 1 : Ndiv_Hc
```

```
            if Xpos(j,i) < Lh + Lw + x_chan
               F(j+4,i) = .75;
            else F(j+4,i) = 0;
            end
         end
      end

   % Updating fill matrix into fabric
      for i = 1 : Ndiv_Lm
         for j = Ndiv_Hc+1 : Ndiv_Hm

            if  Hm - Hc - Ycol(1,i) < Ypos(j,i + Ndiv_Lh + Ndiv_Lw)
               F(j+4,i + Ndiv_Lh + Ndiv_Lw) = .5;
            else  F(j+4,i + Ndiv_Lh + Ndiv_Lw) = .25;
            end

         end
      end

  t = t + dt
end                                                    % end of time step

tmin = round(t/60)
t = round(t)
subplot(3,1,1)
pcolor(F)
title(['Part Dimensions:  ' ,num2str(height),'cm  X  ',num2str(width),'cm  X  ',num2str(length),'cm          time =',num2str(t),'s'])
h = findobj(gca,'Type','surface','EdgeAlpha',1);
set(h,'EdgeAlpha',0.0)
set(gca,'XColor',[1,1,1],'YColor',[1,1,1])
axis ij equal tight

% plot of pressure vs. position
%       for i = 1:x_cells+1                        %creating pressure vs. position graph
%          P_vs_x(i+1,1) = Unk_mat(2*x_cells+1+i,1)*10;
%         x(i+1,1) = Ndiv_Lh + Ndiv_Lw + (i-1);
%       end
%       P_vs_x(1,1) = Papp*10;
%       x(1,1) = 0;
%       x(2,1) = Ndiv_Lh;

%subplot(3,1,2)
%plot(x,P_vs_x);
%axis([0,Ndiv_Lh+Ndiv_Lw+Ndiv_Lm,0,Papp*1.2*10]);
%ylabel('Pressure (kPa)');
%xlabel('x cell number');
%title('Pressure vs. Position')

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%% filling the mold gap and fabric (Stage 1B ) %%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
x_chan = Lm;
x_cells = Ndiv_Lm;                             % takes care of any rounding problems from previous loop
ti2 = (t-ti)/dt;
dt = 1 ;                                       % re-defining time step

while Hf_u_new(1,Ndiv_Lm) > 0
 t = t + dt

         if V_tot > V_inj                      %checking to see if all the resin has been injected
            break
         end

   for i = 1:3*x_cells+2                       %setting initial matrix values to zero
      for j = 1:3*x_cells+2
         Coef_mat( i, j) = 0;
         S_mat(i,1) = 0;
```

```
    end
  end

  %generating solution vector
  S_mat(3*x_cells+1,1) = Papp*K_h/mu;

  for i = 1 : x_cells
       if Hf_u_new(1,i) > 0                                    %checking to see if resin has reached the bottom of the mold
         S_mat(i,1) = A_f * K_f_P(1,i) * P_cap / (mu * Ycol(1,i));
       else
         S_mat(i,1) = 0;                                       %if resin has reached bottom Kf for that cell is zero
       end
  end

%%%%%%%%%%%%%%%%%%%%% generating coefficient matrix %%%%%%%%%%%%%%%%%%%%%

   for d = 1 : x_cells

   Coef_mat(d,d) = 1;

        if Hf_u_new(1,d) > 0                                   %checking to see if resin has reached the bottom of the mold
          Coef_mat(d,2*x_cells + 1+d) = -A_f * K_f_P(1,d) / ( 2 * mu2 * Ycol(1,d));
          Coef_mat(d,2*x_cells + 2+d) = -A_f * K_f_P(1,d) / ( 2 * mu2 * Ycol(1,d));
        else
          Coef_mat(d,2*x_cells + 1+d) = 0;              %if resin has reached bottom Kf for that cell is zero
          Coef_mat(d,2*x_cells + 2+d) = 0;
        end

   Coef_mat(x_cells+d,d) = -1;
   Coef_mat(x_cells+d,x_cells+d) = 1 ;
   Coef_mat(x_cells+d,x_cells+1+d) = -1;

   Coef_mat(2*x_cells+d,x_cells+1+d) = 1;
   Coef_mat(2*x_cells+d,2*x_cells+1+d) = -A_ch_mat(1,d)*K_ch_mat(1,d)/(mu*del_x);
   Coef_mat(2*x_cells+d,2*x_cells+2+d) = A_ch_mat(1,d)*K_ch_mat(1,d)/(mu*del_x);

