Prediction of electric heating load component of distribution feeder loads using statistical modeling
by Vijay Singh

A thesis submitted in partial fulfillment of the requirements for the degree of Master of Science in Electrical Engineering
Montana State University

Abstract:
A statistical model has been developed to represent the thermodynamic behavior of buildings. The model uses an analogous electric circuit to represent the thermodynamic characteristics of each building. The building model parameters are gaussian distributed, each with a specific mean and standard deviation. A computer program has been written which uses this model to predict the heating load component of the distribution load via simulation. The program can predict the feeder electric heating load demand under continuous power supply as well as after a power outage. It is specifically useful for predicting the feeder cold load pickup currents on cold winter days. The program has several features including allowing for changes in the ambient temperature during the outage and changes in the service voltage. Simulation results are presented and some experiments towards validating the computer program are 'included.

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APPROVAL

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Vijay Singh

This thesis has been read by each member of the thesis committee and has been found to be satisfactory regarding content, English usage, format, citations, bibliographic style, and consistency, and is ready for submission to the College of Graduate Studies.

8/24/92 — Date

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8-24-92 — Date

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8/31/92 — Date

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ABSTRACT

A statistical model has been developed to represent the thermodynamic behavior of buildings. The model uses an analogous electric circuit to represent the thermodynamic characteristics of each building. The building model parameters are gaussian distributed, each with a specific mean and standard deviation. A computer program has been written which uses this model to predict the heating load component of the distribution load via simulation. The program can predict the feeder electric heating load demand under continuous power supply as well as after a power outage. It is specifically useful for predicting the feeder cold load pickup currents on cold winter days. The program has several features including allowing for changes in the ambient temperature during the outage and changes in the service voltage. Simulation results are presented and some experiments towards validating the computer program are included.

CHAPTER 1

INTRODUCTION

Restoring power to a circuit after a power outage during cold winter days which is commonly called Cold Load Pickup can result in feeder over currents, which may cause circuit breaker tripping. This is because in cold days a large number of buildings will demand heating power at the same time after the outage, thus making the load undiversified and causing excess currents to flow. It is therefore of interest to predict the magnitude and duration of the overload following an outage.

According to Audlin and Pratt [1] there are four separate time phases of the increased restoral pickup demand on any feeder after an outage.

1) The first phase provides inrush current to cold lamp filaments and to the distribution transformers.
2) The second phase lasts for about 1 second or less and provides the motor starting current.
3) The third phase lasts for about 15 seconds and provides the motor acceleration currents.
4) The fourth phase can last for several hours and is due to an abnormal number of appliances energized. These appliances are mostly the heating furnaces.

The solution to the first three phases is relays with extremely inverse settings.

This thesis makes an analysis of the fourth phase current, which is the heating current during cold ambient temperatures. The duration for which this fourth phase current or the Cold Load Pickup current lasts is dependent on the following factors:

1) Ambient temperature;
2) Length of outage;
3) Number of customers on the feeder;
4) Number and type of connected load like washing machines etc.;
5) Thermal parameters of the affected houses;
6) Type of housing (bungalow, apartment, etc.);
7) Water heater size, set point, consumption, etc.

Analysis of the power required for heating is not a simple problem. It is required to model the thermodynamics of a house and the behavior of the thermostat. House thermodynamics is modeled by using an R-C network connected by a switch to a current source Q. The resistor R represents the house insulation level. The capacitor C represents the thermal mass of the house. The current source represents the heat input from the furnace. The switch is controlled by a thermostat, the setting of which is manually adjustable. When the switch is open the charged capacitor provides the current to the resistor. Charge across the capacitor is analogous to the house temperature and so the discharge of the capacitor would mean cooling of the house.

The parameters which determine the current requirement of a house are the resistor R, the capacitor C, the current source Q and the thermostat setting. To model a large number of unique houses a random number generator is used to select the values of the parameters. A specific mean value is specified for each of these parameters and noise is added to it. The noise is a random number with gaussian distribution, mean of zero, and a specific standard deviation.

If the utility does not have an idea of the value of the Cold Load Pickup current the usual way to overcome the unsuccessful reclosure of the circuit breaker would be to disarm protective relays. There are two drawbacks to this.

1) The relay may allow the fault current to flow along with the Cold Load Pickup current.
2) If the disarmed relay is left in place even after the Cold Load Pickup is completed, it could be a severe danger to the protective system.

This thesis recommends two different ways to restore the electrical service successfully.

1) After an estimate of the Cold Load Pickup the relays can be disarmed to an extent to allow the Cold Load Pickup current and not the fault current.
2) Reducing the Cold Load Pickup current by means of feeder sectionalizing. A simulation program has been developed that provides the option of automatic sectionalizing and manual sectionalizing. In

automatic sectionalizing the computer program calculates the time when there is minimum current flowing through the feeder. It then simulates further as if the next load has been connected. In manual sectionalizing the operator has to enter the time for the next section of load to be connected.

The computer program has the provision of simulating for:

1) Change of ambient temperature during and after power outage;
2) Step change in voltage at which power is supplied.

Since the utilities are reluctant to intentionally disrupt electric service, not much validation of the cold load pickup current has been done. In this thesis data was collected from three different experiments towards the validation of the model.

Content of this thesis is contained within seven chapters described below.

Chapter 1 is a general introduction to the Cold Load Pickup problem.

Chapter 2 discusses the work done in the field of Cold Load Pickup so far.

Chapter 3 deals with the thermodynamic model of a house.

Chapter 4 deals with the aggregate load demand of the feeder.

Chapter 5 deals with the simulated results.

Chapter 6 deals with the results of the experiment performed to validate Cold Load Pickup model.

Chapter 7 is the summery and conclusions of the study of Cold Load Pickup. Also suggestions for further research are presented.

CHAPTER 2

COLD LOAD PICKUP LITERATURE REVIEW

An analysis of the overload after a power outage is important for the utilities in order to prevent damage to their equipment. It is required to efficiently model the thermal characteristics of the house on the feeder in order to determine the magnitude and duration of this overload. In this chapter literature pertaining to Cold Load Pickup current and thermodynamics of a house is reviewed.

Survey

In 1949 Audlin et al. [1] performed a 15 minute outage on a feeder serving 3500 customers. Four time phases of the Pickup current was recognized. McDonald and Bruning [2] did experimentation to determine the value of the parameters of a house. House temperature was monitored for 24 hours. The conductance was determined by the steady state test which requires the house temperature to remain constant over a certain period of time. The heat input to the house, the house temperature and the ambient temperature need to be recorded to determine the conductance of the house. The time constant which is the product of the thermal resistance and the thermal mass is determined by a cool down test. In this test power is shut off for a certain period of time. The temperature of the house after the test period, the initial temperature of the house and the outside temperature are required for the calculation of the time constant. The thermal mass of the house is then calculated by multiplying the conductance to the time constant. He then comes up with the average and standard deviation values of the parameters by conducting the individual tests in six electrically heated homes. His results include showing the average steady state power demand per house at different ambient temperatures and the effect of change in ambient temperature on the Cold Load Pickup demand and the duration of its peak.

Ihara and Schweppe [3] developed a thermodynamic model for a house and derived the equation for house on-time (T_{on}) and house off-time (T_{off}). They point out that the heater is either on with a probability $T_{on}/(T_{on}+T_{off})$ or off with a probability $T_{off}/(T_{on}+T_{off})$. An experiment was conducted to verify the results. House temperature was monitored for 80 and 140 minutes. Model and test results have been compared. The effect of change in ambient temperature, change in outage duration and change in the standard deviation of the thermal parameters of the house on the aggregate power demand is shown.

Lang and Anderson come up with the following values, for the model parameters of a house [4].

Thermal Conductance = .318 kw/°C (.177 kw/°F)

Thermal Mass = 3.21 kwh/°C (1.783 kwh/°F)

Reference [5] models an R-C circuit and derives the equation for house on-time and house off-time. Random numbers are generated for the five parameters which affect the current demand of the house. The effect of change in furnace size, ambient temperature, outage duration and service voltage on the Cold Load Pickup current is shown.

Mortensen and Haggerty [6] modeled an R-C circuit using the same basic equation as Ihara and Schweppe [3]. Time is discretized by using a sampling period h. It is assumed that the thermostat always switches exactly at a sampling instant. An equation to find the temperature of a house after each sampling interval is developed. A discrete white noise term was added to the equation to include the effect of the random influences in the environment.

Mortensen [7] has discussed five models to estimate heating and cooling loads. The models are:

1) Deterministic differential equation;
2) Stochastic difference equation;
3) Markov Chain matrix equation;
4) Hybrid partial differential equation;
5) Alternating renewal process.

According to N.W.P.P.C. [8] the following are the typical values for the house parameters in the northwest United States.

Thermal Mass = 3223.0 wh/°F

Thermal conductance = 180 w/°F

Overview

Little work has been done towards validating the results of Cold Load Pickup current. Also the difference in the Cold Load Pickup current due to the type of construction of the houses has not been recognized.

This thesis uses the actual values of the house parameters best suited for the northwest United States. Three different experiments were performed towards validation of the Cold Load Pickup model.

CHAPTER 3

MODELING

A house model has been represented in the past by a multi node network. Lang and Anderson [4] have represented the thermodynamic model of a house by the following circuit.

