



Frequency Dependence and Anisotropy of the Glass Transition T_g of $\text{Rb}_{0.52}(\text{ND}_4)_{0.48}\text{D}_2\text{PO}_4$

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FREQUENCY DEPENDENCE AND ANISOTROPY OF THE GLASS TRANSITION
 T_g OF $Rb_{0.52}(ND_4)_{0.48}D_2PO_4$

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Abstract The frequency dependence of the glass transition temperature T_g has been calculated from the Vogel-Fulcher law using dielectric data obtained in the 10^2 Hz to 10^{10} Hz region. The best fit was obtained with $\ln f_0 = 29$ and $T_0 = 38$ K. The anisotropy of T_g predicted recently by theory has been observed.

EXPERIMENTAL RESULTS AND DISCUSSION

Studies of the frequency-dependent dielectric properties of $Rb_{0.52}(ND_4)_{0.48}D_2PO_4$ at low frequency were done by Samara and Schmidt¹ and others^{2,3}. In this paper we report the real ϵ' and imaginary ϵ'' dielectric permittivity in the X-band microwave region for temperatures from 5 K to 180 K. Typical rounded cusp dependence for $\epsilon'(T)$ and narrow rounded maximum for $\epsilon''(T)$ were observed. Treating this maximum as the temperature T_g of the glass "transition", $T_g = 86$ K for $f = 9.3$ GHz when the microwave electric field is parallel to the c-axis of the $Rb_{0.52}(ND_4)_{0.48}D_2PO_4$ mixed crystal (FIGURE 1).

According to cluster models of proton glass⁴, short range interactions form partly ordered clusters imbedded in the frustrated proton system. The clusters have a mean relaxation time τ strongly related to their volume and temperature, and τ decreases rapidly with increasing temperature. According to another viewpoint, to be

explained in detail elsewhere⁵, the τ distribution is governed by effective diffusion of HPO_4 and H_3PO_4 defects. In either case, the

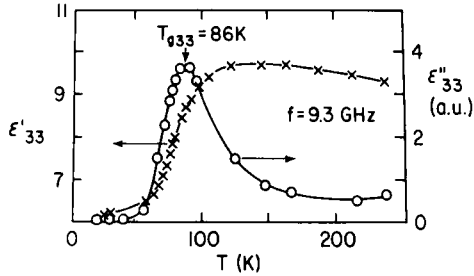


FIGURE 1 Temperature dependences of the real ϵ'_{33} and imaginary ϵ''_{33} parts of dielectric permittivity of 72% deuterated RADP.

mean τ is given by the Vogel-Fulcher law⁶ :

$$\tau^{-1} = f_0 \exp(-E/k(T-T_0)), \quad (1)$$

where f_0 and T_0 are scaling parameters and E is an activation energy. The frequency f_0 is the O-D...O deuteron intrabond transfer attempt frequency, and T_0 should be treated as the temperature below which the O-D...O deuteron system is "frozen". Courtens² proposed that Eq.(1) should be modified to the form:

$$\tau^{-1} = f_0 \exp(-E/k(T-T_0)^\alpha). \quad (2)$$

At the temperature giving maximum ϵ'' we can say that $\tau^{-1} = f$, where f is the measurement frequency and $T = T_g$. Then Eq.(2) gives the formula :

$$(\ln f_0 - \ln f)^{-1} = k(T_g - T_0)^\alpha / E. \quad (3)$$

Figure 2 shows the plot of Eq.(2) for $\alpha=2$, $\ln f_0=29$ and $T_0=38$ K, using our experimental point and low frequency measurements^{1,3} for ϵ''_{33} . The good agreement shows that the Eq.(2) form of the Vogel-Fulcher law describes the proton glass system in our crystal. The values of $\ln f_0$ and T_0 are practically the same as found by Courtens², $\ln f_0=28.5$ and $T_0=30$ K for $\text{Rb}_{0.38}(\text{ND}_4)_{0.62}\text{D}_2\text{PO}_4$. In terms of physical parameters, these results illustrate the rapid slowing down of dynamic processes with decreasing temperature, and depending on the

model adopted, the increase in cluster size⁴ or the increase in defect diffusion path length between creation and annihilation⁵.

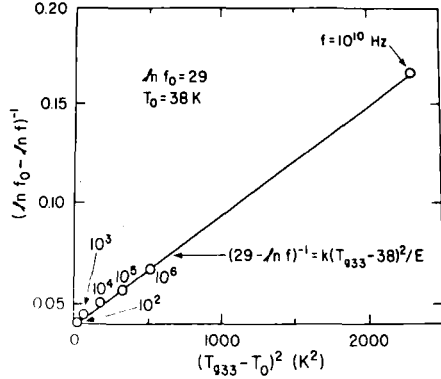


FIGURE 2 A plot of $(\ln f_0 - \ln f)^{-1}$ vs. $(T_{g33} - T_0)^2$ for $\ln f_0 = 29$, $T_0 = 38$ K and $\alpha = 2$.

Matsushita and Matsubara⁷ (MM) using a cluster theory⁴ predicted anisotropy of T_g - different values of T_g for susceptibility along the c and a axes. They introduced two order parameters, q_x and q_z , which give the temperatures T_{g11} and T_{g33} . Figure 3 shows that for $\text{Rb}_{0.52}(\text{ND}_4)_{0.48}\text{D}_2\text{PO}_4$ the ϵ'' maxima occur at different temperatures for microwave electric field parallel to the a and c axes. Our data show $T_{g11} = 82$ K and $T_{g33} = 86$ K, in accord with MM theory which gives $T_{g33} > T_{g11}$ for concentration $x < 0.5$. Further experiments are planned.

CONCLUSION

These experiments show that dielectric behavior for proton glasses obeys the Vogel-Fulcher law also when there is isotropic randomness (72 % deuteration) as well as cation randomness (48 % ND_4). In addition, the anisotropy of T_g predicted by Matsushita and Matsubara⁷ was observed.

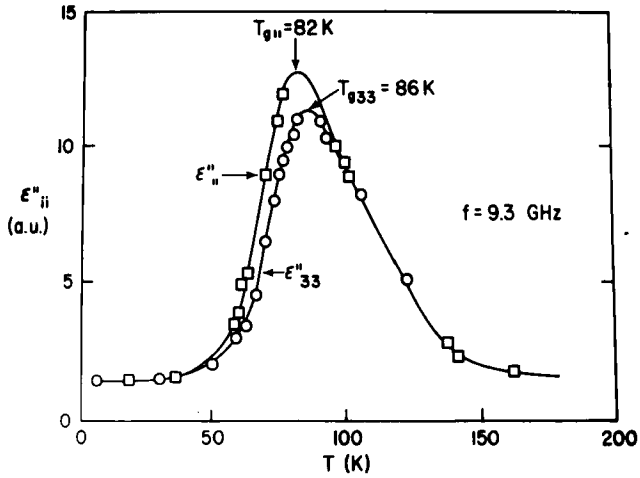


FIGURE 3 Temperature dependences of the imaginary part of electric permittivity in arbitrary units for two orientations of microwave electric field: ϵ''_{33} and ϵ''_{11} .

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