   Coef_mat(3*x_cells+1 , x_cells+1) = 1;
   Coef_mat(3*x_cells+1 , 2*x_cells+2) = K_h/mu;

   Coef_mat(3*x_cells+2 , 2*x_cells+1) = 1;

   end

  Unk_mat = Coef_mat\S_mat;                                %solving for unknowns

  %now calculate the flow into each column of fabric
  flow_fabric = 0;                                          %initial value

       for i = 1:x_cells
            v_column(1,i) = Unk_mat(i,1)/(A_f*e);       %porosity term added to get actual velocity
            Ycol(1,i) = Ycol(1,i) + v_column(1,i)*dt;
            del_Ycol(1,i) = v_column(1,i)*dt;
       end

%%%%%%%%%%%%%%%%%%%% accounting for fabric compressing %%%%%%%%%%%%%%%%%%%%

       for i = 1:x_cells                                   %updating permeability of each column as function of pressure
         K_f_P(1,i) = K_f(Unk_mat(2*x_cells+1+i));
       end

       Tf_P_old = Tf_P_new;
       Hf_u_old = Hf_u_new;
       vol_add = 0;

       for i = 1: x_cells                                  % thickness fraction matrix

       Tf_P_new(1,i) = Tf(Unk_mat(2*x_cells+1+i));
```

```
                    if Tf_P_new(1,i)>1              % thickness fraction cannot exceed one
                        Tf_P_new(1,i) = 1;
                     else  Tf_P_new(1,i) = Tf_P_new(1,i);
                    end

        Hf_u_new (1,i)= (Hf_u_old(1,i) - del_Ycol(1,i)) *  Tf_P_new(1,i) /  Tf_P_old(1,i) ;

        H_chan(1,i) = Hm -Ycol(1,i) - Hf_u_new(1,i);     %height of channel above fabric

        hyd_dia_mat(1,i) = 2 * H_chan(1,i) * Wm / (H_chan(1,i) +  Wm);            %defining the hydraulic diameter

        K_ch_mat(1,i) = (hyd_dia_mat(1,i)^2)*2/(C) ;                    %permeability of the channel

        A_ch_mat(1,i) = Wm * H_chan(1,i);                % area of channel above column

        delta_Hf = (Hf_u_old(1,i) - del_Ycol(1,i)) - Hf_u_new(1,i);       % calculating the change in fabric height

        vol_add = vol_add + delta_Hf * Wm*del_x;          %calculating the extra volume created
       end

 flow_hose = K_h * Papp / mu;
 t = t + vol_add / flow_hose ;            % accounting for time to fill new volume
  V_tot = V_tot + vol_add;

%%%%%%%%%%%%%%%%%%%% flow through channel %%%%%%%%%%%%%%%%%%%%%%%%%%

   flow_chan = Unk_mat(2*x_cells+1,1);
   flow_h = Unk_mat(x_cells+1,1);
   V_tot = V_tot + flow_h * dt;
   P_1 = Unk_mat(2*x_cells+2,1);
   x_chan = x_chan + flow_chan / A_ch_mat(1,x_cells)* dt;                %calculating new position of fluid front
   v_column;

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%% graphic dispay %%%%%%%%%%%%%%%%%%%%%%%%%%%

   % Updating fill matrix into fabric
      for i = 1 : Ndiv_Lm
         for j = Ndiv_Hc+1 : Ndiv_Hm

            if  Hm - Hc - Ycol(1,i) < Ypos(j,i + Ndiv_Lh + Ndiv_Lw)
               F(j+4,i + Ndiv_Lh + Ndiv_Lw) = .5;
            else  F(j+4,i + Ndiv_Lh + Ndiv_Lw) = .25;
            end

         end
      end

end                                                    % end of time step

tmin = round(t/60)
t = round(t)
subplot(3,1,2)
pcolor(F)
title(['Part Dimensions:  ' ,num2str(height),'cm  X  ',num2str(width),'cm  X  ',num2str(length),'cm            time =',num2str(t),'s'])
h = findobj(gca,'Type','surface','EdgeAlpha',1);
set(h,'EdgeAlpha',0.0)
set(gca,'XColor',[1,1,1],'YColor',[1,1,1])
axis ij equal tight
pause
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%% Apply pressure to the bagging (Stage 2) %%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

while Hf_u_new(1,Ndiv_Lm) > 0
t = t + dt
```

```
      for i = 1 : Ndiv_Lm
        if Hf_u_new(1,i) > 0                              %checking to see if resin has reached the bottom of the mold
           K_F_P(1,i) =  K_f(Papp) ;
        else
           K_F_P(1,i) = 0;                                %if resin has reached bottom Kf for that cell is zero
        end
      end

flow_fab = ((Papp + P_cap) * A_f / mu2) .* (K_F_P ./ Ycol);

      for i = 1:x_cells
            v_column(1,i) = flow_fab(1,i)/(A_f*e);        %porosity term added to get actual velocity
            Ycol(1,i) = Ycol(1,i) + v_column(1,i)*dt;
            del_Ycol(1,i) = v_column(1,i)*dt;
      end