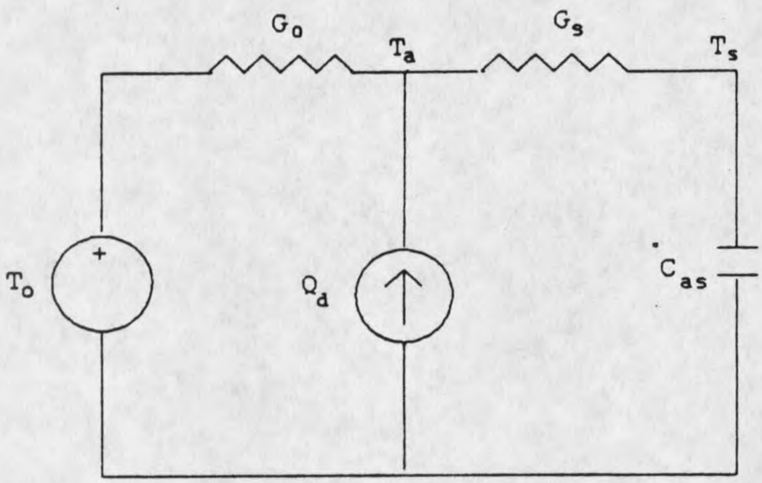

Fig. 1 Heated building electrical equivalent.

Where

T_a is the temperature of the living space air (°C)

T_s is the temperature of the equivalent thermal mass (°C)

T_o is the outdoor temperature (°C)

C_{as} is the equivalent thermal mass representing the entire building (kwh/°C)

G_s is the thermal conductance between the living space and the equivalent thermal mass (kw/°C)

G_o is the thermal conductance between the living space and the outdoors (kw/°C)

Q_d is the total heat injected into the living space (kw)

According to Mortensen and Haggerty [7] only one or two sections are required due to the forgiving nature of highly aggregated configuration. The load on a power system is the aggregation over hundreds or thousands of houses, such that the individual details largely washout, and only consistent trends remain. Most of our references have used a simple RC circuit. Our model of the RC circuit is as follows.

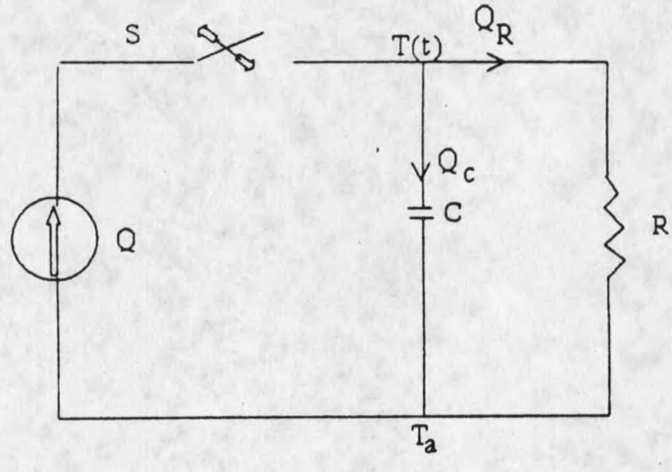

Fig. 2 Analogous electric circuit used for thermodynamic behavior of a house.

In the model

T is the house temperature (°F)

T_a is the ambient temperature (°F)

C is the equivalent thermal mass of the house (kwh/°F)

R is the equivalent thermal resistance of the house (°F/kw)

G is the equivalent thermal conductance of the house (kw/°F)

Q is the total heat injected into the house (kw)

Q_C is the heat flowing into the thermal mass C of the house (kw)

Q_R is the heat loss to the outside environment (kw)

$$Q = Q_C + Q_R$$

The thermal quantities used in this model are analogous to electrical quantities as follows.

Thermal Quantity	Electrical Quantity
Temperature	Voltage
Heat Flow	Current
Thermal Conductance	Electrical Conductance
Thermal Mass	Electrical Capacitance
Time	Time

According to N.W.P.P.C. [8] the following are typical values of the house parameters in the northwest United States.

Thermal Mass C = 3223 wh/°F

Thermal Conductance G = 180 °F/w

A value of heat injected Q = 20.5 kw was found likely in this region.

This thesis uses the above defined value for all plots unless otherwise stated.

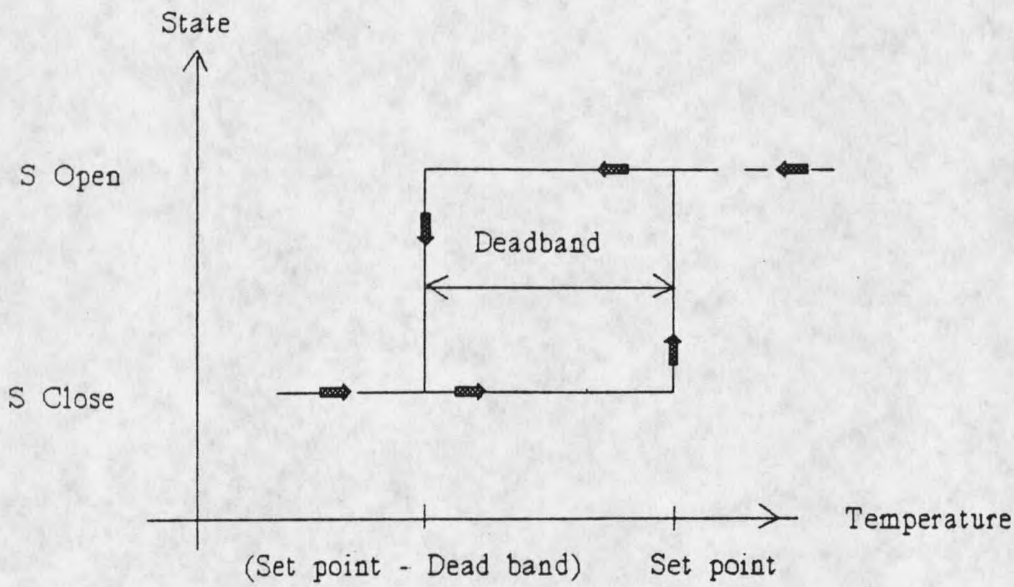

Fig. 3 Hysteresis loop of a thermostat.

Fig. 3 shows the hysteresis characteristics of the thermostat to which the switch S is connected. The upper setting of the thermostat is the setpoint and the lower setting is the setpoint minus the dead band. The switch S closes when the house temperature drops below the lower thermostat setting and opens when the house temperature reaches the upper setting.

It is assumed in this thesis that during power outage people do not add heat to their houses by any other source like wood burning or any gas heating appliance. Also the effect of solar heat is not considered. The following range of values of the thermostat were found most likely.

Set point = 67-70 °F

Dead band = 2 °F

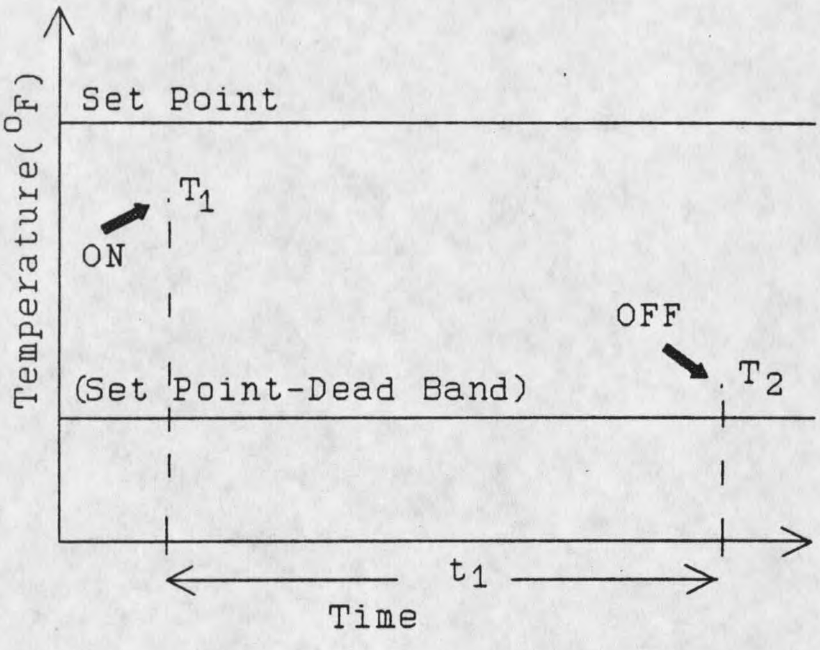

Fig. 4 House ON/OFF state before and after a power outage.

In Fig. 4 house A has a room temperature of T_1 and it is in the on state. There is a power outage for time t_1 after which power is restored. During this time t_1 the house has cooled to a temperature T_2. Since the house temperature is above the lower setting of the thermostat it will be in the cooling state. The house will be switched on once its temperature drops below the lower setting of the thermostat. It is for this reason that for short outages power demand at the instant of power restoration is less than the power demand a short time after power restoration.