%%%%%%%%%%%%%%%%%% accounting for fabric compressing %%%%%%%%%%%%%%%%%%%%

        Tf_P_old = Tf_P_new;
        Hf_u_old = Hf_u_new;
        vol_add = 0;

 for i = 1: x_cells                                       % thickness fraction matrix

        Tf_P_new(1,i) = Tf(Papp);
                      if Tf_P_new(1,i)>1                 % thickness fraction cannot exceed one
                          Tf_P_new(1,i) = 1;
                       else  Tf_P_new(1,i) = Tf_P_new(1,i);
                      end

        Hf_u_new (1,i)= (Hf_u_old(1,i) - del_Ycol(1,i)) *  Tf_P_new(1,i) /  Tf_P_old(1,i) ;

        delta_Hf = (Hf_u_old(1,i) - del_Ycol(1,i)) - Hf_u_new(1,i);       % calculating the change in fabric height

        vol_add = vol_add + delta_Hf * Wm*del_x;          %calculating the extra volume created

       end

       flow_hose = K_h * Papp / mu;
       t = t + vol_add / flow_hose ;            % accounting for time to fill new volume
       V_tot = V_tot + vol_add;

 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%% graphic dispay %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

   % Updating fill matrix into fabric
      for i = 1 : Ndiv_Lm
        for j = Ndiv_Hc+1 : Ndiv_Hm

          if  Hm - Hc - Ycol(1,i) < Ypos(j,i + Ndiv_Lh + Ndiv_Lw)
             F(j+4,i + Ndiv_Lh + Ndiv_Lw) = .5;
          else  F(j+4,i + Ndiv_Lh + Ndiv_Lw) = .25;
          end

        end
      end


end                                                      % end of time step

% Final fill matrix with bagging against fabric for final plot
      for i = 1 : Ndiv_Lm
        for j = Ndiv_Hc+1 : Ndiv_Hm
            F(j+4,i + Ndiv_Lh + Ndiv_Lw) = .5;
        end
      end
```

```
    for i = Ndiv_Lh + 1 : Ndiv_Ltot
        for j = 1 : Ndiv_Hc
            F(j+4,i) = 0;
        end
    end

%%%%%%%%%%%%%%%%%%%%%%%%%%% post processing %%%%%%%%%%%%%%%%%%%%%%%%%%%
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%

tmin = round(t/60)
t = round(t)
subplot(3,1,3)
pcolor(F)
title(['Part Dimensions:  ' ,num2str(height),'cm  X  ',num2str(width),'cm  X  ',num2str(length),'cm            time =',num2str(t),'s'])
h = findobj(gca,'Type','surface','EdgeAlpha',1);
set(h,'EdgeAlpha',0.0)
set(gca,'XColor',[1,1,1],'YColor',[1,1,1])
axis ij equal tight