From the equivalent circuit of a house given in Fig. 2 the temperature T of a house at any time t is given by the following equation. See Appendix A for details.

$$T(t) = Ta + (T_{ho} - T_a) e^{-t/RC} + wQR (1 - e^{-t/RC}) \qquad (M-1)$$

where

T_{ho} is the initial house temperature

T_a is the ambient temperature

$w = 1$ when S is closed or

$w = 0$ when S is open

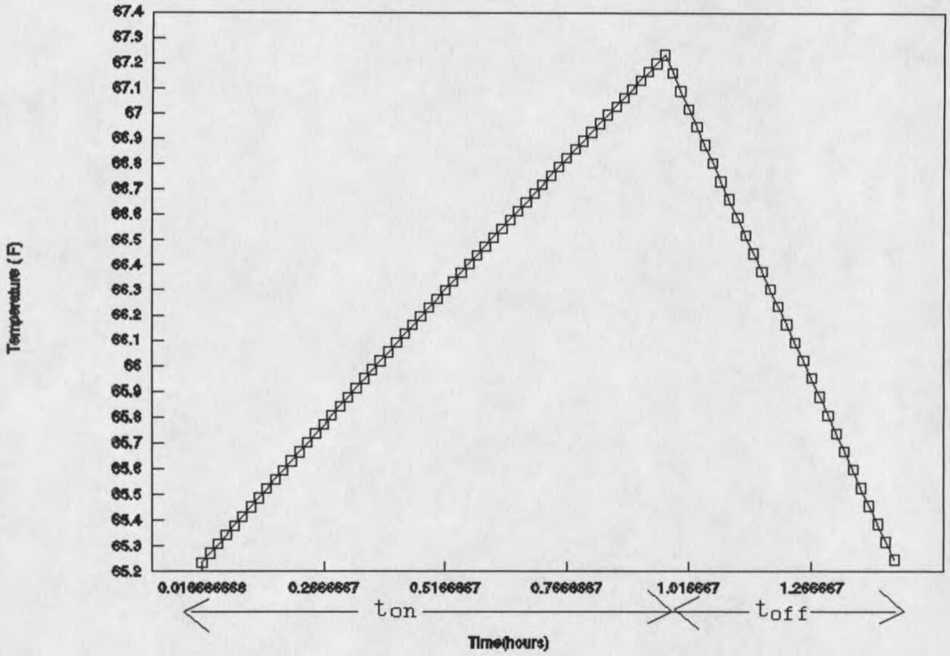

Fig. 5 Variation of house temperature under normal conditions at ambient temperature of -10°F.

Fig. 5 shows the variation of house temperature during one cycle of thermostat operation under normal conditions. It has been obtained using equation M-1. The time interval during which the house temperature rises from the lower thermostat setting to the upper thermostat setting is the on-time of the house. It is denoted by $T_{on.}$ The time interval during which the house temperature falls from the upper setting to the lower setting is called the off-time of the house. It is denoted by T_{off}. It is shown in Appendix A that:

$$T_{on}=-RC\ln\frac{setpoint-T_a-QR}{setpoint-deadband-T_a-QR} \tag{M-2}$$

$$T_{off}=-RC\ln\frac{setpoint-deadband-T_a}{setpoint-T_a} \tag{M-3}$$

The on-time and off-time at ambient temperature of -10°F calculated from the above equations are .95 hours and .47 hours. These values match with those found from Fig. 5.

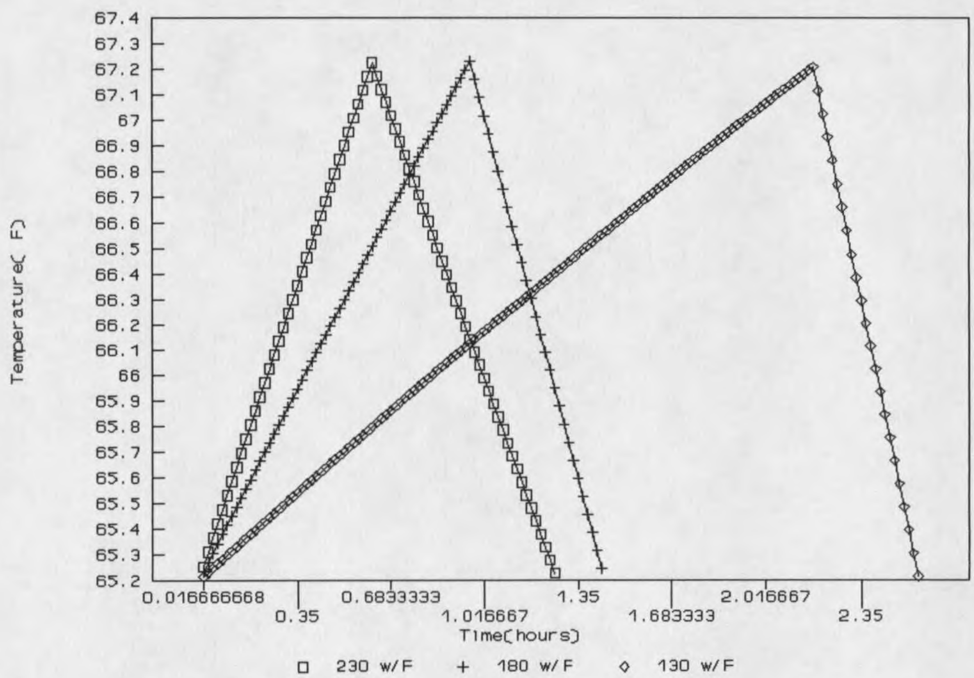

Fig. 6 Effect of thermal conductance on the temperature variation of the house.

Fig. 6 shows the effect of thermal conductance at ambient temperature -10°F. As Thermal Conductance increases, Q_R

increases. Since Q is constant and is the sum of Q_R and Q_C, an increase in Q_R would mean a decrease in Q_C. Q_C is the current responsible for heating the thermal mass of the house. Due to decrease in Q_C the time taken to heat the house increases meaning that T_{on} increases. An increase in Q_R would mean more heat is lost to the environment, meaning that the house will cool down faster.

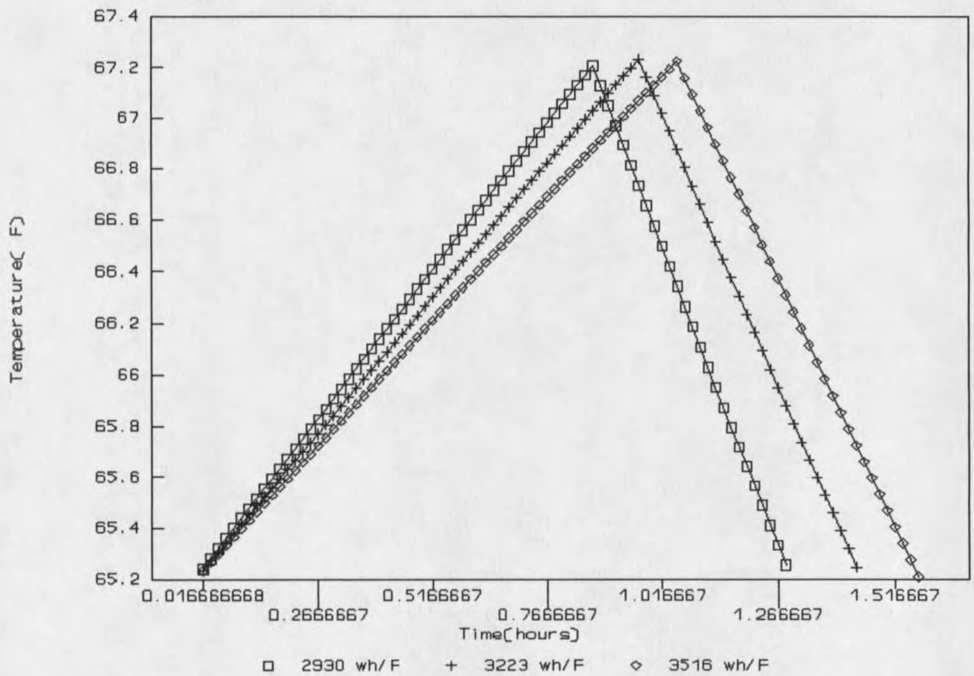

Fig. 7 Effect of change in thermal mass on the temperature variation of the house.

Fig. 7 shows the effect of Thermal Mass at ambient temperature of -10°F. Equations (M-2) and (M-3) show that on-time and off-time are directly proportional to the thermal mass of the house. An increase in thermal mass would mean an increase in both on-time and off-time.

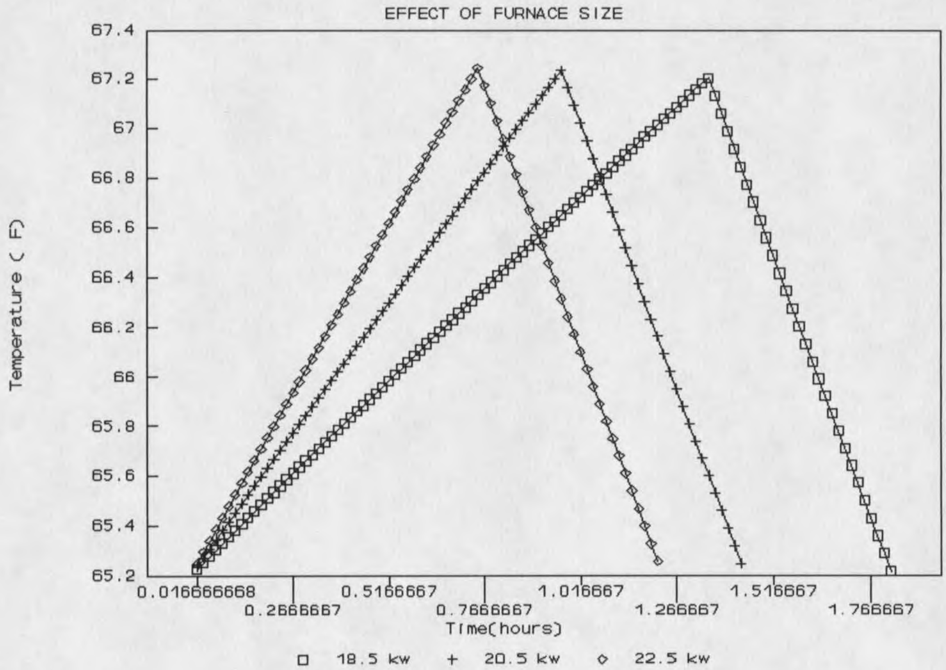

Fig. 8 Effect of change in furnace size on the temperature variation of the house.

Fig. 8 shows the effect of furnace size at ambient temperature of -10°F. An increase in furnace size would mean more heat is being supplied to the house and so the thermostat on-time will decrease. The off-time remains the same irrespective of the furnace size as during this time the furnace is off. Note that equation (M-3) which shows the house thermostat off-time does not contain the term Q.

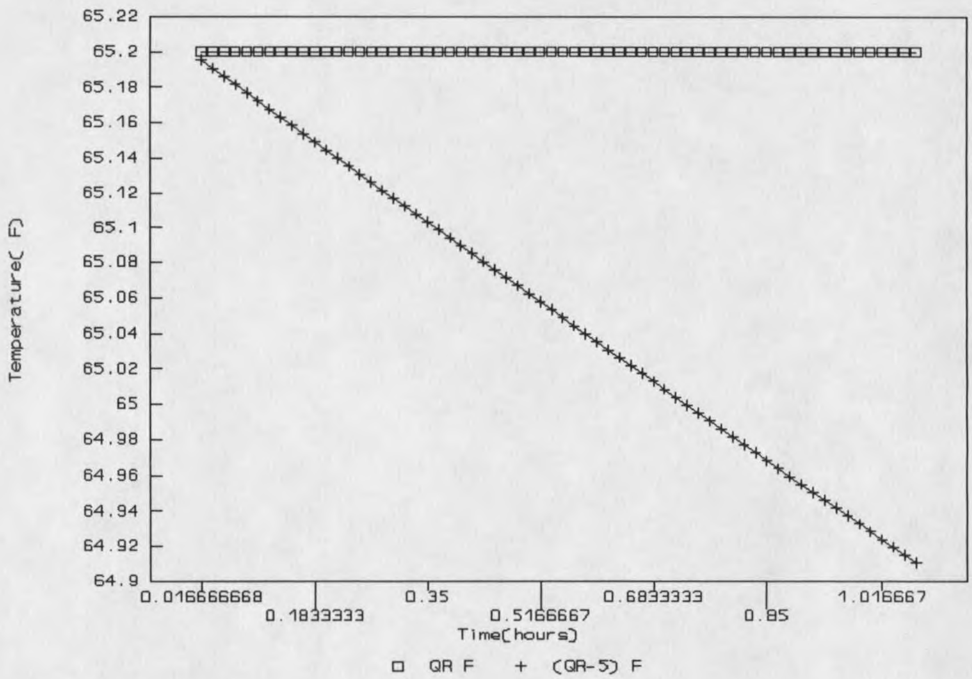

Fig. 9 Variation of house temperature under very cold ambient temperatures.

According to Mortensen and Haggerty [6] when a house furnace is unable to heat the house, the difference in house temperature and ambient temperature is called the temperature gain of the heater. It is denoted by T_g. This is because all the heat input is lost to the environment and does not add to the house temperature. In other words Q_c is zero. Therefore,

$$Q = Q_R + Q_C = Q_R$$

From our model temperature T of the house is given by

$$T = Q_R R + T_a$$

$$= QR + T_a$$

$$T_g = QR = T - T_a$$

$$T_a = T - QR \qquad \text{(M-4)}$$

Substituting the above value of ambient temperature T_a in (M-1)

$$T(t) = T\text{-}QR + (T_{ho} - (T - QR))\ e^{-t/RC} + wQR\ (1 - e^{-t/RC})$$

$$= T_{ho} \qquad \text{(M-5)}$$

Equation (M-5) shows that the house temperature T at any time t remains equal to the initial temperature when ambient temperature is given by (M-4). Therefore line with square symbols in Fig. 9 shows the house temperature does not rise even though the furnace is on. The house temperature falls even though the furnace is on when the difference in the house temperature and ambient temperature is more than T_g. This is shown by the line with plus symbols in Fig. 9.

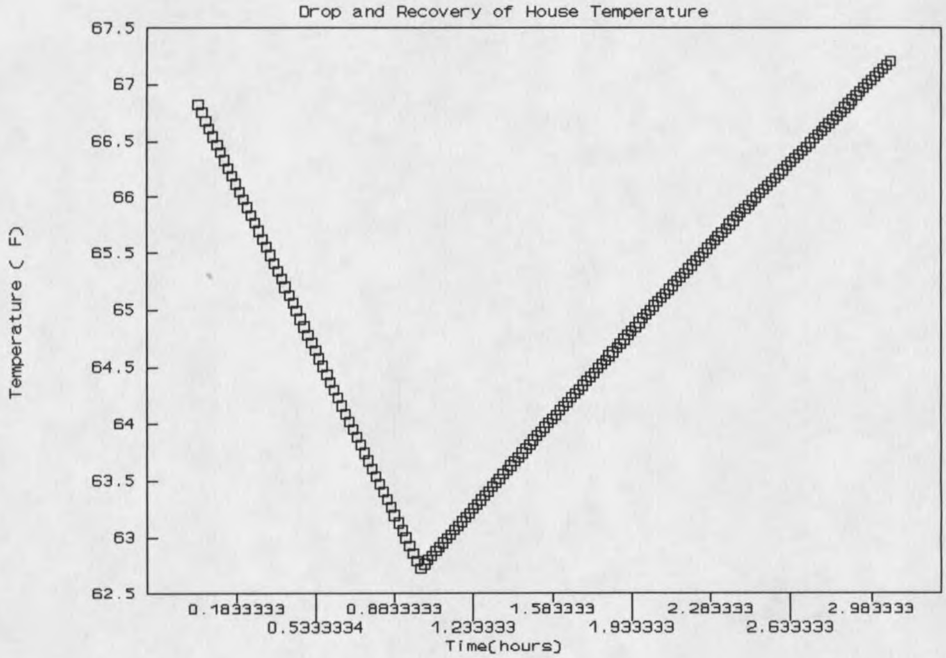

Fig. 10 Drop and recovery of house temperature at ambient temperature of -10°F.

In Fig. 10 the house temperature falls due to a power outage of one hour at ambient temperature of -10°F. The initial temperature of the house was under steady state conditions and so it has to be within the thermostat settings. It was generated using a random number within the thermostat setting. After the power is restored the house temperature recovers. Note that the time for which the house temperature recovers is the T_{on} of the house under conditions of outage. Also the time of the temperature drop is the T_{off} of the house under conditions of outage.

CHAPTER 4

AGGREGATION

This chapter deals with the determination of the total heating current supplied by a feeder. The current requirement of a house is dependent on the following.

1) Ambient Temperature (T_a)
2) Thermal Conductance (G)
3) Thermal Mass (C)
4) Capacity of the furnace (Q)
5) Thermostat set point (setpoint)
6) Thermostat dead band (deadband)

No two houses are the same. Thermal mass, thermal conductance and capacity of the furnace of each house depends on its construction and size. Since the thermostat is manually operated different people adjust it to a different setting depending on their lifestyle.

Due to the above reasons a different value has to be provided for the above parameters for each house. The simulation program adds noise to the specified mean of each parameter. This noise is a random number with a gaussian distribution, mean of zero, and a specified standard deviation. The on-time and off-time of each house depend on these parameters and so a different on-time and off-time is assigned to each house. In the simulation program these on-times and off-times are used to make the estimation of the current requirement.

Current demand of a feeder I_T is given by:

$$I_T = \Sigma I_i$$

where I_i is the current demand of each house on the feeder. The current I_i of each house could be either zero or have a certain value. According to Ihara and Schweppe [3] the probability that the current is not zero is given by

$$D = \frac{T_{on}}{T_{on} + T_{off}}$$

where D is called the duty cycle
Depending on the values of the parameters, D can take a value anywhere between 1 and 0.