t
v_column(1,1);
Ycol(1,1);
V_tot = V_tot*100^3
```

APPENDIX B

HOSE SYSTEM CALCULATIONS FROM MATHCAD

HOSE SYSTEM CALCULATIONS FROM MATHCAD

Hose Calculations(test 1, 8/7/03)

Hose dimensions

$D1a := .0038m$ $D1b := .00635m$ $L1a := .030m$ $L1b := .6096m$

Experimental parameters

$\mu := .337Pa \cdot s$ $t := 112s$ $P_{app} := 20372Pa$ $\rho := 1320\frac{kg}{m^3}$

Determining flow rate

$$v1a := \frac{P_{app}}{32 \cdot \mu \cdot \left(\frac{L1a}{D1a^2} + \frac{D1a^2 \cdot L1b}{D1b^4} \right)} \qquad v1a = 0.252 ms^{-1}$$

$$flow_1 := v1a \cdot \left(\pi \cdot \frac{D1a^2}{4} \right) \qquad flow_1 = 2.86 \times 10^{-6} m^3 s^{-1}$$

Total volume through hose

$Vol_1 := flow_1 \cdot t$

For the side hoses:

Hose dimensions

$D2a := .00389m$ $D2b := .00635m$ $L2a := .04m$ $L2b := .6096m$

Experimental parameters

$\mu := .337Pa \cdot s$ $t := 112s$ $P_{app} := 20372Pa$

Determining flow rate

$$v2a := \frac{P_{app}}{32 \cdot \mu \cdot \left(\frac{L2a}{D2a^2} + \frac{D2a^2 \cdot L2b}{D2b^4} \right)} \qquad v2a = 0.227\,m\,s^{-1}$$

$$P_{minor} := \rho \cdot .9 \cdot \frac{v2a^2}{2}$$

$P_{minor} = 30.646\,Pa$

$$flow_2 := v2a \cdot \left(\pi \cdot \frac{D2a^2}{4} \right) \qquad flow_2 = 2.699 \times 10^{-6}\,m^3\,s^{-1}$$

Total volume through side hoses

$Vol_2 := flow_2 \cdot t \cdot 2$ Since there are two side hoses

Total flow through entire system

$Vol_{tot} := Vol_1 + Vol_2$ $Vol_{tot} = 9.25 \times 10^{-4}\,m^3$

Comparing to experimental value

$$Vol_{exp} := \frac{900}{100^3} \cdot m^3 \qquad error := \frac{Vol_{exp} - Vol_{tot}}{Vol_{exp}} \qquad error = -0.028$$

Calculating and comparing the "permeabilities"

$flow_{tot} := flow_1 + 2flow_2$ $flow_{exp} := \frac{Vol_{exp}}{t}$

$K_h := \frac{flow_{tot} \cdot \mu}{P_{app}}$ $K_{hexp} := \frac{flow_{exp} \cdot \mu}{P_{app}}$

$K_h = 1.366 \times 10^{-10}\,m^3$ $K_{hexp} = 1.329 \times 10^{-10}\,m^3$

APPENDIX C

PERMEABILITY DATA

PERMEABILITY DATA

Ahlostrom uni+mat

pressure (KPa)	Permeability (cm^2)
31.80	6.35E-08
62.47	4.44E-08
97.98	3.48E-08
34.55	6.11E-08
72.13	4.42E-08
99.01	3.72E-08
37.79	4.50E-08
65.23	3.44E-08
97.63	2.63E-08
137.27	2.04E-08
28.35	6.39E-08
69.71	4.40E-08
102.53	3.41E-08
132.93	2.87E-08
31.56	5.89E-08
68.82	3.99E-08
101.49	3.03E-08
137.82	2.27E-08

Glass woven roving

Pressure (KPa)	Permeability (cm^2)
35.50	4.81E-08
70.87	3.38E-08
102.72	2.58E-08
139.67	2.09E-08
37.50	5.63E-08
68.60	4.30E-08
107.41	3.24E-08
29.23	5.19E-08
66.39	3.53E-08
96.17	2.63E-08
134.78	2.07E-08

Hybrid

Pressure (KPa)	Permeability (cm^2)
30.75	1.89E-07
55.57	1.53E-07
95.83	1.28E-07
136.29	1.08E-07

Woven triax carbon all data

Pressure (KPa)	Permeability (cm^2)
30.89	1.58E-07
64.53	1.02E-07
128.92	5.18E-08
203.37	3.11E-08
267.14	2.12E-08
344.70	1.65E-08
36.81	1.45E-07
106.86	5.42E-08
175.80	2.94E-08
245.43	1.89E-08
344.70	1.30E-08

Double bias DB240

Pressure (KPa)	Permeability (cm^2)
25.44	1.76E-07
52.74	1.40E-07
78.45	1.14E-07
107.34	9.55E-08
24.61	1.67E-07
68.94	1.12E-07
113.75	8.37E-08
25.99	1.63E-07
62.80	1.27E-07
94.52	1.07E-07
129.06	9.09E-08

APPENDIX D

COMPACTION DATA

COMPACTION DATA

DB240 three plies

Pressure (kPa)	Ply thickness (mm)	Fiber volume %	Thickness fraction
0.84	1.06	28.98	1.00
1.93	0.97	31.59	1.00
4.70	0.87	35.03	0.90
5.76	0.84	36.53	0.87
7.81	0.82	37.16	0.85
9.72	0.77	39.95	0.79
11.60	0.76	40.52	0.78
13.60	0.71	42.99	0.74
13.60	0.71	43.14	0.73
19.44	0.70	43.92	0.72
29.15	0.69	44.23	0.71
38.87	0.67	45.55	0.69
48.59	0.60	51.20	0.62
71.44	0.59	52.15	0.61

Ahlostrom, 0 plus mat = 42024L/M50, 1250 g/m^2

Pressure (kPa)	Ply thickness (mm)	Fiber volume %	Thickness fraction
0.844463	1.15	43.79	
1.934031	1.0625	47.3921	1
4.700845	1.0425	48.3013	0.981176
5.763796	1.0225	49.24607	0.962353
7.812721	1.02	49.36677	0.96
9.718029	1.0025	50.22854	0.943529
11.60419	0.99	50.86274	0.931765
13.59567	0.975	51.64524	0.917647
13.59646	0.96	52.4522	0.903529
19.43606	0.94	53.5682	0.884706
29.15409	0.92	54.73273	0.865882
38.87211	0.9	55.94901	0.847059
48.59014	0.87	57.87829	0.818824
71.43658	0.8325	60.48542	0.783529

0/90 roving
fiberglast #223 roving, 18 oz/yd^2, balanced weave
two plies

Pressure (kPa)	Ply thickness (mm)	Fiber volume %	Thickness fraction
0.844463	0.7	33.74	1
1.934031	0.6	39.90667	1
4.700845	0.5575	42.94888	0.92916667
5.763796	0.51375	46.60633	0.85625
7.812721	0.50625	47.29679	0.84375
9.718029	0.505	47.41386	0.84166667
11.60419	0.505	47.41386	0.84166667
13.59567	0.505	47.41386	0.84166667
13.59646	0.50125	47.76858	0.83541667
19.43606	0.49	48.86531	0.81666667
29.15409	0.48875	48.99028	0.81458333
38.87211	0.43125	55.52232	0.71875
48.59014	0.415	57.69639	0.69166667
71.43658	0.405	59.12099	0.675

APPENDIX E

INPUT TO MODEL FOR EXPERIMENTAL CORRELATIONS

INPUT TO MODEL FOR EXPERIMENTAL CORRELATIONS

Test 1: Ahlstrom uni+mat fabric

final_cm(1.31E-4,100,7.62, .9525, 13.21, 180, .2, 93, 2.923, .00132,.00003)

permeability of the fabric
K_f = inline('(2.02*10^-10 * P^2 - 6.7*10^-9 * P + 7.82*10^-8)')

ply thickness fraction
Tf = inline('(-.0631*log((P+.001)*10) + 1.073)')

e = .5

Pcap = .4

Test 2: Ahlstrom uni+mat fabric

final_cm(1.31E-4,100,8.89, 1.27, 13.21, 180, .32, 93, 2.90, .00132,.0000335)

permeability of the fabric
K_f = inline('(2.02*10^-10 * P^2 - 6.7*10^-9 * P + 7.82*10^-8)')

ply thickness fraction
Tf = inline('(-.0631*log((P+.001)*10) + 1.073)')

e = .5

Pcap = .4

Test 3: Ahlstrom uni+mat fabric