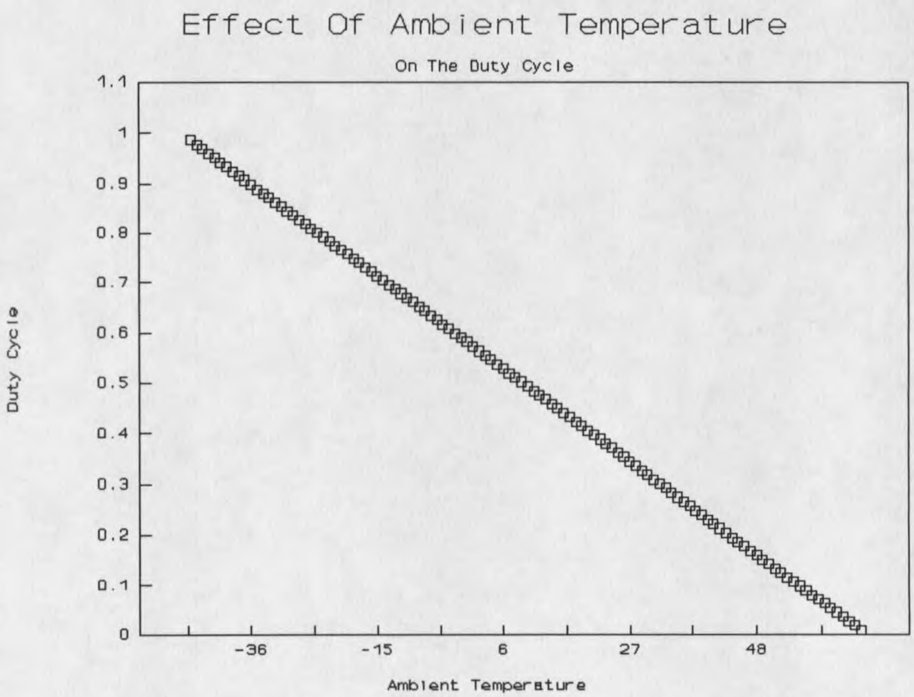

Fig. 11 Effect of ambient temperature on the duty cycle.

Duty cycle takes a value of 0 at ambient temperature of 65.2 °F. Duty cycle becomes 0 when the lower setting of the thermostat is less than the ambient temperature. Duty cycle becomes 1 when the house temperature is equal to or greater than $T_g + T_a$. Where $T_g = QR$ and is called the temperature gain of the heater. See chapter 3 for a complete description.

Algorithm for Sectionalizing

Sectionalizing means to restore power to different sections of a feeder at different times in order to minimize the increased restoral current. Fig. 12 shows power source S supplying power to a feeder. The feeder has two breakers, B1 and B2. Closure of B1 would mean that power is restored to upstream feeder which is the part of the feeder between B1 and B2. Closure of B2 after B1 has been closed would mean power is restored to the entire feeder.

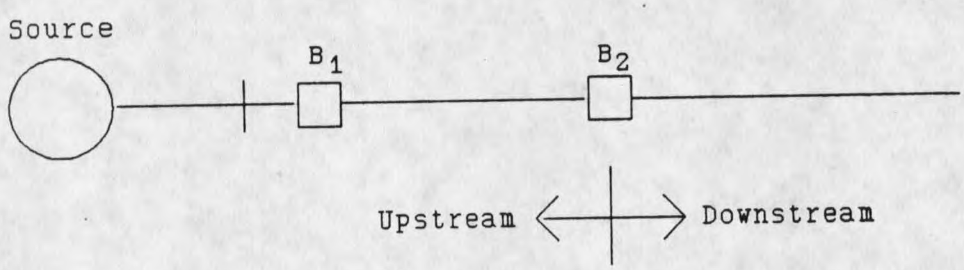

Fig. 12 Sectionalized feeder.

In Fig. 12 for sectionalizing, after a power outage, power is restored on upstream portion of the feeder. The time of peak current requirement is allowed to pass after which power is restored to the downstream feeder. In order to decide the time of restoration of the downstream feeder it is required to know the percentage of electric space heating load on it. Note that the time of outage for the downstream feeder would be the time of normal outage plus extra time for which power was restored on the upstream feeder but not on the downstream feeder.

The simulation program has the provision of automatic sectionalizing as well as manual sectionalizing. In automatic sectionalizing the computer program makes simulations as if the downstream feeder was connected when the current on the upstream feeder is at its minimum. Fig. 13 shows that 64 minutes after power is restored the current is at its minimum so this is the time when the downstream feeder is connected. In manual sectionalizing the time of the closure of breaker B2 is decided by the operator.

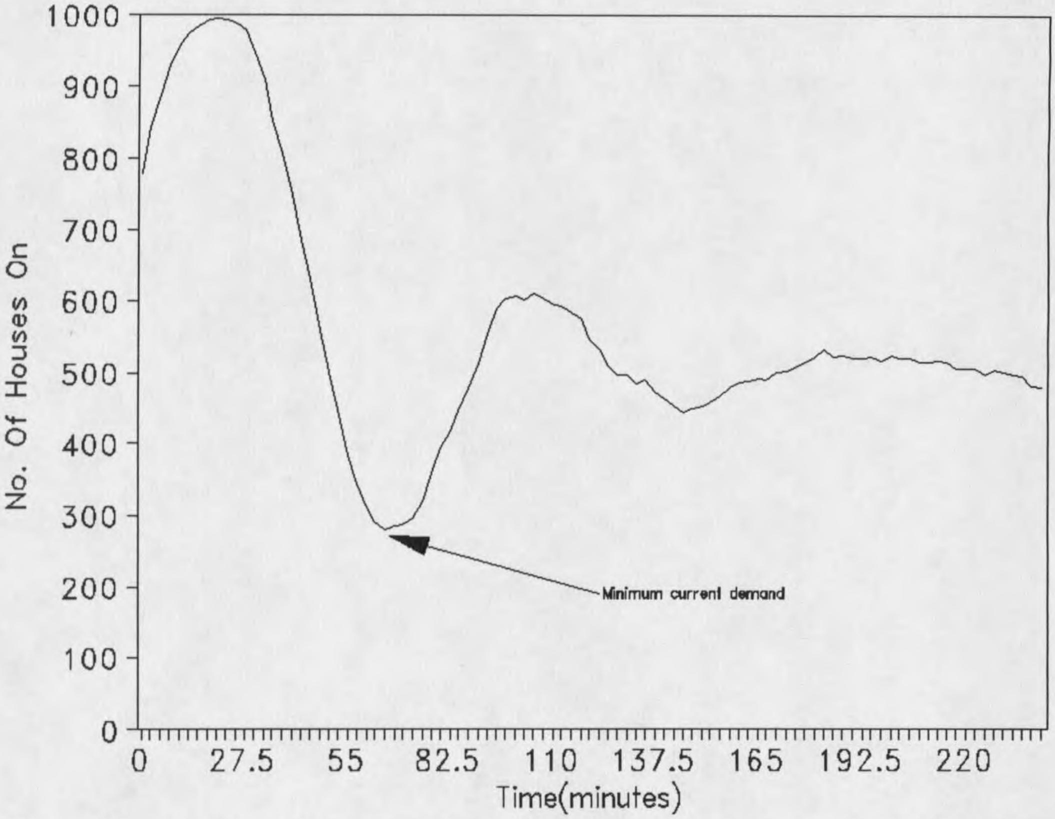

Fig. 13 Shows the number of houses demanding power at ambient temperature of 10°F and after a power outage of 30 minutes.

Algorithm for Change in Voltage

This thesis discusses the effect of change in voltage on the electrical power being supplied to a feeder under steady state conditions and when power is restored after an outage.

Q the current source of the R-C circuit is measured in kw and is the term for the electrical power supplied to the furnace. The power P is given by

$$P = \frac{V^2}{R}$$

If there is a change in voltage the new power will be given

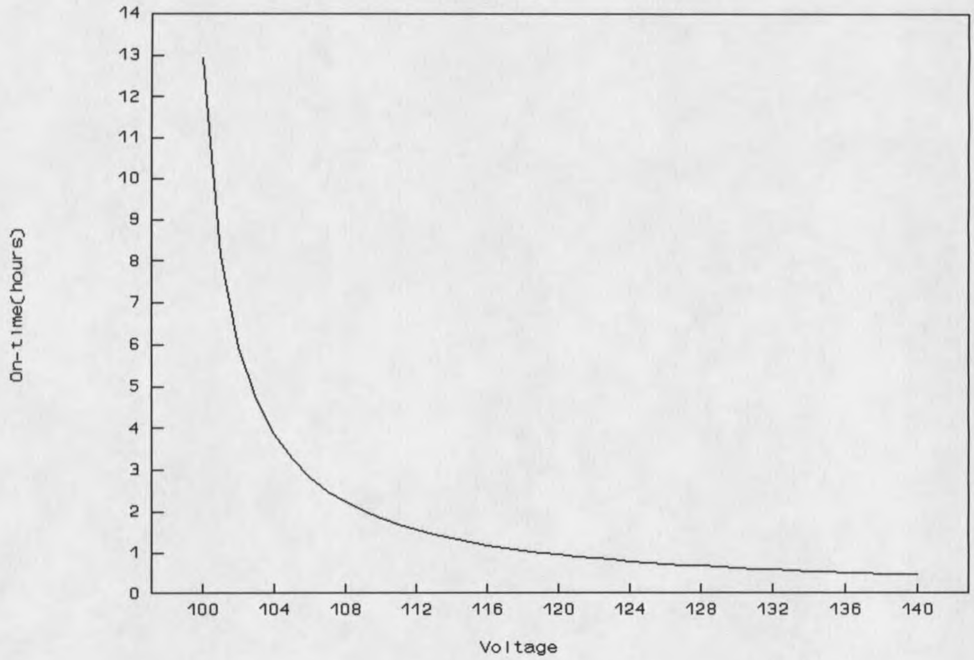

Fig. 14 Effect of voltage on the on-time of the furnace at ambient temperature of -10°F.

by

$$P_{new}=\frac{V_{new}^2 * P_{old}}{V_{old}^2}$$

From Appendix A, the on-time and off-time are given by

$$T_{on} = -RC \ln \frac{(\text{setpoint}-T_a-QR)}{(\text{setpoint}-\text{deadband}-T_a-QR)}$$

$$T_{off} = -RC \ln \frac{(\text{setpoint}-\text{deadband}-T_a)}{(\text{setpoint}-T_a)}$$

Inspection of the above equations show that on-time is dependent on the power where as off-time is not. Fig. 14 shows that an increase in voltage decreases the house on-time and vice versa. This means that a change of voltage affects the rate at which the houses get heated.

If power is restored after an outage, an increase in voltage will have the effect of increase in the demand for power on the feeder. Under steady state conditions houses require a fixed amount of electrical energy to compensate for the heat lost to the environment. This means that the power demand does not change with a change in voltage under steady state conditions. However, the current demand decreases with increase in voltage since the power remains constant.

Algorithm for Change in Temperature

There is a possibility that the ambient temperature might change during the outage or after the outage. Inspection of equations for on-time and off-time show that both are dependent on the ambient temperature. Fig. 15 shows that with a decrease in ambient temperature on-time increases whereas off-time decreases.

The simulation program has the provision of changing the temperature twice. This is explained with the help of Fig. 16 as follows:

1) At time=0 ambient temperature is T_1 and there is a power outage.
2) At time t_1 ambient temperature changes to T_2.
3) At time t_2 power is restored.

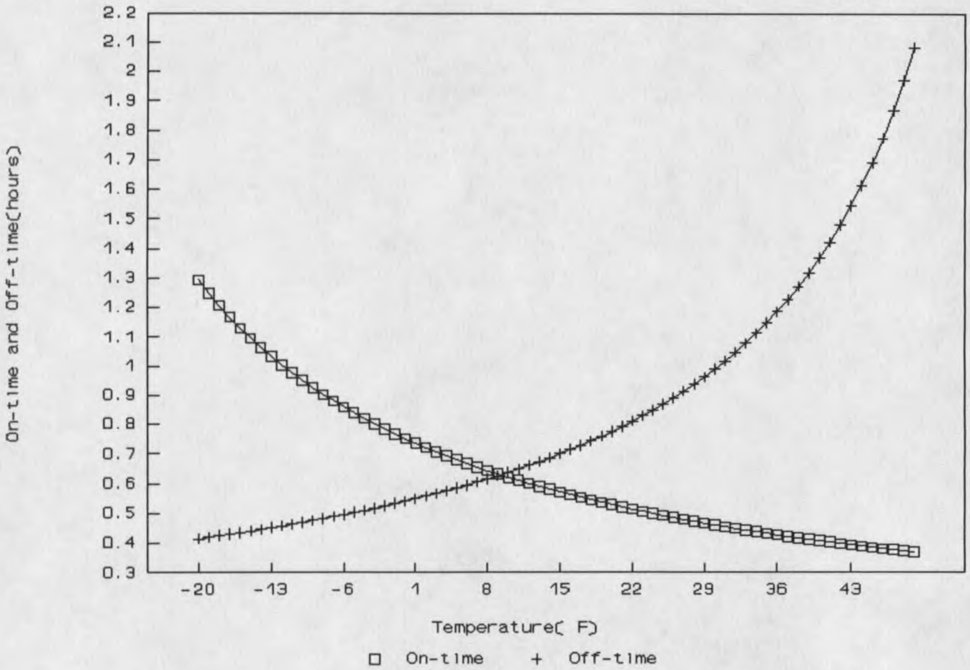

Fig. 15 Effect of ambient temperature on the on-time and the off-time of the furnace.

4) At time t_3 ambient temperature changes to T_3.

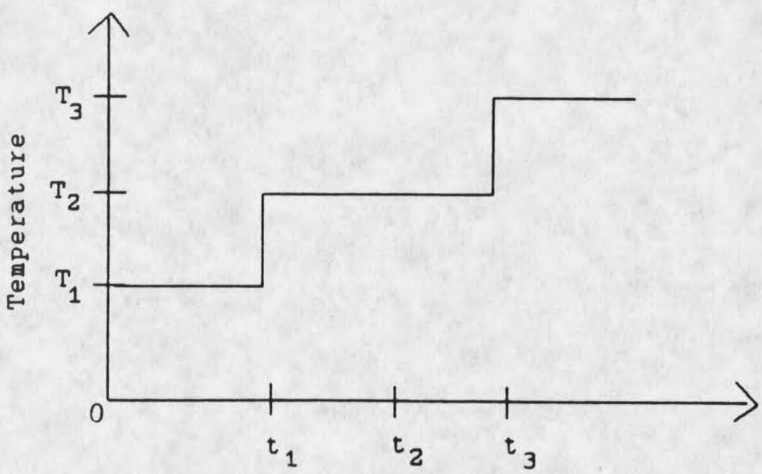

Fig. 16 Change in ambient temperature during the simulation period.

The value of the three ambient temperatures T_1, T_2, T_3 and the time t_1, t_2, t_3 is entered by the operator. Each time the ambient temperature is changed, the old value of the ambient temperature is replaced by the new value in the equation for on-time and off-time. All further simulations are made with the new values of on-time and off-time.

CHAPTER 5

RESULTS

In this thesis all simulations were done for 1000 houses. Random numbers with a specific mean and standard deviation were generated for the following five parameters of the house equivalent electrical model through which the current demand of each house can be determined.

1) Thermal Conductance (G)
2) Thermal Mass (C)
3) Heat Injected to the house (Q)
4) Thermostat Set Point
5) Thermostat Dead Band

Each house on the feeder is randomly assigned a value for the above parameters. The values assigned have a gaussian distribution with specific mean and standard deviation. Listed below are the mean values as well as the standard deviation of the parameters.

Mean G=180.0 w/°F	G Standard Deviation=10%
Mean C=3223.0 wh/°F	C Standard Deviation=16%
Mean Q=20.5 kw	Q Standard Deviation=12%
Mean Set point=67.2°F	Set point Standard Deviation=2%
Mean Dead band=2°F	Dead Band Standard Deviation=3%

The mean values of G and C were estimated based on N.W.P.P.C. report [8]. The mean value of Q, set point and deadband was found most likely. It is assumed that the thermodynamic parameters are statistically independent meaning that the generated values of one parameter are not dependent on values of other parameters.

It is assumed that the random numbers generated are statistically independent meaning that they are not biased. If this is true then the number of houses demanding power are:

$$\frac{T_{on}}{T_{on} + T_{off}} * \text{No. of houses on the feeder}$$

Fig. 17 shows the number of houses demanding power under steady state. The line for Lang uses the value of G and C obtained from Lang and Anderson [4], and the line for N.W.P.P uses the value of G and C obtained from N.W.P.P.C. [8]. The values obtained from Lang and Anderson [4] are C=1783.8 wh/°F and G=176.6 w/°F.

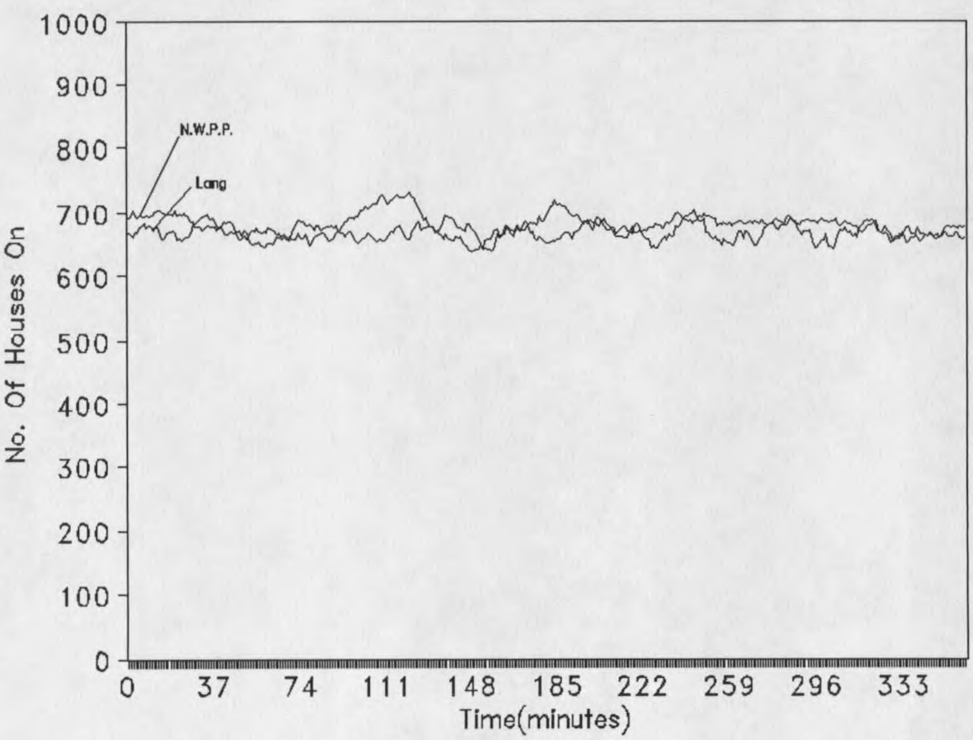

Fig. 17 Steady state response at ambient temperature of -10°F.