```
final_cm(4.48E-4,100,7.62, 2.54, 13.08, 152, .59, 91, 3.5, .00132,.0000297)

permeability of the fabric
K_f = inline('(2.02*10^-10 * P^2 - 6.7*10^-9 * P + 7.82*10^-8)')

ply thickness fraction
Tf = inline('(-.0631*log((P+.001)*10) + 1.073)')

Pressure profile
if t <= 26
   Papp = (3.5 - .07*t)*.6894-.3285;
   end
   if t > 26
      if t < 80
      Papp = 1.68*.6894-.3285;
      end
      if t > 80
      Papp = (5.23 + .0137*(t-80))*.6894-.3285;
      end
   end

e = .5

Pcap = .4
```

Test 4: Woven roving fabric

```
final_cm(4.48E-4,100,10.16, 2.54, 13.08, 121, .86, 90, 3.5, .00132,.0000282)

permeability of the fabric
K_f = inline('(2.05*10^-10 * P^2 – 5.8*10^-9 * P + 5.42*10^-8)')

ply thickness fraction
Tf = inline('(1.038*((P+.001)*10)^-.086)')
```

```
Pressure profile
if t <= 45
   Papp = 2.8235-.3285;
   end
    if t > 45
      Papp = 2.8235+.0160*(t-45)-3.285;
    end
      if t >= 76
         if t < 92
         Papp = 1.0000-.3285;
         else
         Papp = 3.9000+.0032*(t-92)-.3285;
         end
      end


V_inj = 2200 cm^3

e = .55

Pcap = .4
```