The average number of houses demanding power in Fig. 17 are;

669.8 for Lang and Anderson [4]

681.7 for N.W.P.P.C.[8]

The average number of houses demanding power calculated by substituting the values of the parameters in the equation for on-time and off-time are:

For Lang and Anderson [4]:

The on-time and off-time is calculated using equation (M-2) and (M-3)

$$T_{on} = .51 \text{ Hr}$$

$$T_{off} = .26 \text{ Hr}$$

Average number of houses demanding power

$$= \frac{T_{on}}{T_{on}+T_{off}} * 1000 = 662.33$$

Error= 1.1%

For N.W.P.P.C. [8]:

The on-time and off-time is calculated using equation (M-2) and (M-3)

$$T_{on} = .95 \text{ Hours}$$

$$T_{off} = .47 \text{ Hours}$$

Average no. of houses demanding power

$$= \frac{T_{on}}{T_{on} + T_{off}} * 1000 = 669.01$$

Error= 1.9%

The above results prove that the random numbers generated are statistically balanced.

In Fig. 17 the steady state values are close in the two cases where as house on-time and off-time is not. This is because the value of thermal conductance in the two cases is close where as thermal mass is not.

<u>Effect of Change in Thermodynamic Parameters</u>

In order to see the effect of change in parameters on the power demand, this thesis changes the mean value of each of the parameters and discusses the results. The standard deviation in percentage of mean value is kept constant.

Decreasing the value of thermal conductance G means that there is extra insulation. This conserves heat energy. Since

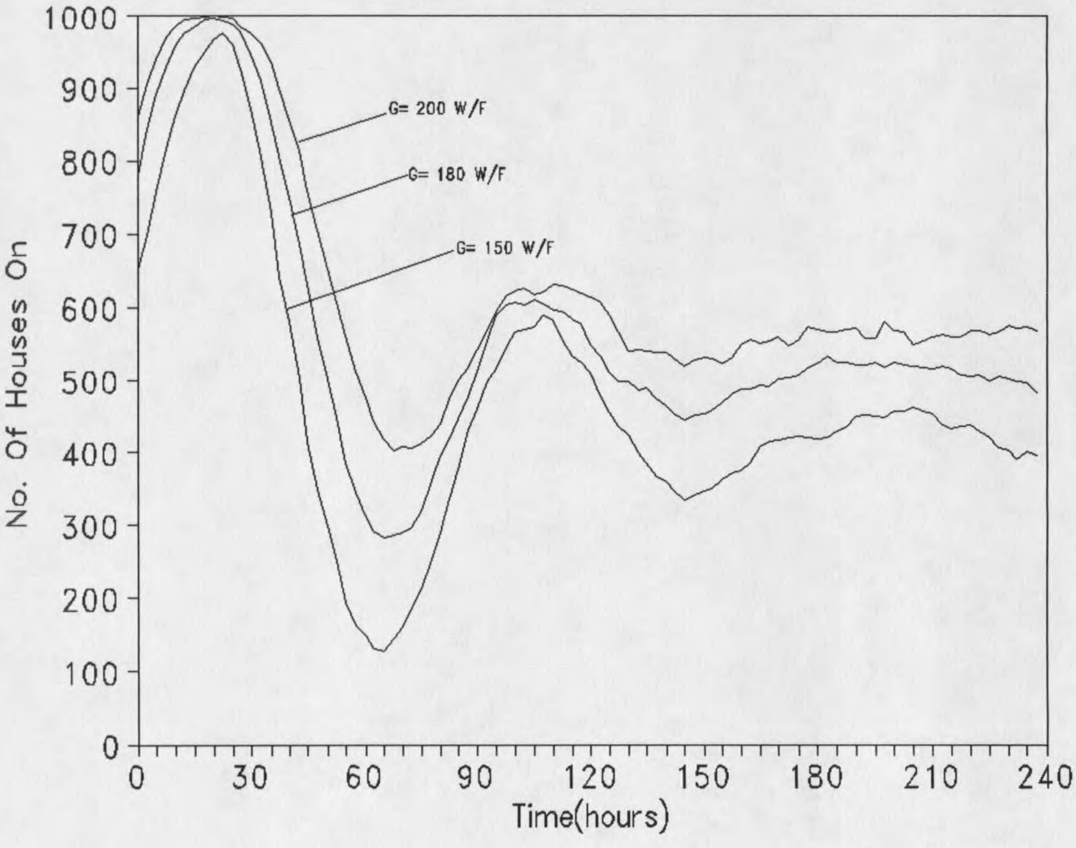

Fig. 18 Effect of change in conductance at ambient temperature of 10°F and after a power outage of 30 minutes.

the loss of heat energy to the environment is less, each house will stay on demanding power for a shorter period of time, therefore the number of houses demanding power would be less both when power is restored after an outage and under steady state conditions. Fig. 18 shows the simulated results for a 30 minutes outage at 10°F.

Electrical capacitance C of the R-C circuit is analogous to the thermal mass of the house. The size of the capacitance

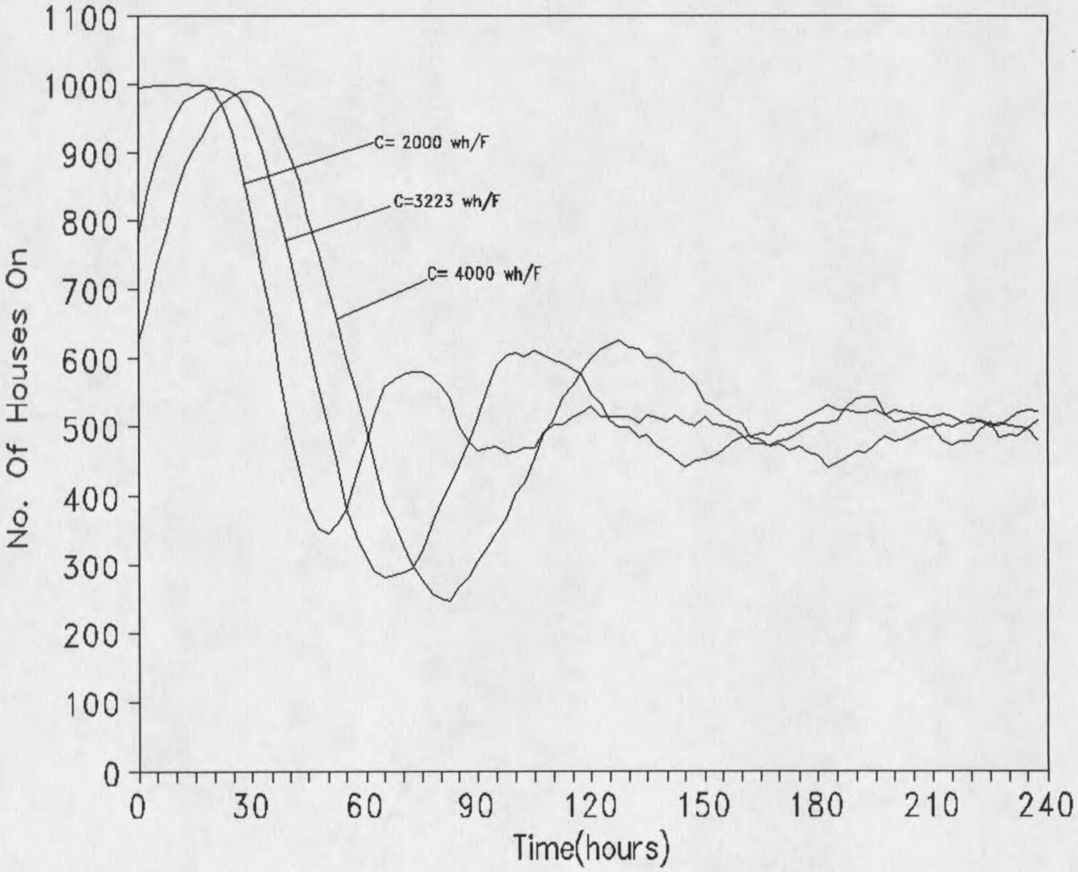

Fig. 19 Effect of change in capacitance at ambient temperature of 10°F and after a power outage of 30 minutes.

is a measure of the amount of electrical energy that can be stored. With a higher value of capacitance the houses will become slow in heating up and cooling down meaning that the on-time and off-time increase. Due to an increase in on-time of the house the peak current demand is delayed. This can be seen in Fig. 19.

With an increase in the value of the heat injected Q, houses get heated up faster. When power is restored after an outage, the power demand of the feeder increases because the

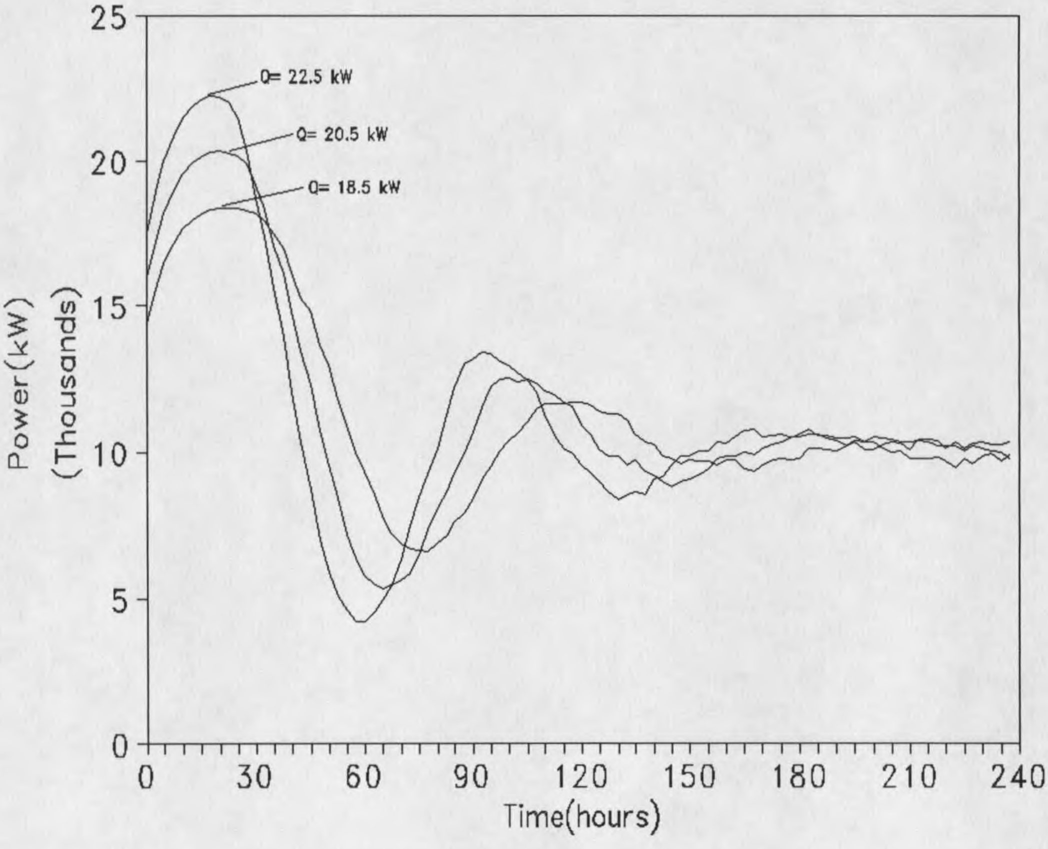

Fig. 20 Effect of change in heat injected into the house at ambient temperature of 10°F and after a power outage of 30 minutes.

furnace capacity of each house has increased. As seen in Fig 20, this produces a higher peak. Under steady state conditions the amount of electrical energy required to keep all the houses at a temperature within their thermostat setting is fixed and so a change in furnace has no effect on the aggregate steady state power demand.

Increase in thermostat set point has the effect of increase in the on-time and a decrease in off-time. This is better explained by an example at ambient temperature of -10°F.

For Set point = 67.2°F and using the mean values for other parameters

$$T_{on} = .95 \text{ Hr}$$

$$T_{off} = .47 \text{ Hr}$$

For Set point = 70.2°F

$$T_{on} = 1.03 \text{ Hr}$$

$$T_{off} = .45 \text{ Hr}$$

This means that with an increase in set point, energy is supplied for longer time and hence more houses will demand power as shown in Fig 21.

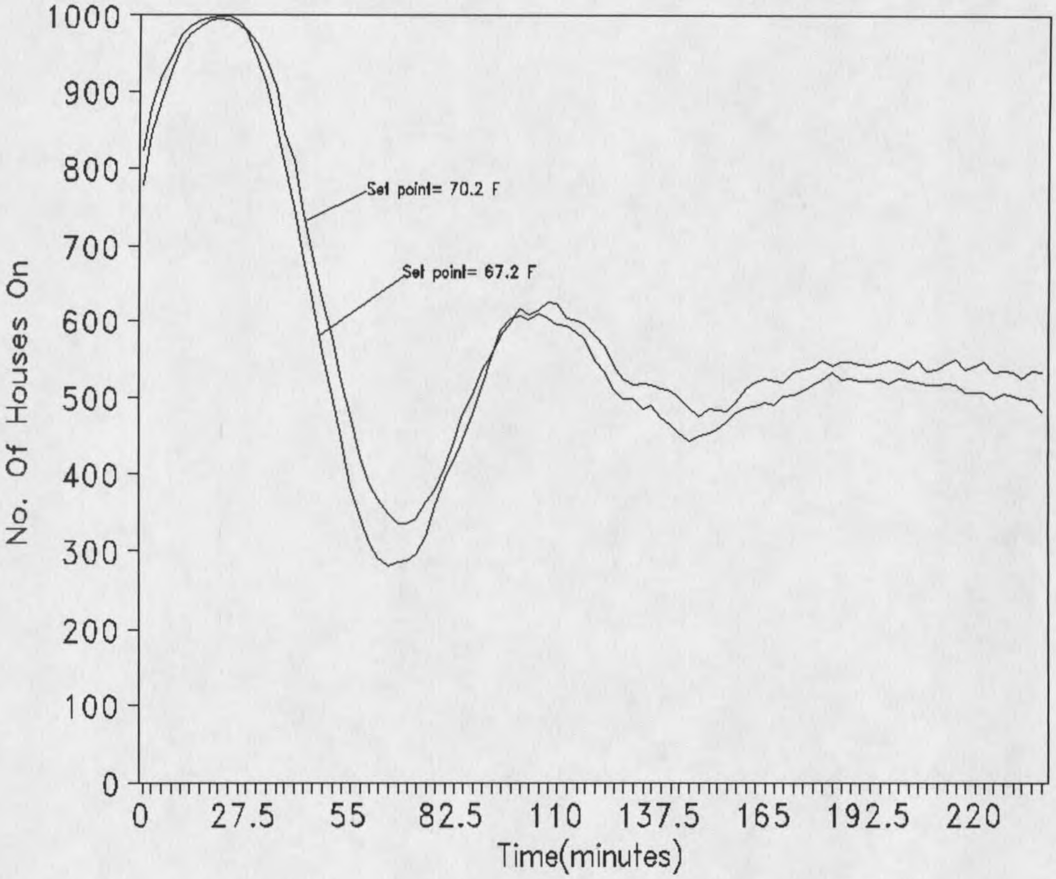

Fig. 21 Effect of change in set point at ambient temperature of 10°F and after a power outage of 30 minutes.

A smaller thermostat deadband would mean lower value of on-time and off-time. When power is restored more houses will be turned on because the lower setting of the thermostat has been raised. It is explained with an example.

Set point = 67.2°F

Deadband = 2.0°F

So, Upper setting = 67.2°F

and Lower setting = 65.2°F

Deadband is changed to 1.0°F

Then Upper setting = 67.2°F

Lower setting = 66.2°F

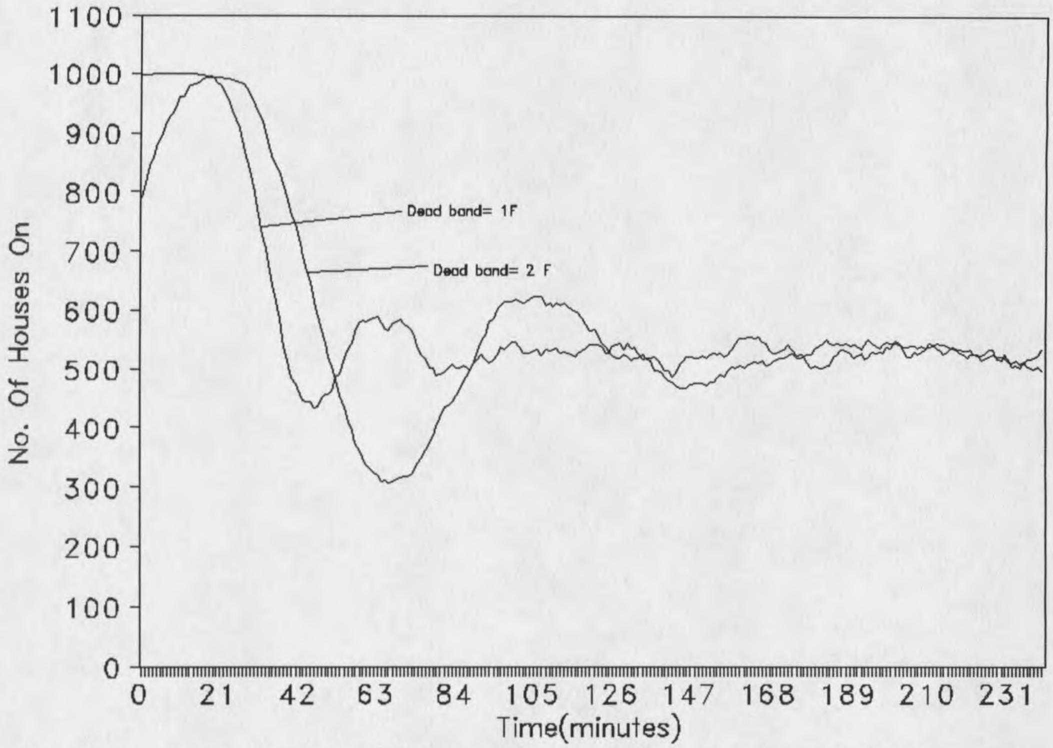

Fig. 22 Effect of change in dead band at ambient temperature of 10°F and after a power outage of 30 minutes.

When power is restored after an outage, there will be houses with temperature between 65.2°F and 66.2°F which will be the extra houses demanding power due to the change in thermostat deadband. Fig 22 shows more number of houses demanding power after an outage with a decrease in dead band.

Change in Voltage

Fig. 23 and Fig. 24 show the effect of voltage change on the power and the current supplied by the feeder. The electrical power is directly proportional to the square of the